



# **CE 442**

## **Geotechnical Engineering Sessional II**



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## **Preface**

The substructure, often situated beneath ground level, plays a vital role in structures by transmitting the weight from the superstructure to the underlying soil or rock. It holds great significance in the context of all types of constructions. This laboratory manual elucidates the mechanism of load transfer from the superstructure to the foundation, outlines the requisite load-bearing capacity of the sub-soil for various foundation types, covers diverse settlement types and their calculations, and provides guidance on designing foundations with reinforcement. As an exercise, the manual also includes a building plan and a soil test report. The creation of this lab manual involved referencing geotechnical engineering literature and lecture notes, among other resources.

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# **Building Foundation, Bearing Capacity, Soil Settlement**

# Building Foundation

## Definition

The substructure or foundation is the part of a structure that is usually placed below the surface of the ground to transmit the load from the superstructure to the underlying soil or rock.

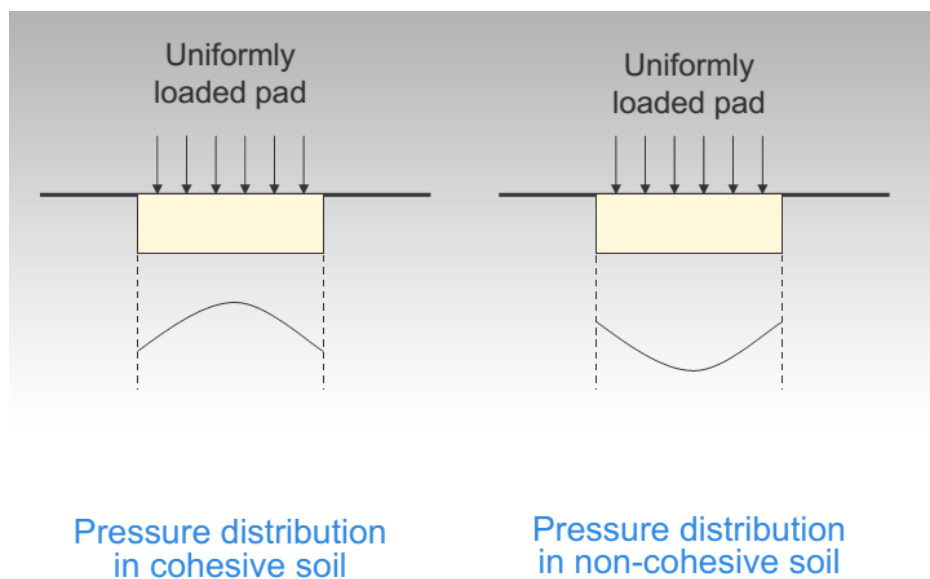
In addition, foundation also serves some other functions, such as:

- Prevent settlement (including differential settlement) of a structure.
- Prevent possible movement of structure due to periodic shrinkage and swelling of subsoil.
- Allow building over water or water-logged ground.
- Resist uplifting or overturning forces due to wind.
- Resist lateral forces due to soil movement.
- Underpin (support) existing or unstable structures.

## Factors to be Considered in Selecting Foundation Type

- Subsurface conditions
- Groundwater conditions
- Column loads and spacing, basements
- Site constraints
  - noise
  - vibrations
  - proximity to existing improvements, slope, channel
- Economics

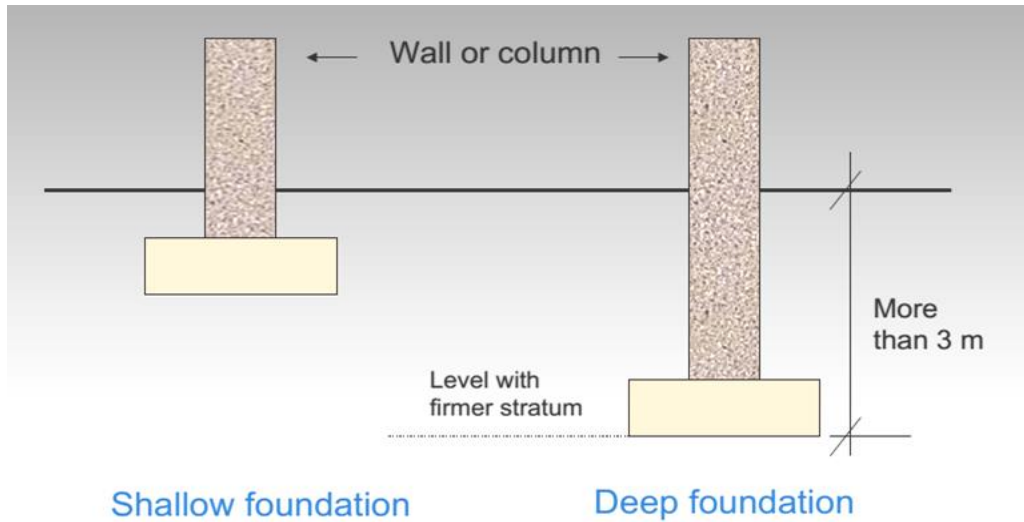
Loading condition of foundation  
(pressure distribution in different soil)



## General Foundation Types

- Shallow Foundations

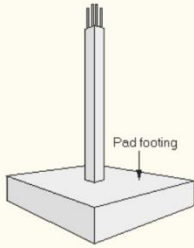
- Spread footings: isolated, continuous
- Strip Footing
- (Beam) Grillage Foundation
- Mats
- Deep Foundations



<p style="text-align: center;"><b>Pad foundation</b></p>	<p style="text-align: center;"><b>strip footing</b></p>	<p style="text-align: center;"><b>Raft foundation</b></p>	<p style="text-align: center;"><b>Pile foundation</b></p>
<p>Where suitable bearing strata are at a shallow depth, mass concrete pad footings can be used. It is also the most economical choice for the ground conditions. The depth of the pad allows dispersion of the load without the need for reinforcement.</p>	<p>Strip footings are used if individual pad footings would be too closely spaced. Strip footings can also be used on weak ground to reduce the bearing pressure.</p>	<p>Where the ground conditions are poor and the depth to a strong bearing strata is excessive, raft foundations are used to distribute the load over a large area.</p>	<p>Piles are used where the bearing strata at the foundation level are too weak to support the superstructure. Piles find support at a deeper, firmer level where the load is dispersed.</p>

## Pad footing

The purpose of a foundation is to transmit loads from the structure to the ground making sure that any settlement, either immediately after construction or during the intended life of the structure, is uniform and acceptably small.

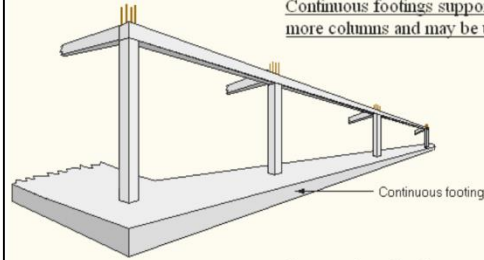


Where there is a good uniform bearing stratum at a relatively shallow depth, columns may be supported on independent pad foundations, (provided of course that the columns are spaced sufficiently far apart for adjacent pads not to overlap).

A good bearing stratum is one where the bearing capacity is adequate to support the foundation safely and economically.

## Continuous footings

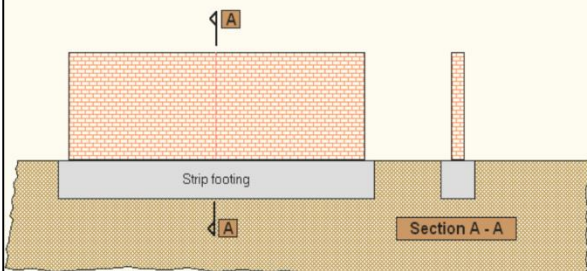
Continuous footings support two or more columns and may be used if :-



- close spacing of columns would lead to the overlap of individual pad footings
- the bearing capacity of the soil is variable
- differential settlement needs to be avoided

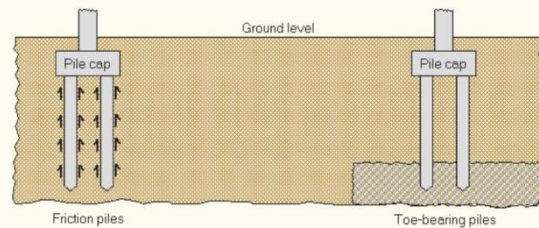
## Strip footings

Strip footings are continuous foundations carrying continuous loads, (for example walls constructed from brickwork, blockwork or reinforced concrete).



## Piled foundation

Where the cost of excavation to a good bearing stratum would be prohibitive, or where the stratum is not continuous, piled foundations may be used.



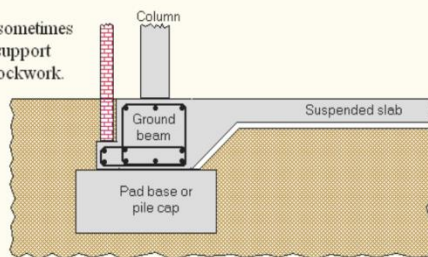
Piles can either rely on friction along their length

or, on end support from a good bearing stratum at some depth below ground level

## Beam foundation

When the upper layer of ground has such a low bearing pressure that it is incapable of sustaining the loads imposed on ground-floor slabs, the slabs are suspended and supported on ground beams.

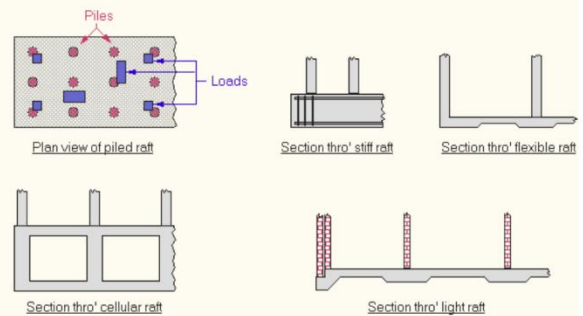
Ground beams sometimes include nibs to support brickwork or blockwork.



The beams are supported at column positions on pad foundations or pile caps.

## Rafts

There are a number of different forms of raft foundation but the common purpose is to spread a system of loads over a large area, thus giving a low linearly-imposed load on to the ground below.



## Shallow Foundation

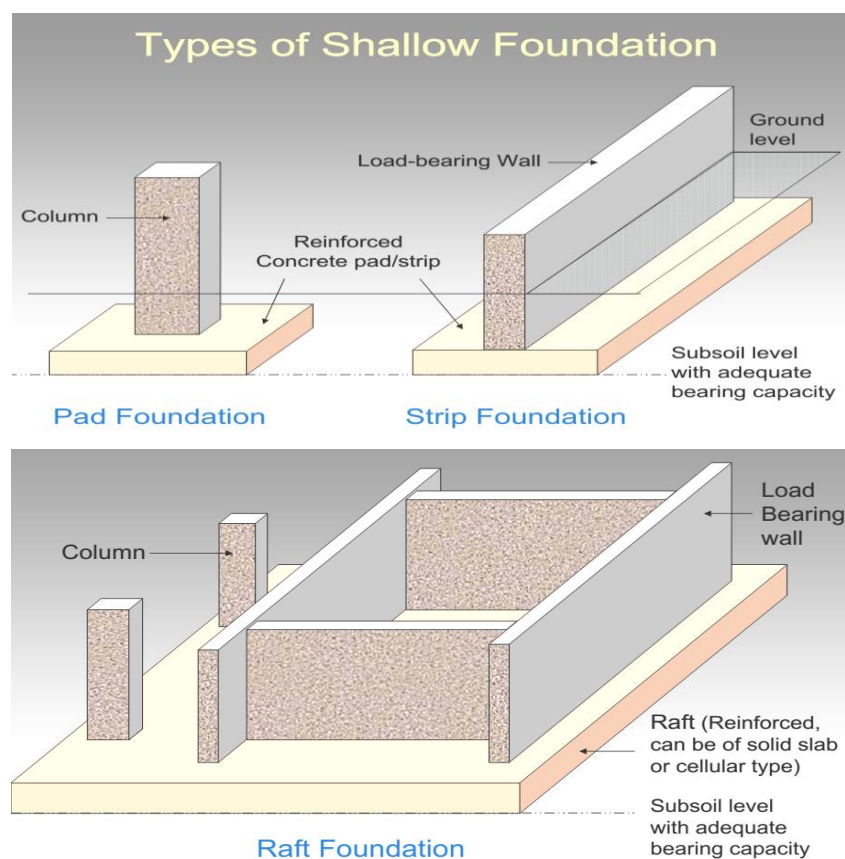
This type of foundation usually refers to those being rested on stratum with adequate bearing capacity and laid less than 3m below ground level. Common examples include pad, strip or raft foundations.

The selection of the right type of shallow foundation normally depends on the magnitude and disposition of the structural loads and the bearing capacity of subsoil. A combination of two or three type of shallow foundation in one single structure is not uncommon.

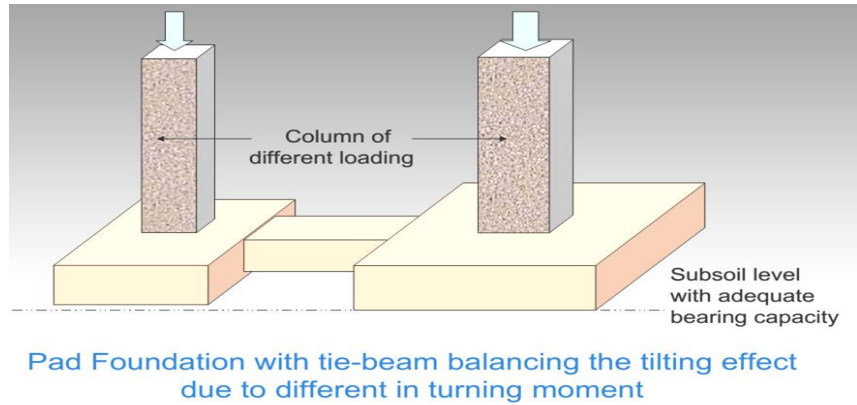
### Raft Foundation

Raft foundation is a large combined thick slab, designed to seat and support the whole or a large part of a structure.

A raft is usually used when subsoil is weak, or columns are closely located and with deviated loadings. It also serves as a transfer slab to combine and tie up all the vertical loading elements to the plate-form foundation. By doing so, differential settlement can be avoided.







## Deep Foundation

### Piled Foundation

Piled foundation is a form of foundation using piles to transfer the loads of a structure down to a firm soil stratum with sufficient loadtaking capacity.

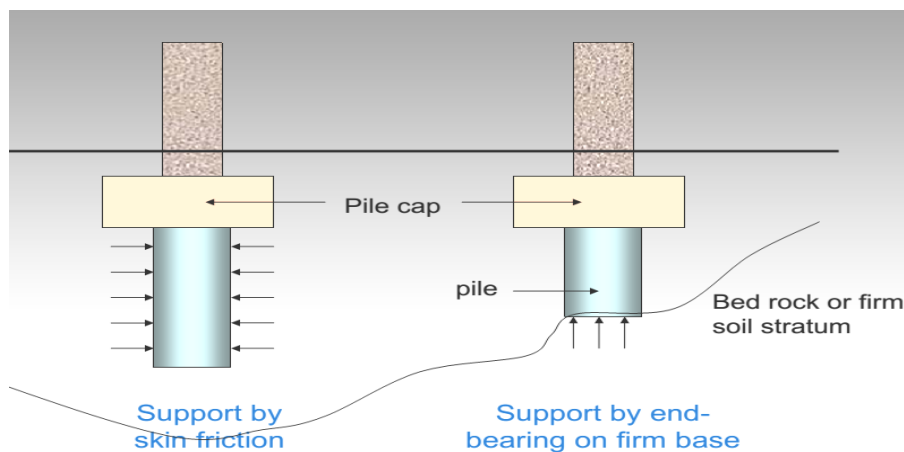
Materials for the piles can be of:

- Timber
- precast concrete (sometimes also prestressed)
- In-situ reinforced concrete
- steel piles in 'H' or circular section

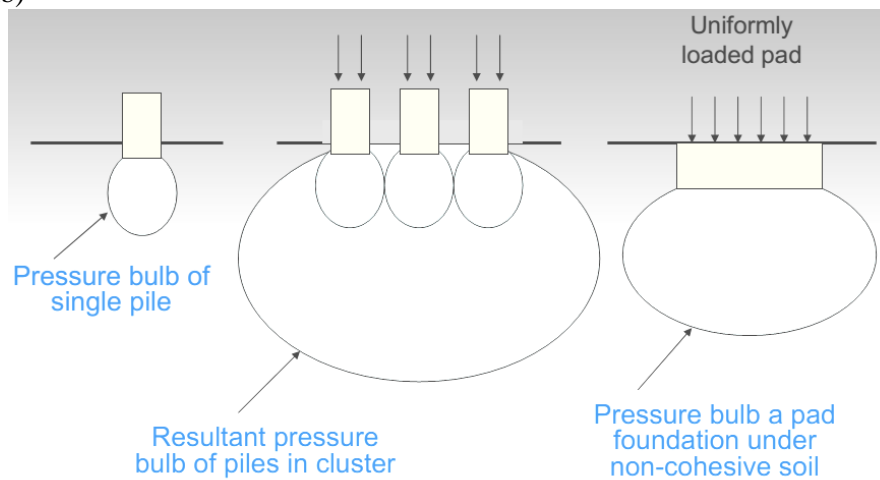
Load from a superstructure is transmitted to the subsoil either by:

**End-bearing**— load is support by resting onto a firm stratum such as bed-rock or stratum of subsoil with the required bearing capacity.

**Skin friction**— load is support by the frictional resistance so created between the contact surface of the pile and the embracing soil.



Loading condition of foundation :  
(pressure bulb)



## BEARING CAPACITY

### Introduction

All civil engineering structures impose a loading on the underlying soil (or rock). The lowest part of the structure, usually lying below the ground level, which transmits the load to the supporting soil/rock strata, is known as foundation. The ability of the underlying soil to bear the load of the foundation without overstressing the soil in terms of either shear failure or excessive settlement is termed as bearing capacity of soil. This is often termed as bearing capacity of foundation.

The bearing capacity of a soil depends mainly on the types of foundation encountered by the soil. Foundations of structures are basically of two types; shallow and deep. The classification indicates the depth of foundation installation and the depth of the soil strata providing most of the support. A number of definitions are relevant in the context of types of foundation and bearing capacity.

### Basic Definitions

**Shallow Foundation:** Shallow foundation is one that is placed on a firm soil near the ground and beneath the lowest part of the superstructure. e.g. spread footing or simply footing, mat or raft etc. The most useful definition of a shallow foundation refers to the founding depth being less than the breadth of the foundation. However, for wide foundation this is not acceptable. It is sensible to limit the term shallow to mean less than 3 m or less than the breadth of the foundation footing.

**Deep Foundation:** Deep foundation is one that transmits the load of the structure considerably at a greater depth below the lowest part of the superstructure. e.g. pile, pier, caissons etc.

**Foundation Soil or Bed:** The soil to which loads are transmitted from the base of the structure.

**Footing:** An enlarged base of the structure to distribute the column or wall load to ground at a compatible strength and deformation characteristics of foundation soil.

**Mat or Raft:** This is characterized by the feature of framing columns or walls into the footing in two directions. Any number of columns can be accommodated with as low as four columns.

**Bearing Capacity:** This is a general term used to describe, the load carrying capacity of a foundation soil that enables to bear and transmit loads from a structure.

**Ultimate Bearing Capacity:** Maximum pressure that a foundation soil can withstand without the occurrence of shear failure of the foundation.

**Gross Bearing Capacity:** The bearing capacity inclusive of the pressure exerted by the weight of the soil standing on the foundation (called the surcharge pressure) is known as gross bearing capacity.

**Net bearing capacity:** Gross bearing capacity minus the original overburden pressure or surcharge pressure at the foundation level; obviously, this will be the same as the gross capacity when the depth of foundation is zero.

**Safe bearing capacity:** Net ultimate bearing capacity divided by a factor of safety. The factor of safety in foundation may range from 2 to 4, depending upon the importance of structure, and the soil profile at the site. The factor of safety should be applied to the net ultimate bearing capacity, and the surcharge pressure should then be added to get the safe bearing capacity.

It is thus the maximum intensity of loading that can be transmitted to the soil without the risk of shear failure, irrespective of the settlement that may occur.

**Allowable bearing capacity/pressure:** The maximum allowable net loading intensity on the soil at which the soil neither fails in shear nor undergoes excessive or intolerable settlement detrimental to the structure. The conventional design of a foundation is based on the concept of bearing capacity or allowable bearing pressure.

### **Criteria for the Determination of Bearing Capacity**

The criteria for the determination of bearing capacity of a foundation are based on the requirements for the stability of the foundation. These are stated as follows:

- **Shear failure of a foundation soil or bearing capacity failure.** This is associated with plastic flow of the soil material beneath the foundation, and lateral expulsion of the soil from underneath the footing.
- **The probable settlements, differential as well as total,** of the foundation must be limited to safe, tolerable and acceptable magnitude.

### **Factors Affecting Bearing Capacity**

Bearing capacity is governed by a number of factors. The following are the some of the important factors that affect the bearing capacity.

- Nature of soil and its physical and engineering properties
- Nature of the foundation and other details such as the size, shape, depth at which the foundation is located and rigidity of the structure
- Total and differential settlement that the structure can withstand without functional failure

- Location of ground water table relative to the level of foundation
- Initial stresses, if any.

In view of the wide variety of factors that affect the bearing capacity, a systematic study of the factors involved is necessary for proper understanding.

### **Bearing Capacity of Shallow Foundations**

The following methods are available for the determination of bearing capacity of a shallow foundation:

- Bearing capacity tables in various building codes
- Analytical methods
- Plate bearing tests
- Penetration tests
- Model tests and prototype tests
- Laboratory tests

**Bearing capacity tables** have been evolved by certain agencies and incorporated in building codes. They are mostly based on past experience and some investigations.

**Various analytical approaches are available.** Usually they are expressed in terms of equations commonly known as bearing capacity equation. The prominent of these are given by:

- Rankine (1857)
- Pauker (1889)
- Bell (1915)
- Prandtl (1921)
- Schleicher (1926)
- Fellinius (1939)
- Terzaghi (1943)
- Meyerhof (1951)
- Skempton (1951)
- Hansen (1961)
- Balla (1962)
- Vesic (1975)

**Plate bearing tests** are load tests conducted in the field on a plate. These involve effort and expense. There are some limitations also.

**Penetration tests** are conducted with devices known as penetrometers which measure the resistance of soil to penetration. This is correlated to bearing capacity.

**Model and prototype tests** are very cumbersome and costly, and are not usually practicable.

**Laboratory tests** are simple, may be useful in arriving bearing capacity especially of pure clays.

### **Analytical Method: Bearing Capacity Equations**

The following analytical approaches are available.

- The theory of elasticity: Schleicher's method
- The classical earth pressure theory: Rankine, Pauker, Bell
- The theory of Plasticity: Fellinius, Prandlt, Terzaghi, Meyerhof, Skempton, Hansen, Balla, Vesic

### Terzaghi's Theory

Terzaghi (1948) developed a bearing capacity theory, assuming a failure surface consisting of three wedges (I, II and III) as illustrated in Fig.1 He considers a strip footing with rough base placed at a depth  $D_f$  on a homogeneous and isotropic soil mass. In the analysis the shearing resistance of the soil above the base (AA' and BB' in Fig. 1) of the footing is neglected, but the effect of soil weight above the base is considered by superimposing an equivalent surcharge of intensity  $q = \gamma D_f$ . The development of the failure surface in the soil is governed by the general shear failure.

The soil immediately beneath the foundation forms a wedge (zone I) which moves downwards. The movement of wedge forces the soil aside and produces two zones of shear (zone II and zone III), consisting of a radial shear zone (zone II) and a linear shear zone (zone III). Zone I is considered to be at Rankine active state, zone II under radial shear and zone III at Rankine passive state. On the verge of failure,  $\Sigma V = 0$ , thus

$$q_{ult} B = 2 P_p + 2 BC \cdot c \sin\phi$$

Substituting  $BC = B/2 \cdot \cos\phi$ ,

$$q_{ult} B = 2 P_p + BC \cdot \tan\phi$$

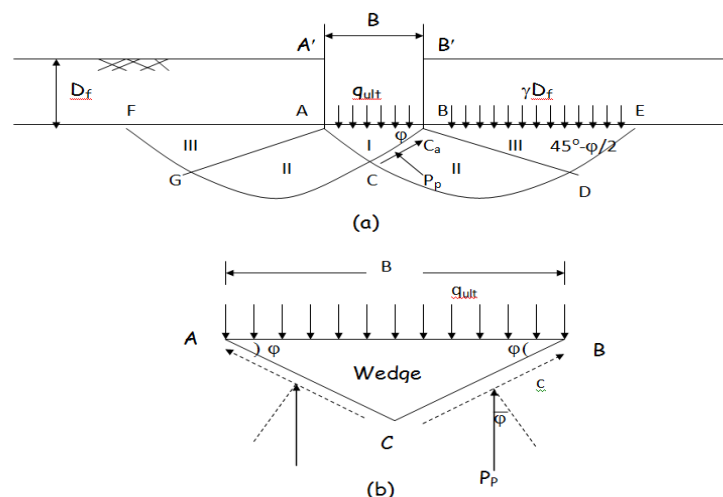


Fig.1.1 Terzaghi's bearing capacity theory; (a) failure mechanism; (b) forces on the elastic wedge

The value of  $P_p$  has been represented as the vector sum of three components, (i) cohesion, (ii) surcharge and (iii) weight of the soil. Terzaghi assumed the method of superposition to be valid presented the unit ultimate bearing capacity in the form

$$q_{ult} = cN_c + \frac{1}{2} B\gamma N_\gamma + qN_q$$

Where,  $N_c$ ,  $N_\gamma$  and  $N_q$  are nondimensional bearing capacity factors and functions only of the angle of internal friction,  $\phi$ .

$$N_q = \frac{\exp\left[2\left(\frac{3\pi}{4} - \frac{\phi}{2}\right)\tan\phi\right]}{2 \cos^2\left(\frac{\pi}{4} + \frac{\phi}{2}\right)}$$

$$N_c = \cot\phi (N_q - 1)$$

$$N_\gamma = \frac{1}{2} \cdot \tan\left(\frac{K_{p\gamma}}{\cos^2\phi} - 1\right)$$

A close approximation of  $K_{p\gamma}$  is given by

$$K_{p\gamma} = 3 \tan^2\left[45 + \left(\frac{\phi+33}{2}\right)\right]$$

Terzaghi's bearing capacity factors are shown in Fig. 1.2

These bearing capacity factors are valid for strip footing only and require to be adjusted for rectangular and circular footings as follows. It is understood that square footing is a special case of rectangular footing where length of the footing,  $L$  equals to its width  $B$ .

#### Rectangular Footing:

$$\begin{aligned} N_{c \text{ rect}} &= N_{c \text{ strip}} (1 + 0.3B/L) \\ N_{\gamma \text{ rect}} &= N_{\gamma \text{ strip}} (1 - 0.2B/L) \\ N_{q \text{ rect}} &= N_{q \text{ strip}} \end{aligned}$$

#### Square Footing:

$$\begin{aligned} N_{c \text{ square}} &= 1.3 N_{c \text{ strip}} \\ N_{\gamma \text{ square}} &= 0.8 N_{\gamma \text{ strip}} \\ N_{q \text{ square}} &= N_{q \text{ strip}} \end{aligned}$$

#### Circular Footing:

$$\begin{aligned} N_{c \text{ circle}} &= 1.3 N_{c \text{ strip}} \\ N_{\gamma \text{ circle}} &= 0.6 N_{\gamma \text{ strip}} \\ N_{q \text{ circle}} &= N_{q \text{ strip}} \end{aligned}$$

As such, the following bearing capacity equations are used to estimate the ultimate bearing capacity of soil.

$$\text{Strip footing: } q_{ult} = cN_c + \frac{1}{2}B\gamma N_\gamma + qN_q$$

$$\text{Square footing: } q_{ult} = 1.3cN_c + 0.4 B\gamma N_\gamma + qN_q$$

$$\text{Circular Footing: } q_{ult} = 1.3cN_c + 0.3 B\gamma N_\gamma + qN_q$$

Recent research works reveal that the values of  $N_c$ ,  $N_q$  and  $N_\gamma$  given by Terzaghi are conservative and the following formulas may be used for the computation of bearing capacity factors.

$$N_q = \tan^2\left(45 + \frac{\phi}{2}\right) e^{\pi \tan\phi}$$

$$N_c = (N_q - 1) \cot\phi$$

$$N_\gamma = 1.5(N_q - 1)\tan\phi$$

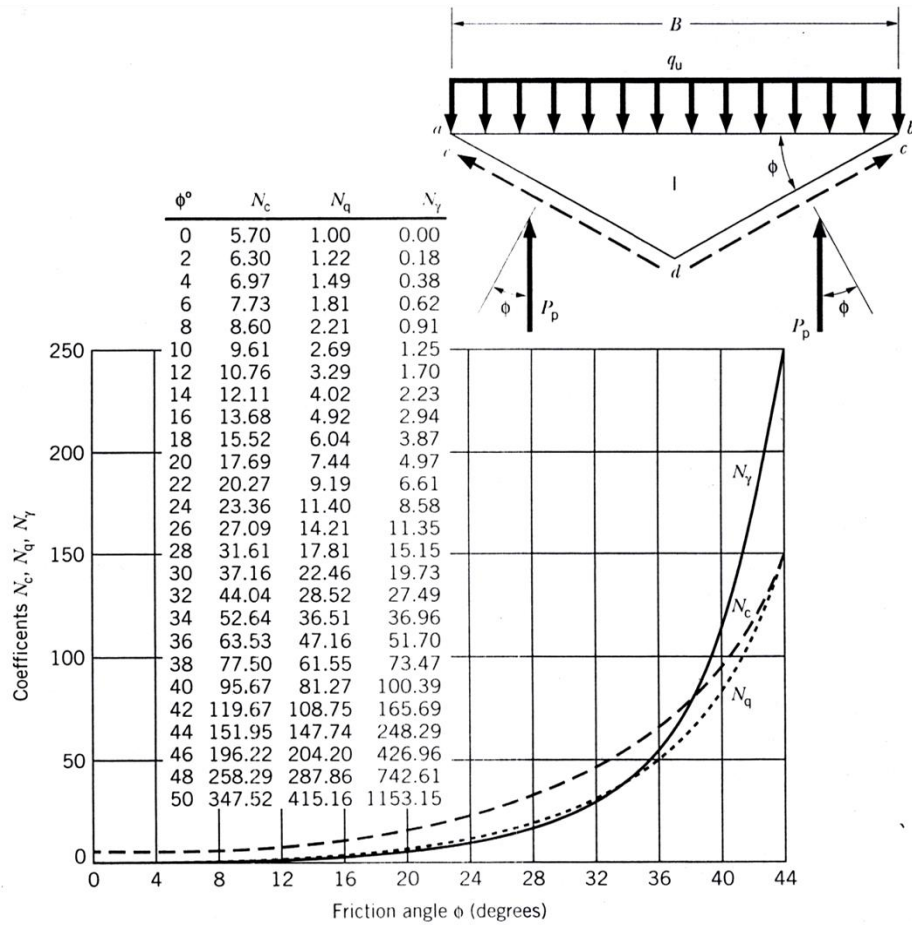


Fig. 1.2. Terzaghi's bearing capacity factors

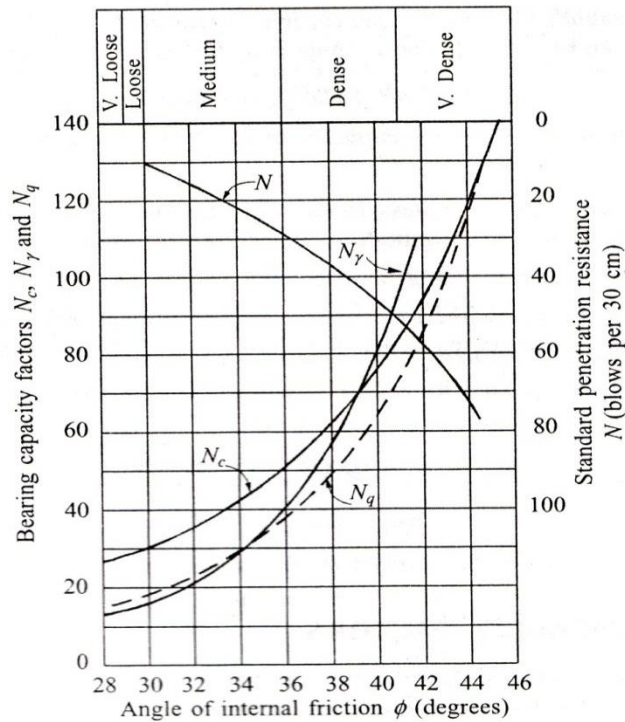


Figure. 1.3 Terzaghi's general bearing capacity factors against SPT values for cohesionless soils

Peak, Hanson and Thornburn proposed a chart for practical use where bearing capacity factors can be obtained against SPT values for cohesionless soil. The SPT values are however to be corrected for overburden and water table. The chart is presented in Fig. 1.3

### Meyerhof's Theory

Meyerhof (1951) considered the effects of shearing resistance within the soil above foundation level, the shape and roughness of foundation, and derived a general bearing capacity equation. According to Meyerhof,

$$\text{For vertical Load: } q_{ult} = cN_c S_c d_c + \frac{1}{2} B \gamma N_\gamma S_\gamma d_\gamma + q N_q S_q d_q$$

$$\text{For inclined load: } q_{ult} = cN_c S_c d_c i_c + \frac{1}{2} B \gamma N_\gamma S_\gamma d_\gamma i_\gamma + q N_q S_q d_q i_q$$

Where,

$$N_q = \exp^{\pi \tan \phi} \tan^2(\pi/4 + \phi/2)$$

$$N_c = (N_q - 1) \cot \phi$$

$$N_\gamma = (N_q - 1) \cdot \tan(1.4\phi)$$

S, d and i's are known as shape, depth and load inclination factors respectively to be used along with the bearing capacity factors  $N_c$ ,  $N_\gamma$  and  $N_q$  as indicated by their subscript. The bearing capacity factors  $N_c$ ,  $N_\gamma$  and  $N_q$  as obtained by Meyerhof's theory are presented in Fig. 3.11. The other associated factors are given in Table 3.2. Meyerhof also suggested considering the



reduced footing dimensions to account for load eccentricity in calculating ultimate bearing capacity. Accordingly, modified length,  $L'$  and width,  $B'$  of the footing are given by

$$L' = L - 2e_x; \text{ and } B' = B - 2e_y$$

Where,  $e_x$  and  $e_y$  represents the load eccentricity in longer (along the length  $L$ ) and shorter (along the width  $B$ ) directions respectively. He also suggested the use of plain strain  $\phi$  in the bearing capacity equations. The triaxial  $\phi$  should be adjusted to obtain plain strain  $\phi$  using the formula:  $\phi_{ps} = (1.1 - 0.1B/L) \phi_{\text{triaxial}}$

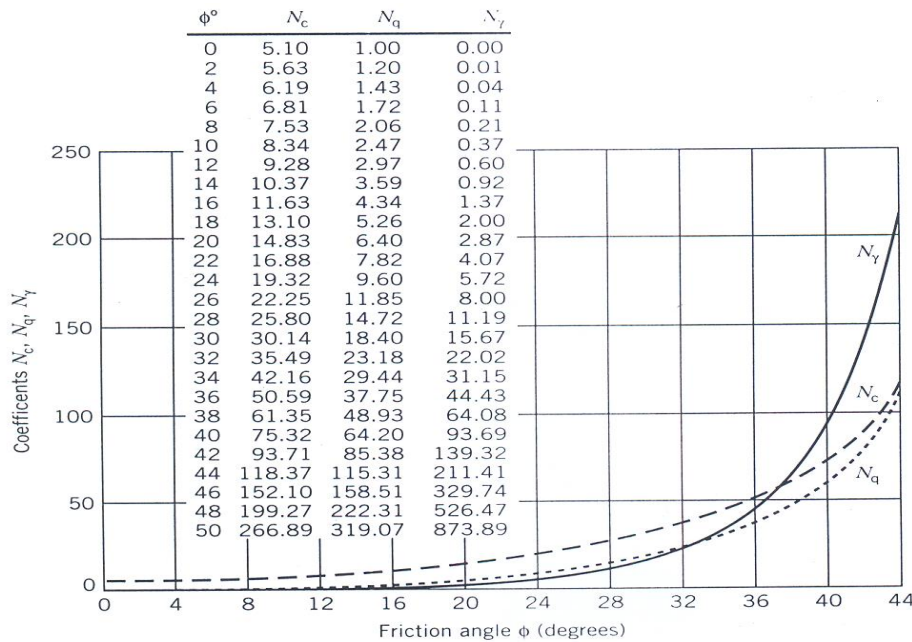


Fig. 1.4. Meyerhof's bearing capacity factors

Table: Meyerhof's factors for shape, depth and load inclination (after Cernica, 1995)

Friction, angle $\phi$	Shape factors	Depth factors	Inclination factors
Any $\phi$	$S_c = 1 + 0.2K_P B/L$	$d_c = 1 + 0.2\sqrt{K_P} D/B$	$i_c = i_q = (1 - \alpha/90^\circ)^2$
For $\phi = 0^\circ$	$S_\gamma = S_q = 1.0$	$d_\gamma = d_q = 1.0$	$i_\gamma = 1.0$
For $\phi \geq 10^\circ$	$S_\gamma = S_q = 1 + 0.1K_P B/L$	$d_\gamma = d_q = 1 + 0.1\sqrt{K_P} D/B$	$i_q = (1 - \alpha/\phi)$

$K_P = \tan^2(45^\circ + \phi/2)$

$\alpha =$  angle of resultant measured from vertical axis.

### Skempton's Bearing Capacity Equation for Clay Soil

Skempton (1951) proposed equations for bearing capacity of footings founded on purely cohesive soils based on extensive investigations. According to him the bearing capacity factor

$N_c$  is a function of the depth of foundation and also of its shape. The equation for net ultimate bearing capacity,  $q_{\text{net-ult}}$  is as follows:

$$q_{\text{net-ult}} = cN_c \quad (3.36)$$

The bearing capacity factor,  $N_c$  is given by:

**For strip footing:**

$$N_c = 5(1 + 0.2 D_f/B) \quad (3.37)$$

With a limiting value of  $N_c$  of 7.5 for  $D_f/B$  greater than 2.5.

**For square and circular footings:**

$$N_c = 6(1 + 0.2 D_f/B) \quad (3.38)$$

With a limiting value of  $N_c$  of 9.0 for  $D_f/B$  greater than 2.5  $B$  is the width of strip, side of square or diameter of a circular footing.

**For rectangular footings:**

$$N_c = 5(1 + 0.2 B/L) (1 + 0.2 D_f/B) \quad \text{for } D_f/B \leq 2.5 \quad (3.39)$$

And

$$N_c = 7.5(1 + 0.2 B/L) \quad \text{for } D_f/B > 2.5. \quad (3.40)$$

Where,  $B$  and  $L$  are breadth and length respectively, of the rectangular footing. Skempton's bearing capacity factor  $N_c$  for different shapes and depths of foundation can be obtained directly from Fig. 3.14

Table: Comparative statement of bearing capacity factors

$\phi^\circ$	Terzaghi			Meyerhof			Hansen		
	$N_c$	$N_q$	$N_\gamma$	$N_c$	$N_q$	$N_\gamma$	$N_c$	$N_q$	$N_\gamma$
0	5.70	1.00	0.00	5.10	1.00	0.00	5.10	1.00	0.00
2	6.30	1.22	0.18	5.63	1.20	0.01	5.63	1.20	0.01
4	6.97	1.49	0.38	6.19	1.43	0.04	6.19	1.43	0.05
6	7.73	1.81	0.62	6.81	1.72	0.11	6.81	1.72	0.11
8	8.60	2.21	0.91	7.53	2.06	0.21	7.53	2.06	0.22
10	9.61	2.69	1.25	8.34	2.47	0.37	8.34	2.47	0.39
12	10.76	3.29	1.70	9.28	2.97	0.60	9.28	2.97	0.63
14	12.11	4.02	2.23	10.37	3.59	0.92	10.37	3.59	0.97
16	13.68	4.92	2.94	11.63	4.34	1.37	11.63	4.34	1.43
18	15.52	6.04	3.87	13.10	5.26	2.00	13.10	5.26	2.08
20	17.69	7.44	4.97	14.33	6.40	2.37	14.83	6.40	2.95
22	20.27	9.19	6.61	16.88	7.82	4.07	16.88	7.82	4.13
24	23.36	11.40	8.58	19.32	9.60	5.72	19.32	9.60	5.75
26	27.09	14.21	11.35	22.25	11.85	8.00	22.25	11.85	7.94
28	31.61	17.81	15.15	25.80	14.72	11.19	25.80	14.72	10.94
30	37.16	22.46	19.73	30.14	18.40	15.67	30.14	18.40	15.07
32	44.04	28.52	27.49	35.49	23.18	22.02	35.49	23.18	20.79
34	52.64	36.51	36.96	42.16	29.44	31.15	42.16	29.44	28.77
36	63.53	47.16	51.70	50.59	37.75	44.43	50.59	37.75	40.05
38	77.50	61.55	73.47	61.35	48.93	64.08	61.35	48.93	56.18
40	95.67	81.27	100.39	75.32	64.20	93.69	75.32	64.20	79.54
42	119.67	108.75	165.69	93.71	85.38	139.32	93.71	85.38	113.96
44	151.95	147.74	248.29	118.37	115.31	211.41	118.37	115.31	165.58
46	196.22	204.20	426.96	152.10	158.51	329.74	152.10	158.51	244.65
48	258.29	287.86	742.61	199.27	222.31	526.47	199.27	222.31	368.68
50	347.52	415.16	1153.15	266.89	319.07	873.89	266.89	319.07	568.59

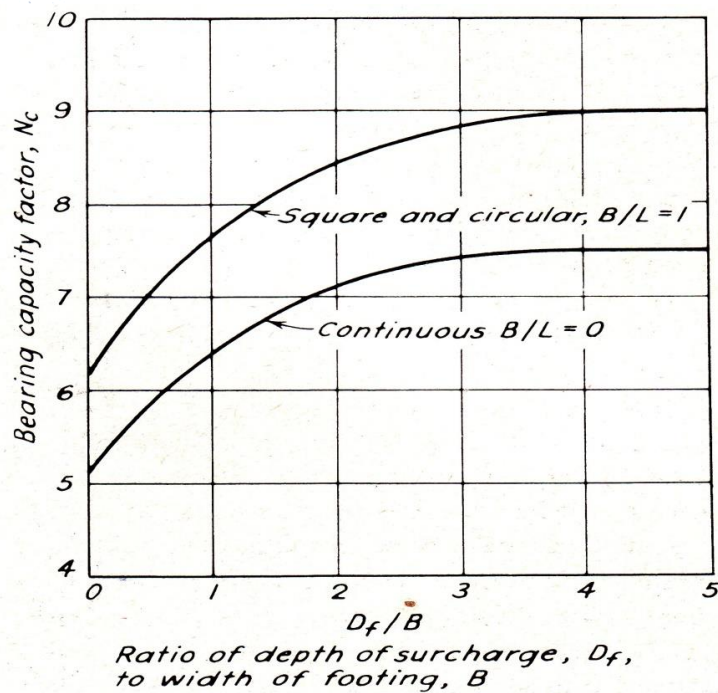


Fig. 1.5 Skempton's bearing capacity factors for clay soils

## Effect of Water Table on Bearing Capacity

The general bearing capacity equation is based on the assumption that the water table is located well below the foundation level. The equation contains unit weight,  $\gamma$ , cohesion,  $c$  and the bearing capacity factors,  $N_c$ ,  $N_\gamma$  and  $N_q$  that depend on the value of  $\phi$ . As such, some modifications are necessary in the formulation to account for the effect of water table.

In the general equation there are two terms which are affected by water table movement, (i) the soil weight component that is,  $\frac{1}{2}B \cdot \gamma \cdot N_\gamma$ ; and (ii) the surcharge component,  $\gamma D_f \cdot N_q$ .

Let us consider three locations of water table, as illustrated in Fig. 1.6

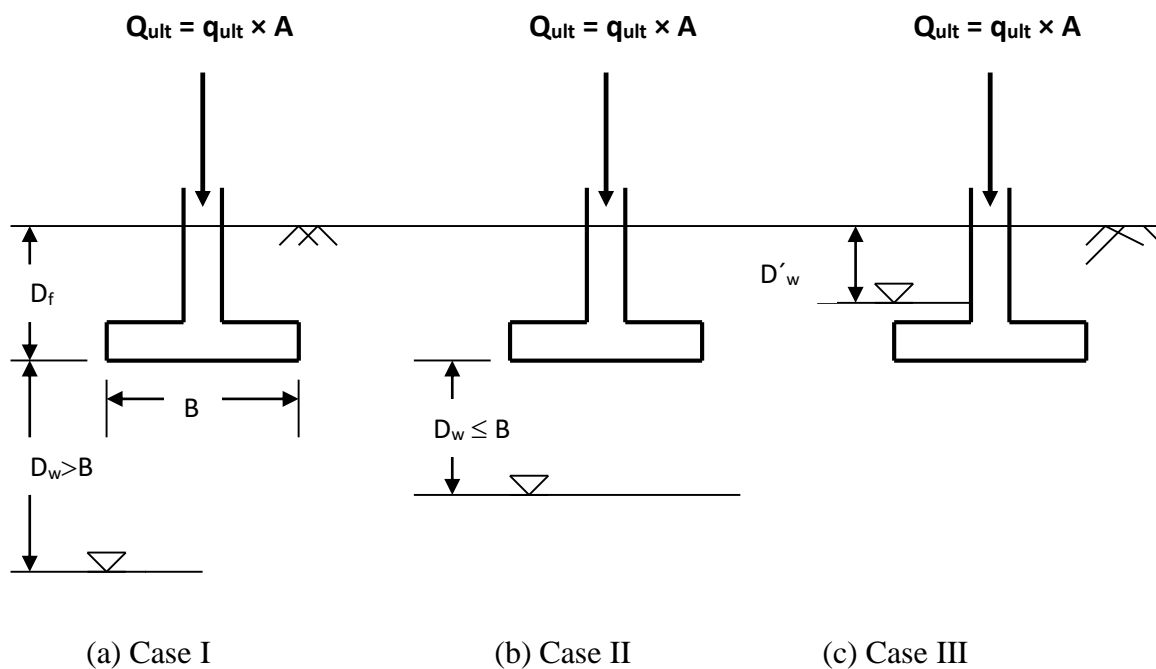


Fig. 1.6 Effect of water table and correction factors

**Case I:** When the water table is well below the foundation, that is  $d_w \geq B$ . For this case no correction is needed for both the components.

**Case II:** When the water table is anywhere from the base of the footing to a level well below the foundation, that is,  $0 \leq d_w \leq B$ . In this case, only the weight component is affected; whereas surcharge component remains unaffected. The aspect can be considered by substituting an equivalent unit weight  $\gamma_e$  in place of  $\gamma$ . That is,

$$\gamma_e = [d_w \gamma + (B - d_w) \gamma'] / B$$

or,

$$\gamma_e = \gamma' + d_w / B \cdot (\gamma - \gamma') \quad (3.41)$$

Case III. When the water table is anywhere between the ground surface and the base of the footing, that is  $0 \leq d'_w \leq D_f$ . In this case both the components are affected. For the surcharge component, the equivalent surcharge is

$$q = d'_w \gamma + (D_f - d'_w) \gamma' \quad (3.42)$$

For the soil weight component, the required substitution in the formula is  $\gamma'$  in place of  $\gamma$  in the term  $\frac{1}{2} B \gamma N_\gamma$ . Teng(1962) suggested water table correction factors, as the unit weight of soil as 50% of its bulk unit weight. Considering case III, when the water table is at the ground surface,  $d'_w/D_f = 0$  and  $\gamma = \gamma'$ . While water table is at the base of the footing  $d'_w/D_f = 1$  and  $\gamma = \gamma_{sat}$ . This suggests a correction factor to have a value of 0.5 at  $d'_w/D_f = 0$  and 1.0 at  $d'_w/D_f = 1$ . The general expression assuming linear variation is  $R'_w = \frac{1}{2}(1 + d'_w/D_f)$ .

Considering case II, for  $d_w/B = 0$ , the correction factor is 0.5 when water table is at the base ; for  $d_w/B = 1$ , the correction factor should be 1.0. The general expression is for correction factor is  $R_w = \frac{1}{2}(1 + d_w/B)$ . Hence, the bearing capacity formula takes the form

$$Q = cN_c + \frac{1}{2} R_w \cdot B \cdot \gamma \cdot N_\gamma + R'_w \cdot q \cdot N_q \quad (3.43)$$

Case I requires no correction for water table.

### **Effect of Layering of Soil**

When footing rests on a multilayer deposit, Bowles recommends that the ultimate bearing capacity of the footing be determined using average values of cohesion,  $c_{av}$  and the angle of internal friction  $\phi_{av}$ . The average values are computed over a depth H below the base of the footing, where:

$$H = \sum_{i=1}^n h_i = 0.5B \tan\left(45 + \frac{\phi}{2}\right) \quad (3.44a)$$

$c_{av}$  and  $\phi_{av}$  are given by

$$c_{av} = \frac{\sum c_i h_i}{\sum h_i} \quad (3.44b)$$

$$\tan(\phi_{av}) = \frac{\sum h_i \tan \phi_i}{\sum h_i} \quad (3.44c)$$

If necessary any value of  $h_i$  may be multiplied by a suitable weighing factor. Average parameters should be determined, Fig. 1.7 , by trial and error, since the term H used in the equation itself dependent on  $\phi_{av}$ .

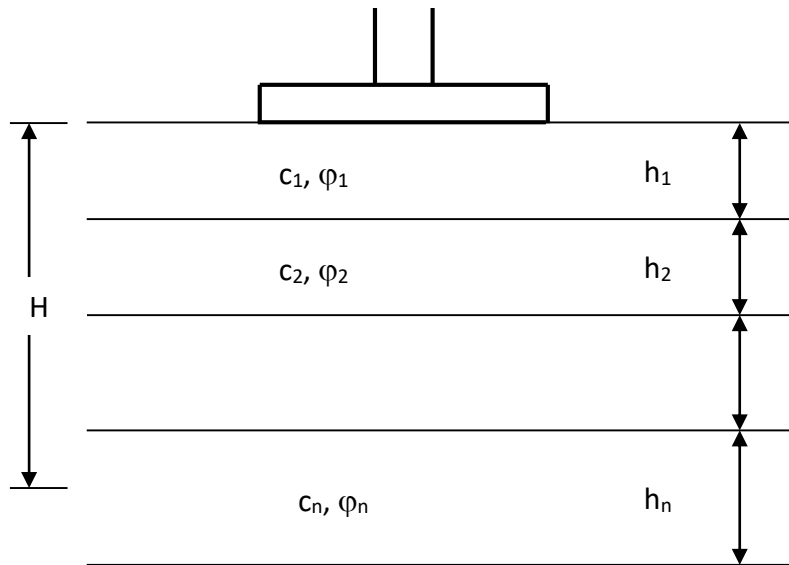


Fig. 1.7 Bearing capacity of multilayered soil system

### **Corrections for Different Modes of Failure**

There are mainly three principal modes of shear failure namely general shear, local shear and punching shear. They are illustrated in Fig. 1.8.

**General Shear Failure** This occurs when a clearly defined plastic yield slip surface forms under the footing and develops outward towards one or sides and eventually to the ground surface. Failure is sudden and will often be accompanied by severe tilting leading to final collapse on one side. This mode of failure is associated with dense and overconsolidated soils of low compressibility.

**Local Shear Failure** In compressible soils, significant vertical movement may take place before any noticeable development of shear planes occurs. As the soil beneath the footing reaches the yield condition shear planes develop, but fail to extend to the ground surface. Some adjacent bulging may occur, but very little tilting takes place. The settlement, which occurs, will usually be the principal design criteria.

**Punching Shear Failure** In weak compressible soils, considerable vertical movement may take place with the development of slip surface restricted to vertical planes adjacent to the sides of the footing. Bulging at the surface is usually absent and may even be replaced by drag down.

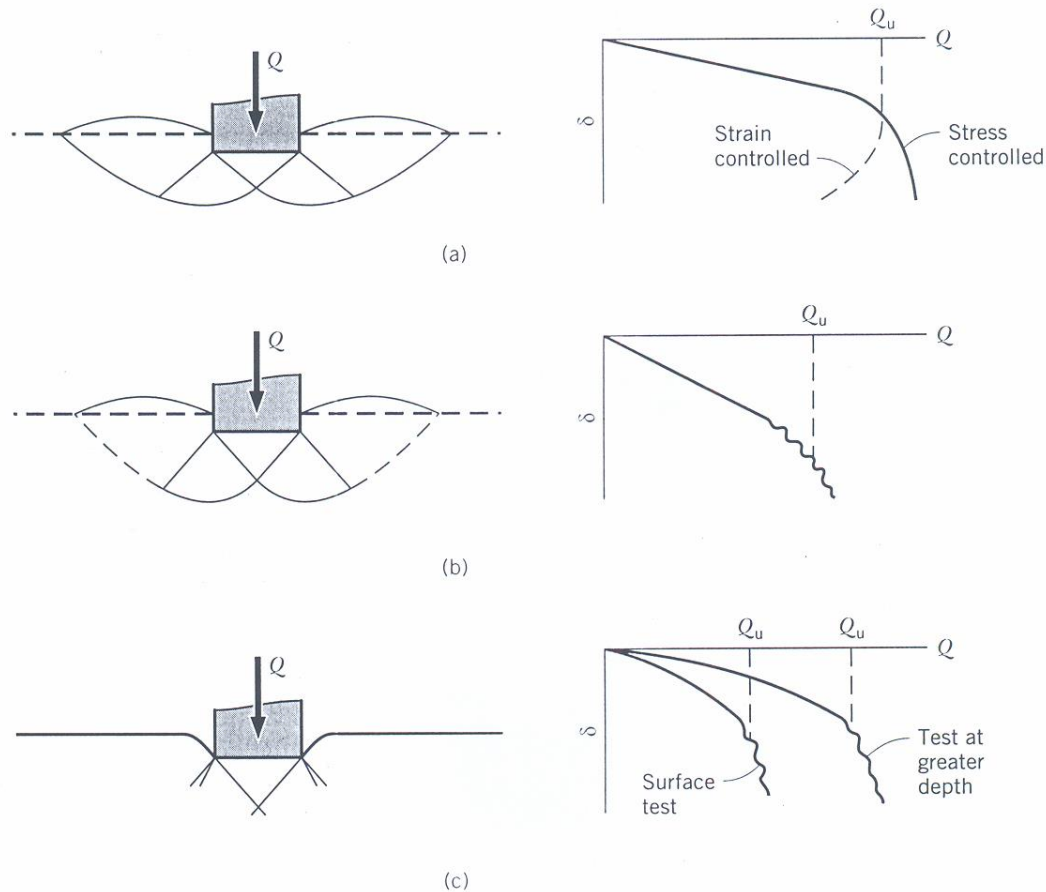


Fig. 1.8 Modes of failure of foundation soil; (a) General shear; (b) Local shear; (c) Punching shear

### Correction Factors

Terzaghi developed his bearing capacity equations assuming a general shear failure. For failures other than general shear he proposed reduced values of  $c$  and  $\phi$  as:

$$c' = 0.67c ; \quad \phi' = \tan^{-1}(0.67\tan\phi)$$

The ultimate bearing capacity is to be determined using the corrected values of  $c$  and  $\phi$ .

Vesic (1975) suggests the following modification of  $\phi$  in case of sandy soil.

$$\phi^* = \tan^{-1}[(0.67 + I_D - 0.75I_D^2)\tan\phi], \quad \text{for } 0 \leq I_D \leq 0.67$$

$$\phi^* = \phi, \quad \text{for } I_D > 0.67.$$

### Allowable Bearing Capacity

**Allowable bearing capacity** is the minimum of the safe net bearing capacity (determined from considerations of shear failure) and safe bearing pressure (determined from considerations of

permissible settlement). When wind and seismic forces are considered in design the allowable bearing capacity is suitably designed accordingly.

**Safe net bearing capacity** is the maximum net intensity of loading that the foundation will safely carry without the risk of shear failure of soil irrespective of any amount of settlement that may occur. It is obtained by dividing the ultimate net bearing capacity by a suitable factor of safety.

$$q_{\text{safe-net}} = q_{\text{ult-net}} / FS$$

**Ultimate net bearing capacity** is the net intensity of loading at the base of the foundation which would cause shear failure of soil. This is obtained as the difference of ultimate bearing capacity ( $q_{\text{ult}}$ ) and the effective surcharge intensity ( $q$ ) at the base level of foundations.

$$q_{\text{ult-net}} = q_{\text{ult}} - q$$

Hence, the equation for ultimate net bearing capacity for a strip footing considering general shear will take the form

$$q_{\text{ult-net}} = cN_c + \frac{1}{2} B\gamma N_\gamma + q(Nq - 1)$$

**Safe bearing pressure** ( $q_{\text{safe-pr}}$ ) is the maximum net intensity of loading that can be imposed on the soil by the foundation without the settlement exceeding the permissible value to be determined for each type of structure and type of soil.

### Allowable Bearing Capacity for Sandy Soil

For sandy soil safe bearing pressure is usually determined from its empirical correlations with SPT value as suggested by Terzaghi and Peck, shown in Fig. 3.18. It gives the bearing pressure for permissible settlement of 25 mm. For any other value of permissible settlement the safe bearing pressure can be linearly extrapolated. For any value of permissible settlement,  $S_p$ , the safe bearing pressure is given by

$$q_{\text{safe-pr}, S_p} = (q_{\text{safe-pr}}/25) \cdot S_p \cdot C_w \cdot C_D$$

Average value of measured  $N$  should be within a zone of  $2B$  below the base of the footing.  $C_w$  and  $C_D$  are the correction factors of  $N$  for water table and overburden respectively.



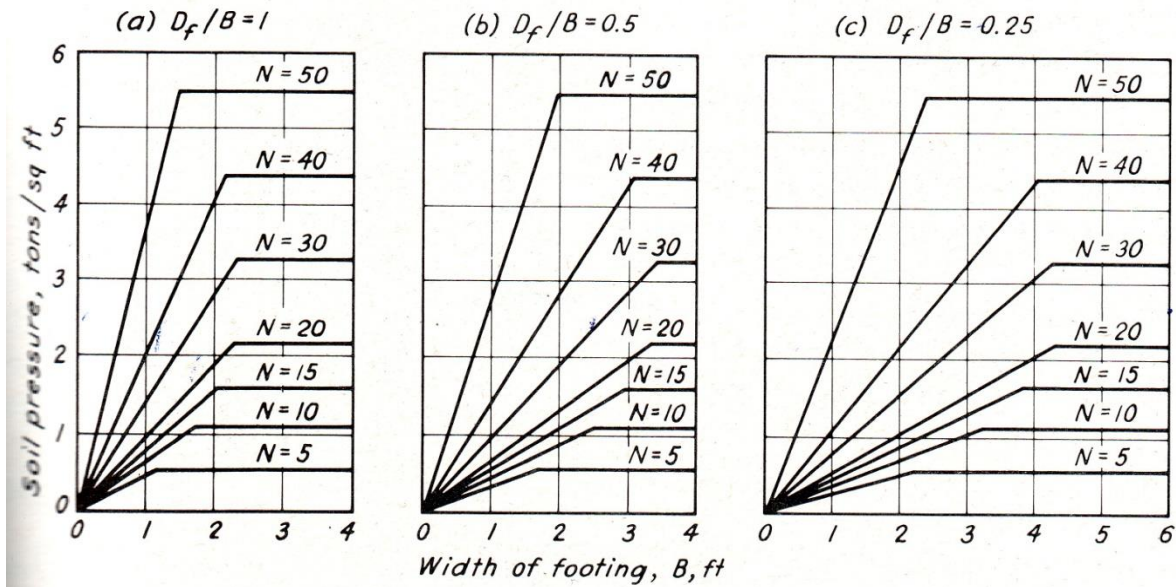


Fig. 3.18 Correlation between  $q_{\text{safe-net}}$  and N value

### Allowable Bearing Capacity for Clayey Soil

Allowable bearing capacity is estimated comparing the safe bearing pressure against settlement and safe bearing capacity against shear failure of foundation soil.

Safe bearing pressure for clay soil is estimated considering settlement of foundation soil due to load. The total amount of settlement includes elastic, consolidation and secondary compressions.

Safe net bearing capacity of clay soil is usually determined using Skempton's formula for ultimate bearing capacity and a suitable factor of safety. For a continuous footing in clay ultimate net bearing capacity can be expressed in terms of unconfined compressive strength,  $q_u$  and is given by:

$$q_{\text{ult-net}} = cN_c = 2.85q_u$$

Using a factor of safety of 3, for a strip footing, we get the relationship:

$$\frac{q_{\text{ult-net}}}{FS} = \frac{2.85q_u}{3} = 0.95q_u \approx q_u$$

Thus gross safe bearing capacity is:

$$q_{\text{safe-gross}} = \frac{q_{\text{ult-net}}}{FS} + \gamma D_f = q_u + \gamma D_f$$

Peak, Hansen and Thornburn proposed a set of curves for the safe bearing capacity as shown in Fig. 3.19.

Unlike that of sandy soil allowable bearing capacity is usually governed by the safe bearing pressure. As such Fig. 3.19 may be used as a design chart for clayey soils.

## Selection of Factor of Safety

The factor of safety used in shallow foundation design depends on factors like design maximum load that coming on the foundation, shapes of foundation and the extent of subsoil investigation carried at the site.

- For structures where maximum loads are likely to occur **often like railway bridges, water tanks etc., the factor of safety (FS) should be 3 to 4.**
- Where the maximum loads occur occasionally as in highway bridges, FS should be 2.5 to 3.5.
- When maximum loads are not likely to occur as in residential buildings, the factor of safety should be 2.0 to 3.0.

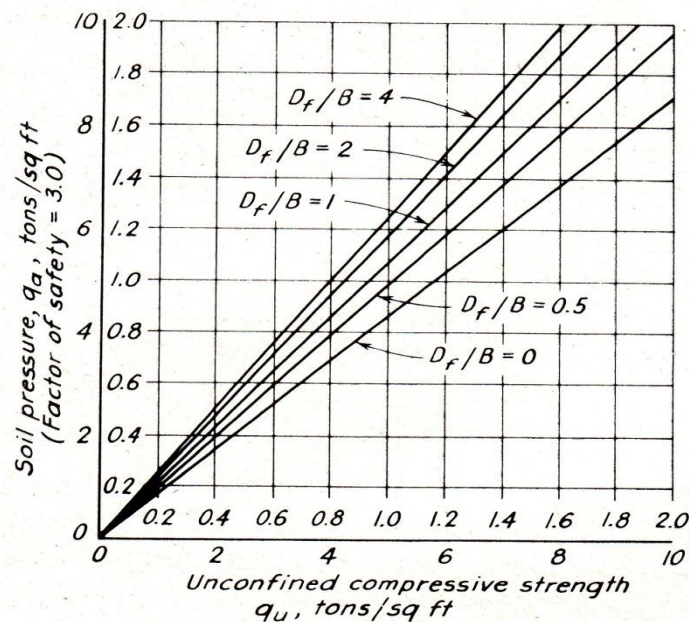


Fig. 3.19 Safe bearing capacity of footing in clay

Where extensive soil investigation has been done the lower value of the range is suggested; in case of limited subsoil investigation the higher ranges of factor of safety has been recommended. Bowles suggested to following factor of safety for the types of foundation.

Spread Footing: 2 to 3

Mat Foundation: 1.7 to 2.5

Footing Subjected to Uplift Forces: 1.7 to 2.5

## Soil Settlement

A soil shear failure can result in excessive building distortion and even collapse. Excessive settlements can result in structural damage to a building frame nuisances such as sticking doors and windows, cracks in tile and plaster, and excessive wear or equipment failure from misalignment resulting from foundation settlements.

It is necessary to investigate both base shear resistance (ultimate bearing capacity) and settlements for any structure. In many cases settlement criteria will control the allowable bearing capacity.

Except for occasional happy coincidences, soil settlement computations are only best estimates of the deformation to expect when a load is applied.

### **The components of settlement of a foundation are:**

1. Immediate settlement
2. Consolidation Settlement, and
3. Secondary compression (creep)

$$\Delta H = \Delta H_i + U \Delta H_c + \Delta H_s$$

$\Delta H$  = total settlement,  $\Delta H_c$  = consolidation settlement,  $\Delta H_s$  = secondary compression,  $U$  = average degree of consolidation. Generally, the final settlement of a foundation is of interest and  $U$  is considered equal to 1 (i.e. 100% consolidation)

### **1. Immediate Settlement**

Immediate settlement concerns the initial pressure on the soil under and surrounding the foundation. It is "immediate" because it occurs during and right after construction. It has nothing to do with water displacement, but is merely caused by the weight of the structure. In terms of building foundations, immediate settlement is relatively easy to predict and measure. In many cases, given the nature of the soil, foundations are constructed with the ability to withstand a certain amount of shift without damage. Damage usually occurs only in the long term, as the shift slowly continues over time.

- Immediate settlement takes place as the load is applied or within a time period of about 7 days.
- Predominates in cohesion less soils and unsaturated clay
- Immediate settlement analysis are used for all fine-grained soils including silts and clays with a degree of saturation < 90% and for all coarse grained soils with large coefficient of permeability (say above 10.2 m/s)

### **2. Consolidation Settlement ( $\Delta H_c$ )**

Consolidation settlement is distinguished from immediate settlement both by the duration of the settlement and by displacement of water. Consolidation is the more worrisome form of settlement because it is difficult to predict over months or years. Consolidation settlement is the settling of a foundation, over time, due to pressure exerted by the structure and squeezes out the water content of the soil, thus compressing it. Expulsion of moisture from the soil usually is a long-term process.

- Consolidation settlements are time dependent and take months to years to develop. The leaning tower of Pisa in Italy has been undergoing consolidation settlement for over 700 years. The lean is caused by consolidation settlement being greater on one side. This, however, is an extreme case. The principal settlements for most projects occur in 3 to 10 years.
- Dominates in saturated/nearly saturated fine grained soils where consolidation theory applies.  
Here we are interested to estimate both consolidation settlement and how long a time it will take or most of the settlement to occur.

### 3. Secondary Settlement/Creep ( $\Delta H_c$ )

Consolidation settlement has two components, primary and secondary. The former deals explicitly with the settlement caused by soil moisture displacement, and the latter deals with the elastic settlement after all movable water has been squeezed out of the soil. Primary consolidation is the most significant and potentially harmful of the two. Primary consolidation takes quite a bit of time, from weeks to years. Secondary consolidation is the quicker result of primary consolidation. Once primary has been completed, and all movable water has been moved, secondary kicks in. Secondary consolidation occurs immediately after primary, and takes far less time to complete. After secondary consolidation is complete, the structure remains in its permanent position. As a result, many builders advise residents in new homes to avoid repairing any settlement damage until secondary consolidation is complete, which is normally after two years at most.

- Occurs under constant effective stress due to continuous rearrangement of clay particles into a more stable configuration.
- Predominates in highly plastic clays and organic clays.

### Immediate settlement computation

$$\Delta H_i = q_0 B \frac{1 - \mu^2}{E_s} m I_s I_E$$

Where

$q_0$  = intensity of contact pressure in units of  $E_s$  (Undrained Modulus of Elasticity)

$B'$  = least lateral dimension of contributing base area in units of  $\Delta H_i$

$E_s, \mu$  = Elastic Soil Parameters. A major problem is of course to obtain correct stress-strain modulus  $E_s$ .  $E_s$  can be found from laboratory tests like unconfined compression tests, Triaxial compression tests, and in-situ tests like SPT, CPT, Plate load tests, Pressure meter etc

$m$  = number of corners contributing to settlement  $\Delta H_i$ . At the footing center  $m = 4$ ; and at a corner  $m = 1$ , at a side  $m = 2$ .

$I_E$  = Embedment reduction factor, which suggests that the settlement is reduced when it is placed at some depth in the ground. For surface footing  $I_E = 1$

$I_s$  = Influence Factor

$$I_s = I_1 + \frac{1 - 2\mu}{1 - \mu} I_2$$

The above equation for  $I_s$  is strictly applicable to flexible bases on the half space. In practice, most foundations are flexible because even every thick footing deflects when loaded by superstructure load. If the base is rigid, reduce  $I_s$  factor by about 7%. The half space may consist of either cohesion less material or any water content, or unsaturated cohesive soils.

## Secondary compression/creep

After primary consolidation the soil structure continues to adjust to the load for some additional time. This settlement is termed secondary consolidation/secondary compression. At the end of secondary consolidation the soil has reached a new  $K_0$ -state (at-rest state).

Secondary consolidation may be the larger component of settlement in some soils, particularly in soils with a large organic component. Secondary consolidation is associated with both immediate & consolidation type settlements, although it is usually not of much significance with immediate settlements. The magnitude of secondary compression for a given time is generally greater for NCC than for OCC.

The rate of secondary compression  $J$  in the consolidation (oedometer) test can be defined by the slope  $C_\alpha$  of the final part of the compression/log time curve. Where  $H_{sl}$  = thickness of the laboratory sample at time  $t_1$ ,  $\Delta H_{sl}$  = Change in sample thickness of soil sample between  $t_1$  and  $t_2$ .

To find secondary consolidation settlement in the field ( $\Delta H_s$ ),

$$\Delta H_s = \Delta C_\alpha \log \frac{t_{100(f)} + \Delta t}{t_{100(f)}}$$

$H$  = Thickness of the field consolidating stratum at the end of primary consolidation.

Commonly initial thickness is used unless the primary consolidation is very large. Say more than 10% of initial thickness.

$t_{100(f)}$  = time taken for primary consolidation to complete in the field

$\Delta t$  = time interval beyond  $t_{100(f)}$

$t_2 = t_{100(f)} + \Delta t$  = time for which secondary settlement is to be calculated.

To find  $t_{100(f)}$  following relationship is used

$$\frac{t_{100(f)}}{d_f^2} = \frac{t_{100(lab)}}{d_{lab}^2}$$

Where  $t_{100(lab)}$  and  $t_{100(f)}$  = time taken for primary consolidation to complete in the laboratory  
 $d_f$ ,  $d_{lab}$  = are respectively maximum drainage paths in the field and laboratory. For one-way drainage  $d$  = thickness of the layer of interest or sample thickness in the laboratory, for two-way drainage  $d$  = half of the thickness of the layer of interest/sample.

## **Settlement Limits**

Total settlement is the magnitude of downward movement. Differential settlement is non-uniform settlement. It is "the difference of settlement between various locations of the structure. Angular distortion between two points under a structure is equal, to the differential settlement between the points divided by the distance between them. Theoretically speaking, no damage will be done to a structure if it settles uniformly as a whole regardless of how large the settlement may be. The only damage would be to the connections of the underground utility lines. However, when the settlement is non-uniform (differential), as is always the case, damage may be caused to the structure. The tolerable, settlements of different structures, vary considerably. Simple-span frames can take considerably greater distortion than rigid frames. A fixed-end arch would suffer greatly if the abutments settle or rotate. For road embankments, storage silos and tanks a settlement of 300mm - 600mm may be acceptable, but for machine foundations the settlement may be limited to 5mm 30mm. Different types of construction

materials can withstand different degrees of distortion. For example, sheet metal wall panels do not show distress as readily as brick masonry.

To reduce differential settlement, the designer may limit the total settlement and use the following equation for the calculation of the differential settlement:

$$(\Delta H_{diff})_{max} = \frac{1}{2} \Delta H_{total}$$

Guidelines to limiting values are suggested by a number of sources, but following routine limits appear to be conventionally acceptable (Skempton and Mac Donald, 1956)

**Skempton and MacDonald suggested the following permissible settlements**

**SANDS**

- Maximum total settlement = 40 mm for isolated footing  
= 40 – 65 mm for rafts.
- Maximum differential settlement = 25 mm between adjacent columns.

**CLAYS**

- Maximum total settlement = 65 mm for isolated footing  
= 65 – 100 mm for rafts.
- Maximum differential settlement = 40 mm between adjacent columns.

The differential settlement may also be evaluated in terms of the angular distortion given by:

$$(\Delta H_{diff}) = \Delta/L$$

Where  $\Delta$  = relative settlement between the two points and L = Horizontal distance between the two points.

Based on a large number of settlement observations and performance of structures, the suggested limits for tolerable differential settlements are shown in table below.

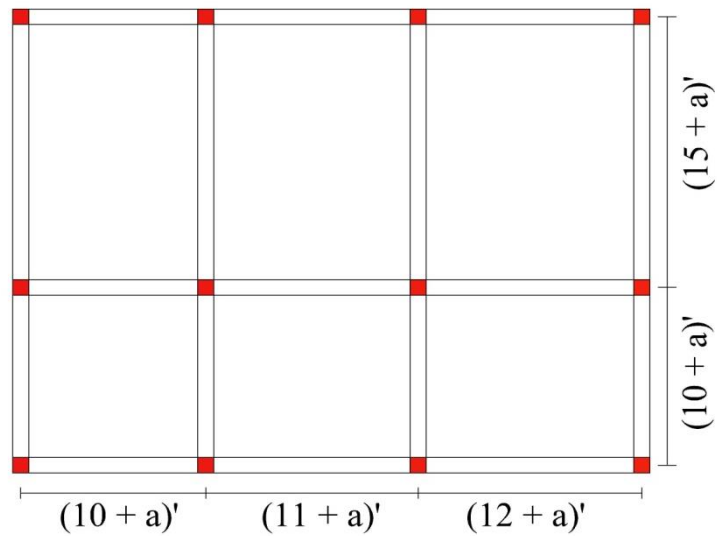
<b>Angular distortion</b>	<b>Type of limit and structure</b>
1/150	Structure damage of general buildings expected
1/250	Tilting of high rigid buildings may be visible
1/300	Cracking in panel walls expected
	Difficulties with overhead cranes
1/500	Limit for buildings in which cracking is not permissible
1/600	Overstressing of structural frames with diagonals
1/750	Difficulty with machinery sensitive to settlement

## Calculation of Superimposed Load



**Q:** There is a column-beam layout plan for a 6 storied residential building given below. Calculate load of each columns.

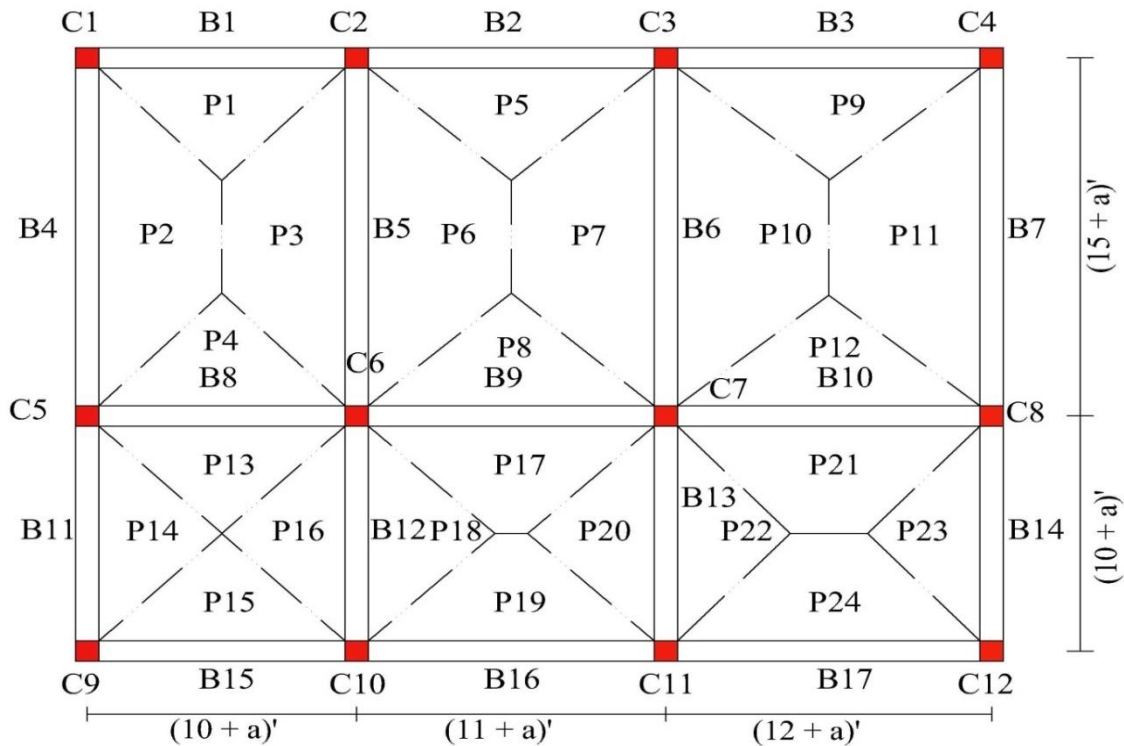
- Use:
- Slab thickness : 6"
  - All Beams : 12" X 18"
  - All Columns : 12" X 12"
  - Floor Finish (FF) : 25psf
  - Partition Wall (PW) : 40psf
  - Live load (LL) : 60psf
  - Factor, a : Roll x 0.2



**Solution:**

First the live load, Floor finish load, partition wall load will be taken by the slab adding its own weight. Then a slab will transfer the load to the adjoining beams. Beam will transfer the load from slab adding its self weight to both sides column. The column will then transfer the load from beams adding its self weight to foundation and then the foundation will transfer the total load to the soil.

The load from slab panel will be transferred to the beam in two ways. For the rectangular slab it will be transferred by two triangular and two trapezoidal panels. For the square slab panel it will transfer loads by four triangular panels. This system is called yield line analysis. The panels are shown in figure below. Now first number the columns, beams and all slab panels for calculation.





**Step 1: Calculating self weight of members**

Slab self weight :  $\frac{6}{12} \times 150 = 75 \text{psf}$   
 Beam self weight :  $\frac{12 \times 18}{144} \times 150 \times \text{length} = 225 \text{pcf}$   
 Column self weight :  $\frac{12 \times 12}{144} \times 150 \times \text{length} = 150 \text{pcf}$

**Step 2: Load on Slab:**

Slab UDL = (25+40+60+75) = 200psf

**Slab load on triangular panel:**

Panel name	Base	Hight	Area = 0.5xbasexhight	Total load = area x UDL

**Slab load on trapezoidal panel:**

Panel name	Short length, b	Long Length, c	Height, h	Area = $\frac{b+c}{2}$ h	Total load = area x UDL

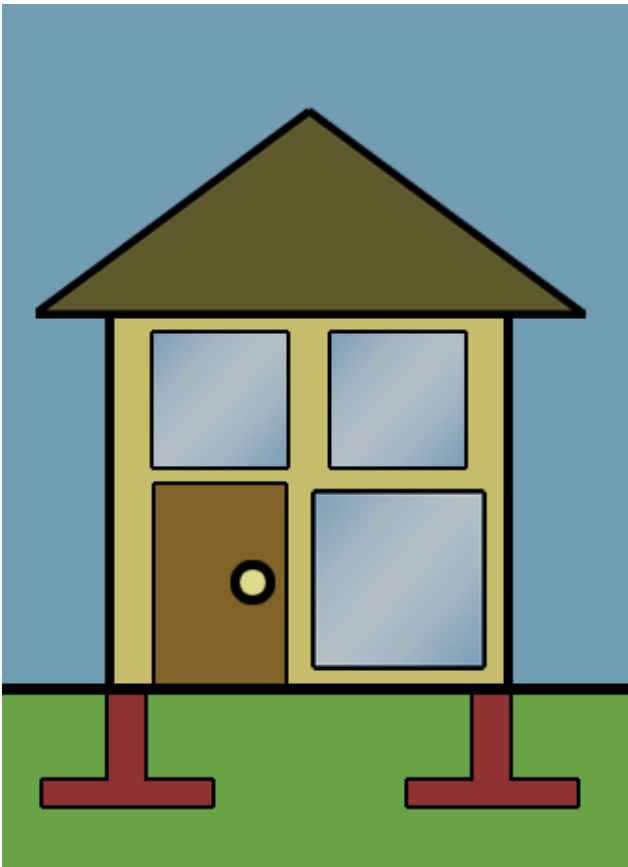
**Step 3: Load on beam:**

Beam name	Length L	Self weight, L x Beam self weight	Load contributing Slab panel	Load from slab	Total load

**Step 4: Load on column:**

Column name	Load contributing beam	Load from beam (half load)	Self weight of column 150 x story height	Total load for each story	Total load Load for each story x total story no.

# Bearing Capacity Calculation of Shallow Foundation



**Q:** From the previous problem, using the column load and the soil test report of the site given below, calculate the bearing capacity and footing size.

**Solution:**

Bearing Capacity is a general term used to describe, the load carrying capacity of a foundation soil that enables to bear and transmit loads from a structure.

**\* Using Terzaghi's equation:**

This equation can be used both for cohesionless and cohesive soil. The common equation is-

$$q_{ult} = cN_c + \frac{1}{2} B\gamma N_\gamma + qN_q$$

Where,  $N_c$ ,  $N_\gamma$  and  $N_q$  are nondimensional bearing capacity factors and functions only of the angle of internal friction,  $\phi$ .

Strip footing:  $q_{ult} = cN_c + \frac{1}{2}B\gamma N_\gamma + qN_q$

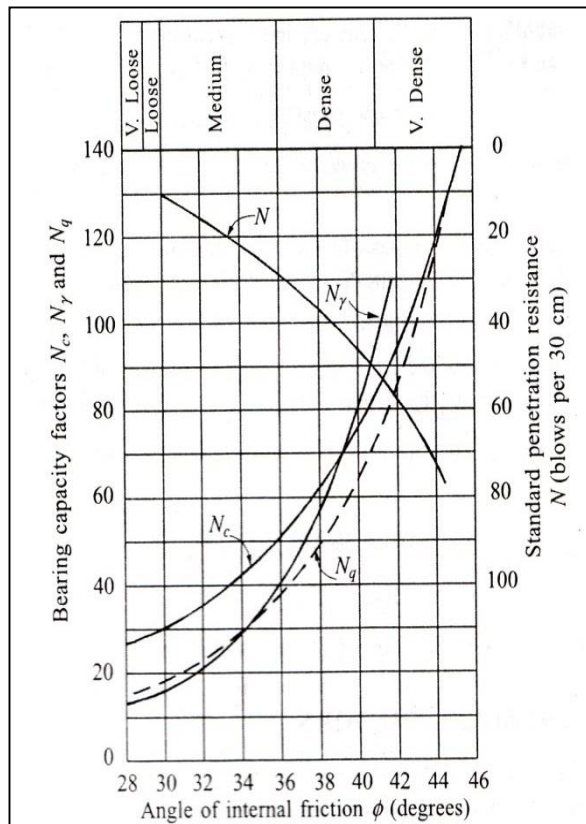
Square footing:  $q_{ult} = 1.3cN_c + 0.4 B\gamma N_\gamma + qN_q$

Circular Footing:  $q_{ult} = 1.3cN_c + 0.3 B\gamma N_\gamma + qN_q$

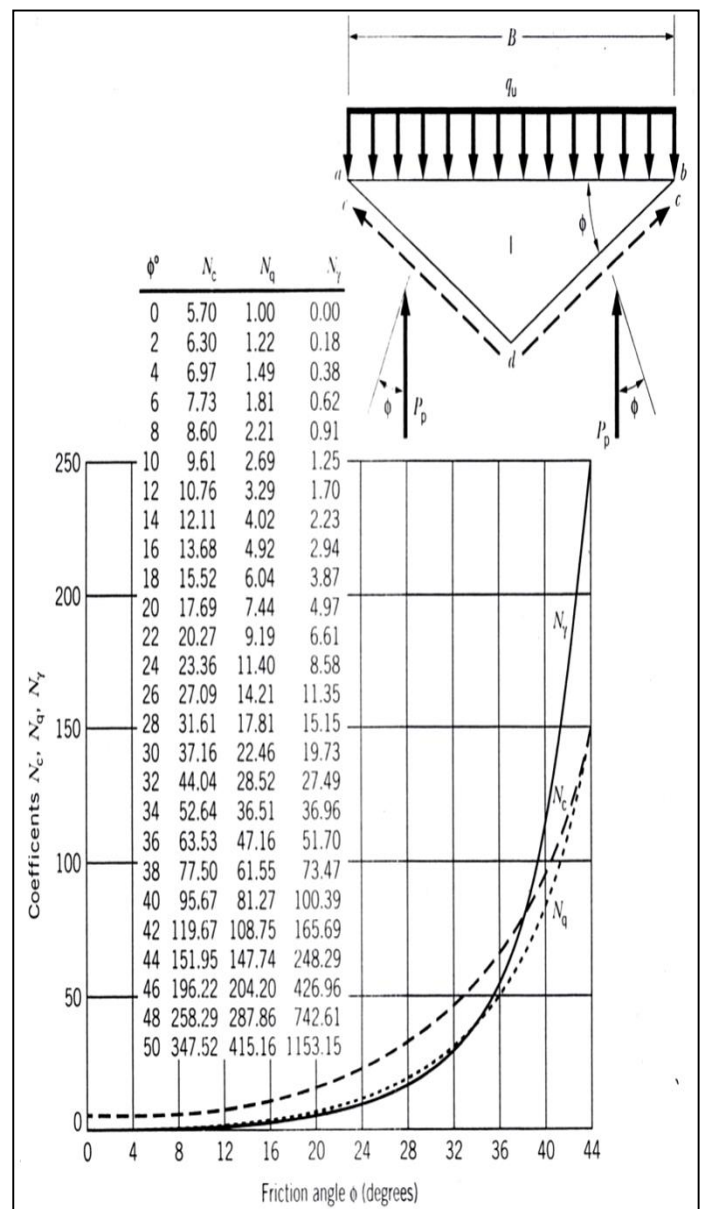
$$N_q = \tan^2(45 + \frac{\phi}{2})e^{\pi \tan \phi}$$

$$N_c = (N_q - 1) \cot \phi$$

$$N_\gamma = 1.5(N_q - 1) \tan \phi$$



Terzaghi's general bearing capacity factors against SPT values for cohesionless soils  
Terzaghi's bearing capacity factors



### Calculation of bearing capacity

Column	B (Let)	Depth of foundation, $D_f$	Cohesion $C = \frac{q_u}{2}$ ( $q_u$ = unconfined compressive strength)	Angel of internal friction $\phi$ .	Bearing Capacity factors			Ultimate bearing capacity, $q_{ult}$	Allowable bearing capacity, $q_{all} = \frac{q_{ult}}{F.S.}$
					$N_c$	$N_q$	$N_\gamma$		

### Calculation of footing size

Column	Column load	Allowable bearing capacity, $q_{all}$	Footing Area = $\frac{\text{Load}}{q_{all}}$	$B = \sqrt{\text{area}}$ (for square footing)	B (rounded)	Check B ok/ not

\* If the calculated B is less than the B that you let, then it is ok but not economical. The calculated B should be a nearest value of the B that you let but should not exceed the value.

### \* Using Skempton's Bearing Capacity Equation for Clay Soil

Skempton (1951) proposed equations for bearing capacity of footings founded on purely cohesive soils based on extensive investigations

$$q_{ult} = cN_c$$

The bearing capacity factor,  $N_c$  is given by

For strip footing:

$$N_c = 5(1 + 0.2 D_f/B)$$

For square and circular footings:

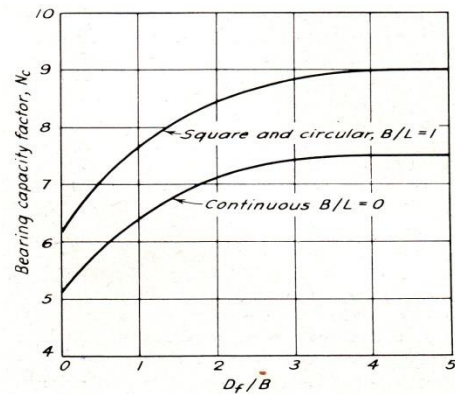
$$N_c = 6(1 + 0.2 D_f/B)$$

For rectangular footings:

$$N_c = 5(1 + 0.2 B/L)(1 + 0.2 D_f/B) \quad \text{for } D_f/B \leq 2.5$$

And  $N_c = 7.5(1 + 0.2 B/L) \quad \text{for } D_f/B > 2.5.$

Or from the graph



Skempton's bearing capacity factors for clay soils

### Calculation of bearing capacity

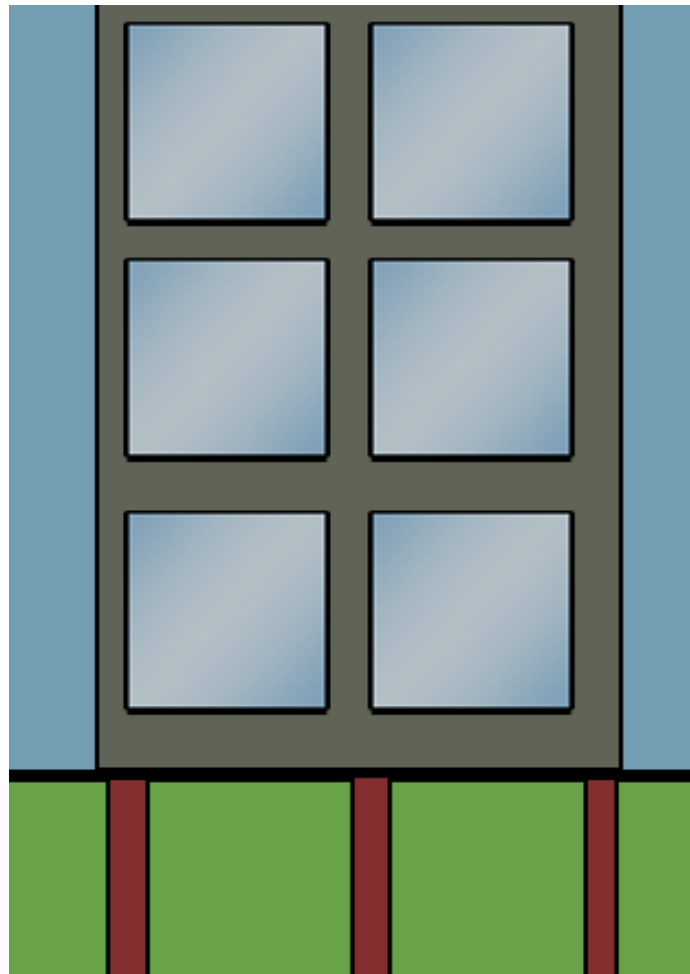
Column	Depth of foundation $D_f$	Cohesion $C = \frac{q_u}{2}$ ( $q_u$ = unconfined compressive strength)	Bearing Capacity factor $N_c$	Ultimate bearing capacity $q_{ult}$	Allowable bearing capacity $q_{all} = \frac{q_{ult}}{F.S.}$

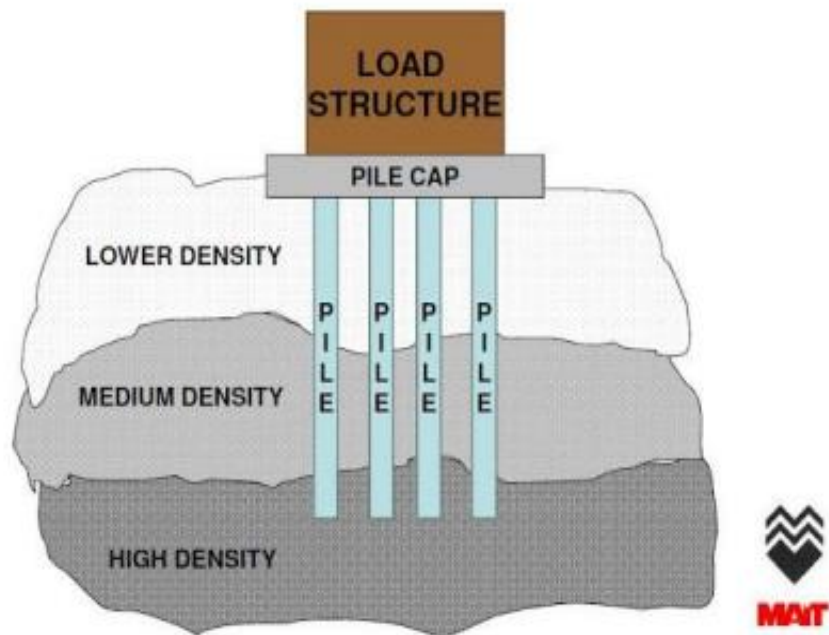
### Calculation of footing size

Column	Column load	Allowable bearing capacity $q_{all}$	Footing Area = $\frac{\text{Load}}{q_{all}}$	$B = \sqrt{\text{area}}$ (for square footing)	B (rounded)	Check B ok/ not

\* If the calculated B is less than the B that you let, then it is ok but not economical. The calculated B should be a nearest value of the B that you let but should not exceed the value.

## Bearing Capacity Calculation of Pile Foundation





### Pile Capacity

Pile has **Two** types of capacity

1. Structural Capacity &
2. Geotechnical Capacity

Normally **geotechnical capacity** is lower than **structural capacity**.

Failure in Soil ←                      Failure in Pile ←

Failure in Soil may be **two** types.

1. Failure from Bearing capacity (Both Sand & Clay) &
2. Failure from Settlement (Only for Clay)
  - a. Individual Settlement
  - b. Differential Settlement

A spacing of three times the diameter of the piles is commonly selected as the trial spacing and checked against the criterion that the sum of the shearing and bearing capacities of the group of piles must be at least equal to the capacity of a single pile multiplied by the number of piles in the group, which termed as **Individual Action of Pile Cap**.

In **Group Action of Pile Cap**, the pile group is considered as a single pile and capacity is determined. But 2/3 of the total capacity is considered effective to carry the total load. Therefore,

Individual action of Pile Cap = Individual capacity of a pile x number of pile in the pile group

$$\text{Group action of Pile Cap} = \frac{2}{3} \times \text{Capacity of group pile}$$

### Pile Foundation Type

There are **Four** types of Pile Foundation based on **Materials**

1. Timber Pile **or** Wooden Pile
2. Concrete Pile
3. Steel Pile
4. Composite Pile

There are **Two** types of Pile Foundation based on **Construction Method**

1. Cast in-situ Pile **or** Bored Pile **or** Drilled Pile &
2. Pre-cast Pile **or** Driven Pile

There are **Two** types of Pile Foundation based on **Load Transfer**

1. End Bearing Pile (Load is Transferred from depth L )
2. Friction Pile (Load is Transferred from depth  $\frac{2}{3} L$  )

L = Total Depth of Pile

### Pile Foundation Design

We consider two types in design on Bearing Capacity -

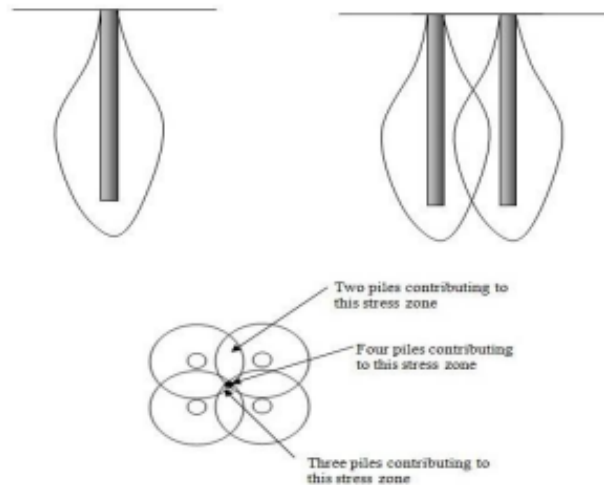
#### 1. Individual Action Capacity

Total Capacity = Capacity of 1 Pile × No. of Pile

#### 2. Group Action Capacity

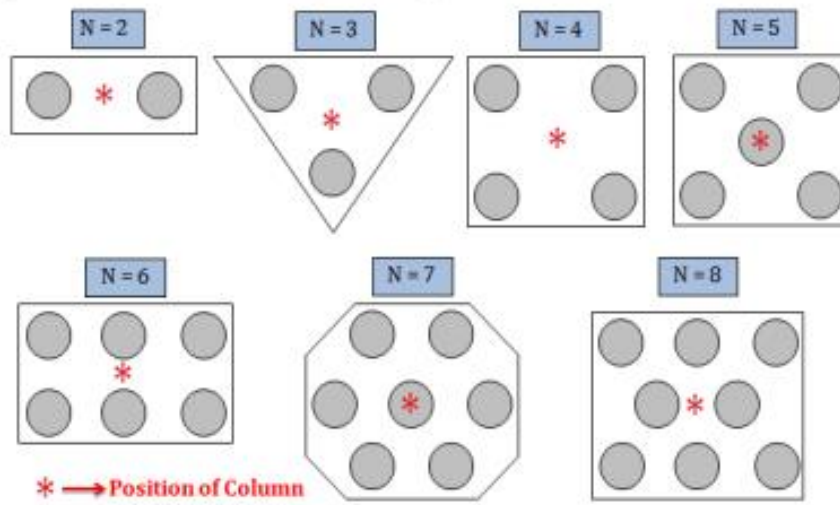
Inter pile spacing =  $3 \times \text{Diameter of Pile}$  → Efficiency 80%

Inter pile spacing =  $2.5 \times \text{Diameter of Pile}$  → Efficiency 70%



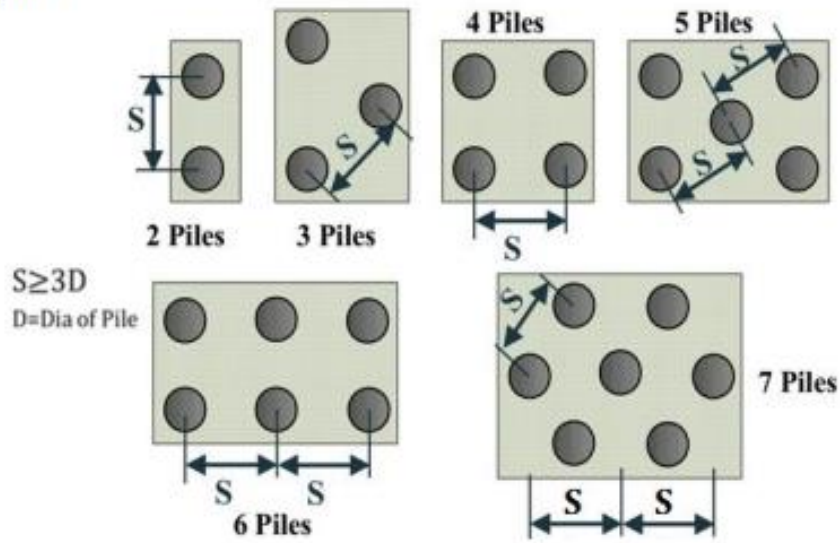
**Figure 4.1:** Individual and Group Action Capacity

**Pile, Pile Cap & Column Position**



**Figure 4.2: Pile, Pile Cap & Column Position**

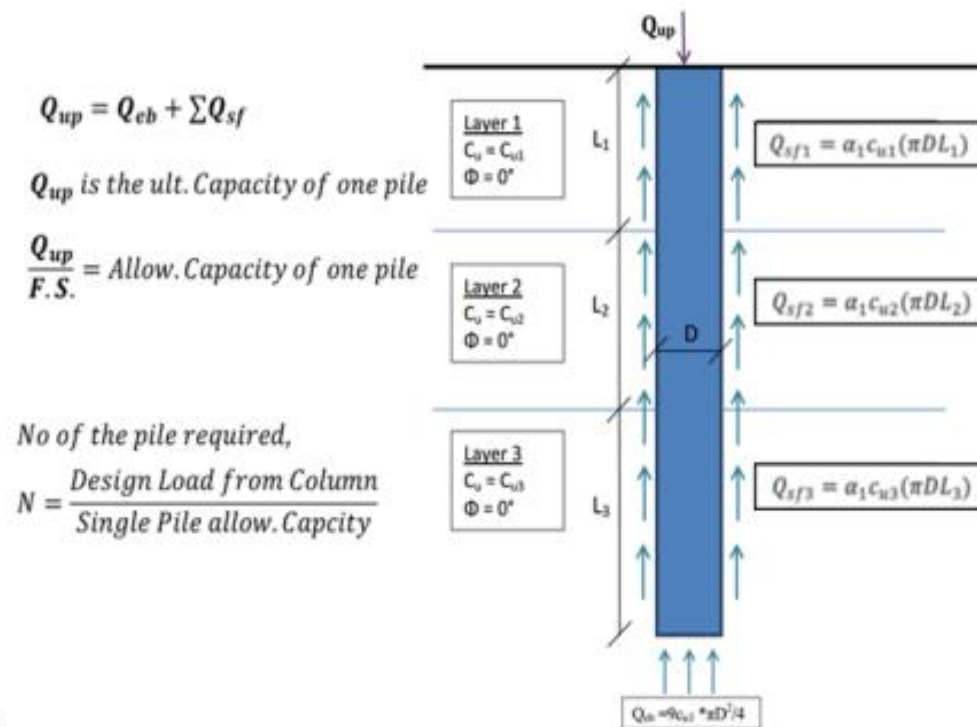
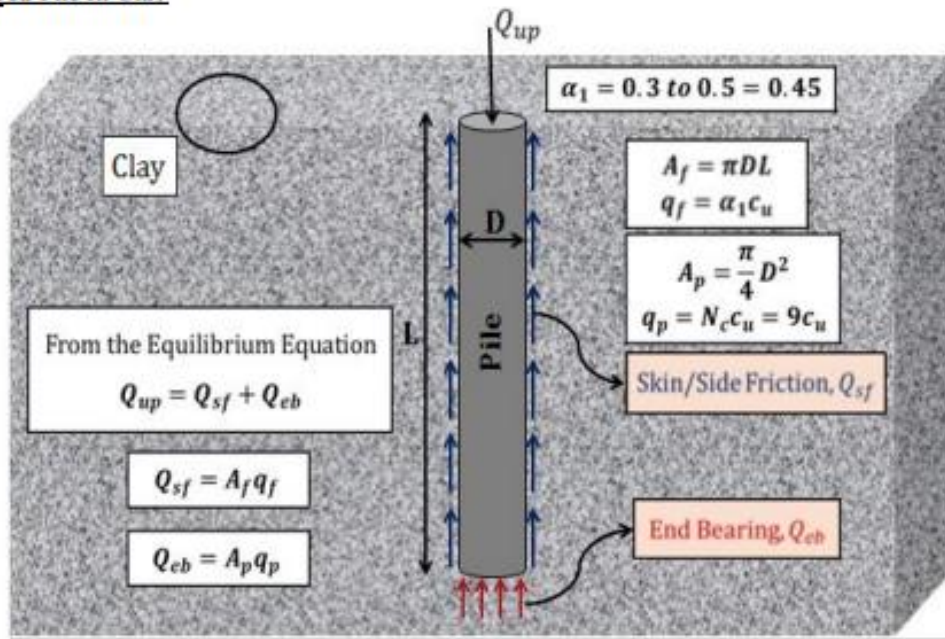
**Pile Spacing**



**Figure 4.3: Pile Spacing**



**Bored Pile In Clay**



**Figure 4.4: Bored Pile in Clay**

The ultimate bearing capacity of a pile is considered to be the sum of end bearing resistance and the resistance due to skin friction

$$Q_{up} = Q_{eb} + Q_{sf} \quad (4.1)$$

where,

- $Q_{up}$  = Ultimate bearing load of the pile
- $Q_{eb}$  = End bearing resistance of the pile
- $Q_{sf}$  = Skin friction resistance of the pile

$$Q_{eb} = A_p q_p \quad (4.2)$$

- $A_p$  = Effective area of the tip of the pile
- For a circular closed end pile =  $\pi D^2/4$
- $q_p = 9c_u$  = Theoretical unit tip-bearing capacity for cohesive soils
- $c_u$  = Undrained shear strength of soil at the base

1. Skin friction of top 5' of pile should be neglected [ due to loose soil at top]
2. Skin friction of bottom 2' -5' of pile should be neglected [ due to induced soil at bottom]

$$Q_{sf} = A_f q_f \quad (4.3)$$

- $A_f$  = Effective surface area of the pile
- For a circular pile =  $\pi DL$  [L = thickness of soil layer]
- $q_f = \alpha_1 c_u$  = Theoretical unit friction capacity [ $c_u$  = Undrained shear strength of soil layer]
- [ $\alpha_1$  = reduction factor,  $\alpha_1$  value varies from 0.3-0.5. Normally 0.45 is used. While determining capacity by AASHTO method,  $\alpha_1 = 0.55$  should be used]

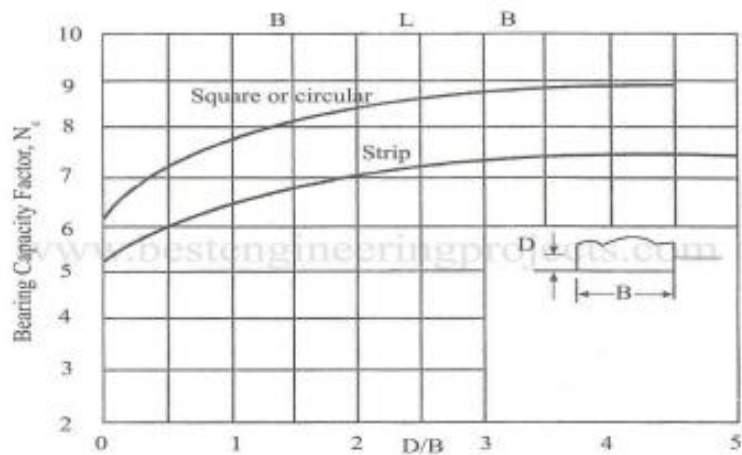


Figure 4.4: Skempton's Bearing Capacity Factor  $N_c$

## Bored Pile In Sand

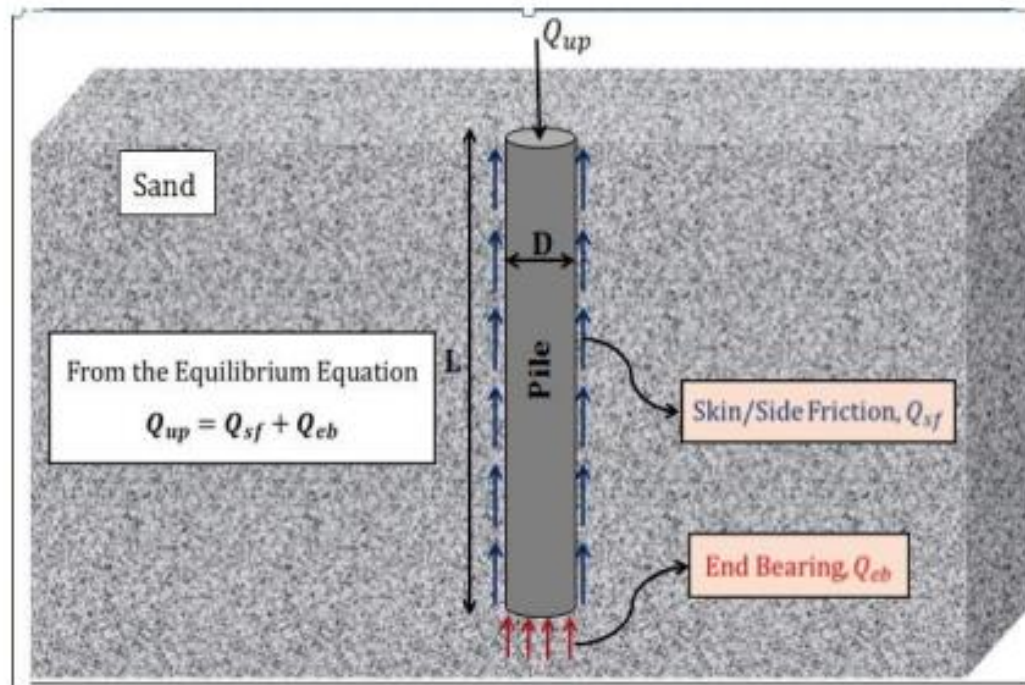


Figure 4.5: Bored Pile in Sand

$$\text{End Bearing, } Q_{eb} = 1.2 * N * A_p \quad (4.4)$$

$$\text{Skin Friction, } Q_{sf} = \beta * p_o' * A_f \quad [ \beta = 1.5 - 0.135\sqrt{z} ] \quad (4.5)$$

Where,

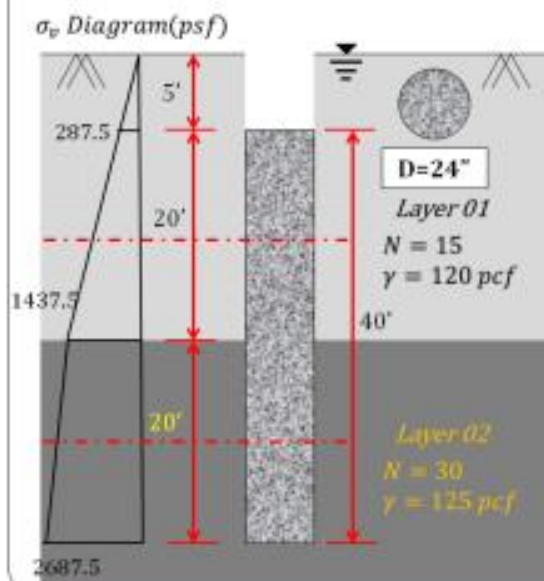
$z$  = depth from GL to middle of the layer

$N$  = Field  $N$  value from standard penetration test at the level of bottom

$p_o'$  = effective overburden pressure

1. Skin friction of top 5' of pile should be neglected [ due to loose soil at top]
2. Skin friction of bottom 2'-5' of pile should be neglected [ due to induced soil at bottom]

## Bored Pile Example In Sand



### Layer 01:

$$\beta = 1.5 - 0.135\sqrt{z} = 1.5 - 0.135\sqrt{15} = 0.977$$

$$\begin{aligned} \text{Skin Friction} &= \beta \sigma_v A_f \\ &= 0.977 \times \frac{287.5 + 1437.5}{2} \times (\pi \times 2 \times 20) \\ &= 105.89 \text{ kip} \end{aligned}$$

### Layer 02:

$$\beta = 1.5 - 0.135\sqrt{z} = 1.5 - 0.135\sqrt{35} = 0.701$$

$$\begin{aligned} \text{Skin Friction} &= \beta \sigma_v A_f \\ &= 0.701 \times \frac{1437.5 + 2687.5}{2} \times (\pi \times 2 \times 20) \\ &= 181.69 \text{ kip} \end{aligned}$$

$$\begin{aligned} \text{Total Skin Friction} &= (105.89 + 181.69) \\ &= 287.58 \text{ kip} \end{aligned}$$

$$\begin{aligned} \text{Total End Bearing} &= 1.2 N A_p (\text{kip}) \\ &= 1.2 \times 30 \times \frac{\pi}{4} \times 2^2 \\ &= 113.1 \text{ kip} \end{aligned}$$

### Total Ult. Capacity,

$$Q_{up} = (287.58 + 113.1) \text{ kip} = 400.68 \text{ kip}$$

$$\text{Allowable Capacity} = \frac{Q_{up}}{F.S.}$$

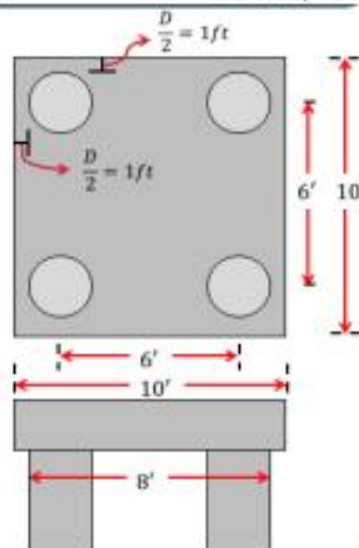
$$= \frac{400.68}{2.5} = 160.272 \text{ kip}$$

Total Load on Foundation from Column = 630 kip (Assume)

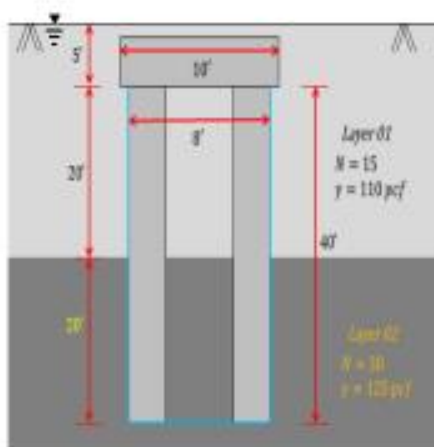
$$\text{No. of Pile required, } N = \frac{630}{160.272} = 3.93 \approx 4$$

$$\text{Inter Spacing, } S = 3D = 3 \times 2 = 6 \text{ ft}$$

$$\text{Face Spacing, } S = \frac{D}{2} = 1 \text{ ft}$$



## Group action



### Layer 01:

$$\beta = 1.5 - 0.135\sqrt{z} = 1.5 - 0.135\sqrt{15} = 0.977$$

$$\text{Skin friction} = \beta \sigma_v A_f = 0.977 \times \frac{287.5 + 1437.5}{2} \times (8 \times 20 \times 4) = 539.304 \text{ kip}$$

### Layer 02:

$$\beta = 1.5 - 0.135\sqrt{z} = 1.5 - 0.135\sqrt{35} = 0.701$$

$$\text{Skin friction} = \beta \sigma_v A_f = 0.701 \times \frac{1437.5 + 2687.5}{2} \times (8 \times 20 \times 4) = 925.32 \text{ kip}$$

$$\text{Total Skin Friction} = (539.304 + 925.32) \text{ kip} = 1464.624 \text{ kip}$$

$$\text{Total End Bearing} = 1.2 N A_p (\text{kip}) = 1.2 \times 30 \times (8 \times 8) = 2304 \text{ kip}$$

Efficiency = 80%

$$\text{Total Capacity} = 0.8(1464.624 + 2304) \text{ kip} = 3014.899 \text{ kip} > 680 \text{ kip}$$

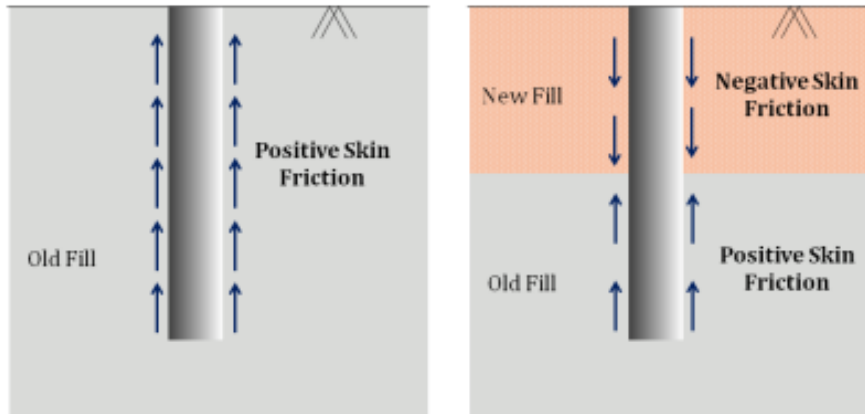
NB: Sometime Skin friction is neglected for smooth surface in group action

$$\text{Total Capacity} = 0.8(2304) \text{ kip} = 1843.2 \text{ kip} > 680 \text{ kip}$$

End of Bearing Capacity; No need for Settlement Calculation for Sand

**Special Case**

**Negative Skin Friction**



**Figure 4.5: Negative Skin Friction**

**IN CLAY SOIL**

Pile	Diameter D (ft)	Length L (ft)	$c_u$ (ksf)	$q_f = \alpha_1 c_u$ (ksf)	$A_f = \pi DL$ (kip)	$Q_{sf} = A_f * q_f$ (kip)	$Q_{eb} = 9 * c_u * A_p$ (kip)	$Q_{up} = Q_{sf} + Q_{eb}$ (kip)

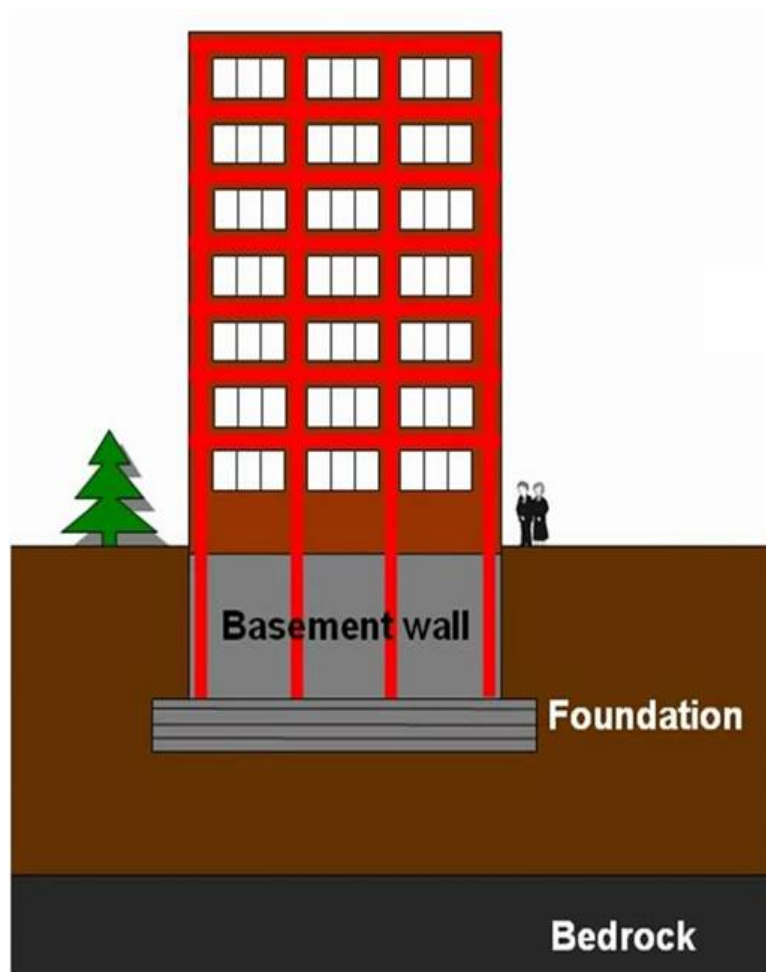
Column	Load, P (kip)	$Q_{up}$ (kip)	No. of pile reqd. (rounded), $P/Q_{up}$	Pile group length, (ft)	Pile Group Width (ft)	Group action Capacity of Pile cap	Individual action capacity of pile cap	Remarks

**IN SANDY SOIL**

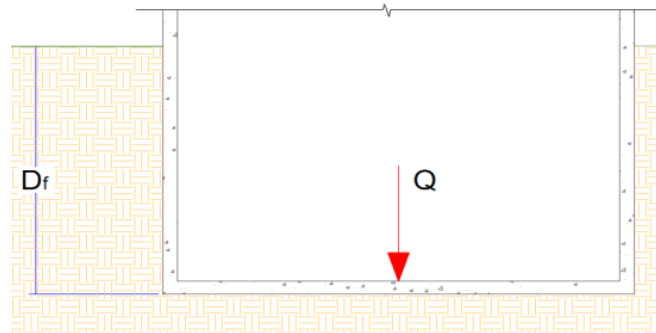
Pile	Diameter D (ft)	Length L (ft)	N (at tip level)	$Q_{eb} = 1.2 * N * A_p$ (kip)	$\beta = 1.5 - 0.135 \sqrt{z}$	$p_o' = \gamma' * z$ (ksf)	$A_f$ (sft)	$Q_{sf} = \beta * p_o' * A_f$ (kip)	$Q_{up} = Q_{sf} + Q_{eb}$ (kip)

Column	Load, P (kip)	$Q_{up}$ (kip)	No. of pile reqd. (rounded), $P/Q_{up}$	Pile group length, (ft)	Pile Group Width (ft)	Group action Capacity of Pile cap	Individual action capacity of pile cap	Remarks

# Bearing Capacity Calculation of Mat Foundation



## Determination of Depth $D_f$ of a mat foundation



The net soil pressure  $q$  under the mat is the load from the building  $Q$  over the entire mat, minus the weight of the soil excavated  $D_f \square \square$

$$q = \frac{Q}{A} - D_f \gamma$$

When the mat is fully compensated, the weight of the soil excavated is equal to the weight of the newly imposed building  $Q$ , in other words  $q = 0$  and therefore

$$D_f = \frac{Q}{A \gamma}$$

## Determination of Bearing Capacity of a mat foundation

### Mat on Clay

Mat foundations in purely cohesive soils have the following ultimate bearing capacity:

$$q_{\text{ult}(\text{net})} = 5.14 c_u \left(1 + \frac{0.195B}{L}\right) \left(1 + \frac{0.4D_f}{B}\right)$$

Here,

$c_u$  = Undrained cohesion of soil

$B$  = Width of the building

$L$  = Length of building

$D_f$  = Depth of mat foundation

### Mat on Sand

The allowable bearing capacity of a mat foundation in granular soils was proposed by Meyerhof (with a Factor of Safety of 3) to be based on the SPT corrected to a 55% efficiency as,

$$q_{\text{net}(\text{all})} = \frac{N_{60}}{0.08} \left[1 + \frac{0.33D_f}{B}\right] \left[\frac{\Delta S_c}{25.4\text{mm}}\right] \leq 16.63 N_{60} \left[\frac{\Delta S_c}{25.4\text{mm}}\right]$$

Here,

$N_{60}$  = corrected standard penetration number

$B$  = Width of the building

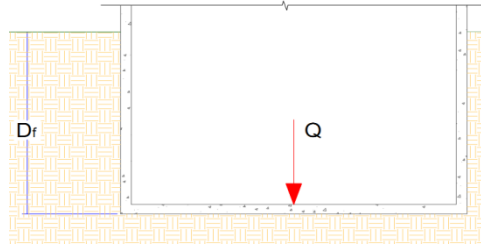
$D_f$  = Depth of mat foundation

$\Delta S_c$  = Allowable settlement for mat foundation



### **Problem 1**

The mat shown below is 30 m wide by 40 m long. The live and dead load on the mat is 200 MN. Find the depth  $D_f$  for a fully compensated foundation placed upon a soft clay with a unit weight  $\gamma = 18.75 \text{ kN/m}^3$ .



### **Solution:**

For fully compensated condition,

$$D_f = \frac{Q}{A\gamma} = \frac{200 \times 10^3}{(30 \times 40) \times 18.75} = 9 \text{ m}$$

### **Problem 2**

Determine the ultimate bearing capacity of a mat foundation measuring 70 feet long by 50 feet wide placed 8.5 feet below the surface and resting upon a saturated clay stratum with  $c_u = 1,950 \text{ lb/ft}^2$  and  $\phi = 0^\circ$ .

### **Solution:**

$$\begin{aligned} q_{\text{ult}(\text{net})} &= 5.14 c_u \left(1 + \frac{0.195B}{L}\right) \left(1 + \frac{0.4D_f}{B}\right) \\ &= 5.14 * 1.95 * \left(1 + \frac{0.195 * 50}{70}\right) * \left(1 + \frac{0.4 * 8.5}{50}\right) = \text{ksf} \end{aligned}$$

### **Problem 3**

What will be the net allowable bearing capacity of a mat foundation 15 m long by 10 m wide, embedded 2 m into a dry sand stratum with a corrected SPT to 60% efficiency  $N_{60} = 10$ . It is desired that the allowable settlement is  $\Delta S_c = 30 \text{ mm}$ .

### **Solution:**

$$\begin{aligned} q_{\text{net}(\text{all})} &= \frac{N_{60}}{0.08} \left[1 + \frac{0.33D_f}{B}\right] \left[\frac{\Delta S_c}{25.4 \text{ mm}}\right] \leq 16.63 N_{60} \left[\frac{\Delta S_c}{25.4 \text{ mm}}\right] \\ &= \frac{10}{0.08} * \left[1 + \frac{0.33 * 2}{10}\right] \left[\frac{30 \text{ mm}}{25.4 \text{ mm}}\right] = \text{KN/m}^2 \end{aligned}$$

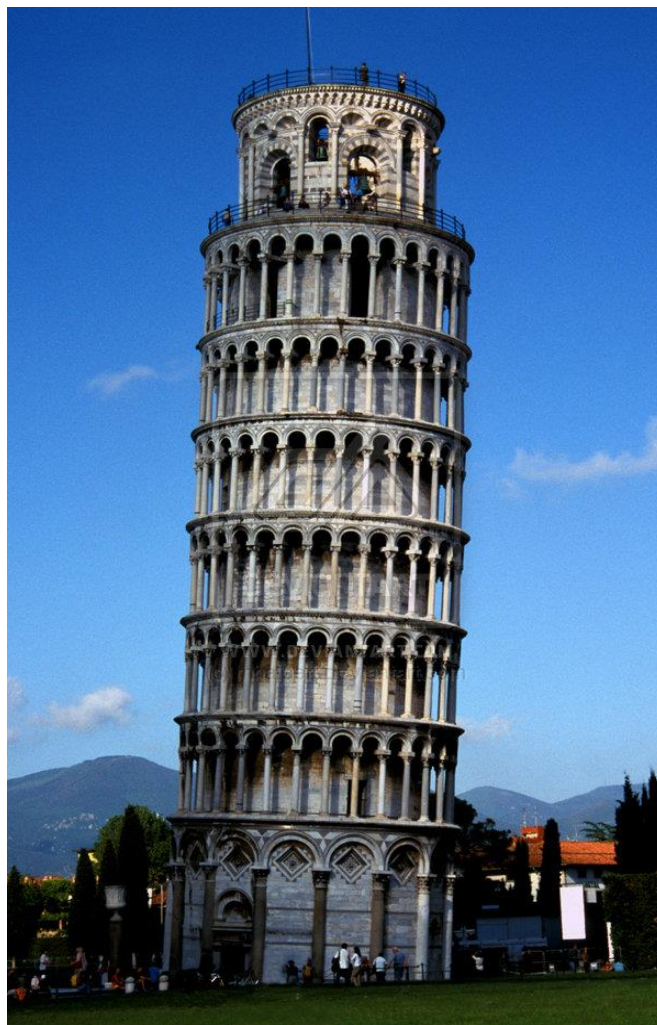
Again,

$$\begin{aligned} &16.63 N_{60} \left[\frac{\Delta S_c}{25.4 \text{ mm}}\right] \\ &= 16.63 * 10 \left[\frac{30 \text{ mm}}{25.4 \text{ mm}}\right] = \end{aligned}$$

So,

$$q_{\text{net}(\text{all})} = \text{KN/m}^2$$

## Soil Settlement Calculation



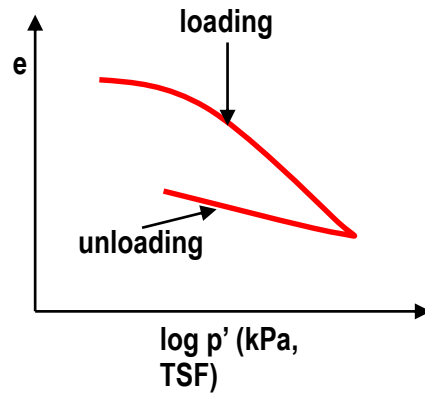
**Q:** If the soil is clayey soil, calculate the consolidation settlement and check the differential settlement for the columns.

Solution:

**Estimation of Consolidation Settlement of Clay Soils**

One dimensional consolidation test results:

(Used for estimating total consolidation settlement)



**Normally consolidated clay:** whose present effective overburden pressure is the maximum pressure that the soil was subjected to in the past.

**Over consolidated clay:** whose present effective overburden pressure is less than that which the soil experienced in the past.

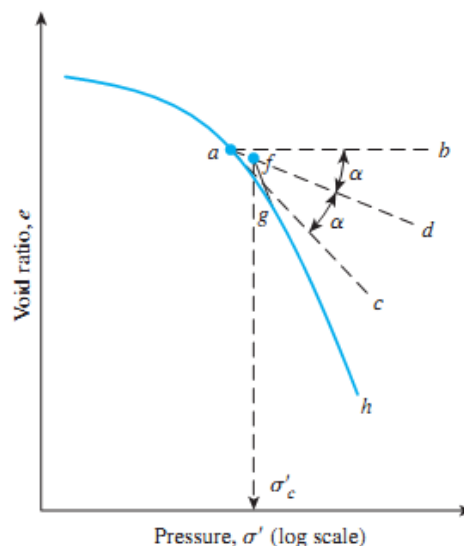
**Pre-consolidation pressure** is the maximum effective past pressure.

Normally consolidated clay:  $p'_o = p_c'$

Over consolidated clay:  $p'_o < p_c'$ ,  $OCR = p_c'/p_o'$

**Step 1: Determination of pre consolidation pressure,  $p_o$**

1. By visual observation, establish point a, at which the e–logp plot has a minimum radius of curvature.
2. Draw a horizontal line ab.
3. Draw the line ac tangent at a.
4. Draw the line ad, which is the bisector of the angle bac.
5. Project the straight-line portion gh of the e–logp plot back to intersect line ad at f. The abscissa of point f is the preconsolidation pressure,  $p_c$ .



## Step 2: Calculation of Consolidation settlement

### For Normally consolidated clay:

$$S_c = \frac{C_c H}{(1+e_o)} \log_{10} \frac{p_o + \Delta P}{p_o}$$

Here,

$C_c$  = Compressibility Index

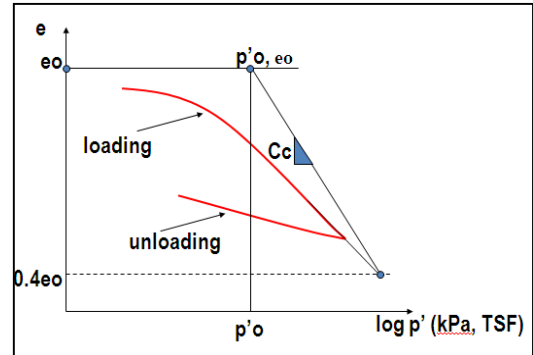
$H$  = Height of clay layer (from footing bed to mid height of clay layer)

$e_o$  = Initial void ratio

$p_o$  = Effective overburden pressure,  $p_o = \gamma h$

$h = D_f + H$

$\Delta P$  = Additional pressure due to structure  $\Delta P = \frac{\text{Load}}{(B+H)^2}$



Field consolidation line for normally consolidated clay

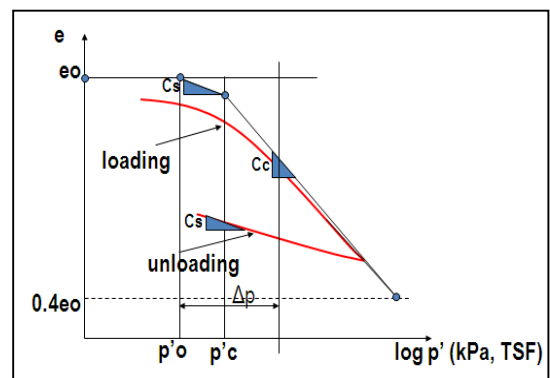
### For Over consolidated clay:

Case 1:  $(p_o + \Delta p) \leq p_c$ :

$$S_c = \frac{C_s H}{(1+e_o)} \log_{10} \frac{p_o + \Delta P}{p_o}$$

Case 2:  $(p_o + \Delta p) > p_c$ :

$$S_c = \frac{C_s H}{(1+e_o)} \log_{10} \frac{p_c}{p_o} + \frac{C_c H}{(1+e_o)} \log_{10} \frac{p_o + \Delta P}{p_c}$$



Field consolidation line for over consolidated clay

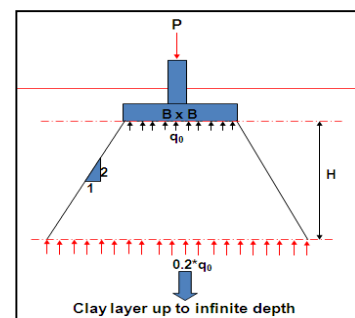
### Definition of H for infinite depth of clay layer:

Solution of the equation:

$$P/(B+H)^2 = 0.2 * P/B^2$$

Gives:

$$H \approx 1.25B$$



**Consolidation settlement data sheet**

Initial void ratio,  $e_o =$

Pre-consolidation pressure,  $p_c =$

Compressibility index,  $C_c =$

Swelling index,  $C_s =$

Column	Depth of Foundation $D_f$	Width of footing $B$	Load from structure	Height of clay layer $H$	Additional pressure due to structure. $\Delta P = \frac{Load}{(B+H)^2}$	Effective overburden pressure $P_o = \gamma H$	Consolidation Type	$C_c$	$C_s$	Consolidation Settlement $S_c$

**Step 3: Check Angular Rotation for differential settlement**

Differential settlement for two columns  $C_1$  and  $C_2$ :

$$\Delta S = S_c C_1 - S_c C_2$$

Angular rotation:

$$\frac{\Delta S}{L} \quad (L = \text{center to center distance between two columns})$$

$$\frac{\Delta S}{L} < \frac{1}{300} = \text{OK}$$

$$\frac{\Delta S}{L} > \frac{1}{300} = \text{Not OK}$$

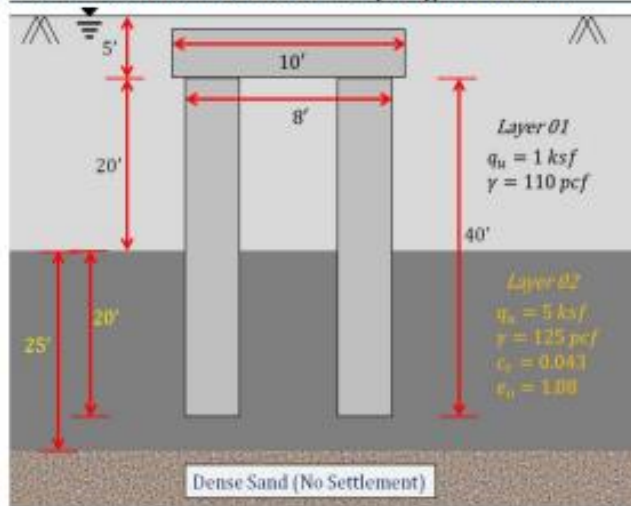
Angular Rotation Check data sheet:

Considered Columns	Corresponding span, $L$	Differential settlement, $\Delta S$	Angular rotation $\frac{\Delta S}{L}$	Check $\frac{\Delta S}{L} < \frac{1}{300} = \text{OK}$

\* For each column differential settlement of nearest two columns should be checked.

## SETTLEMENT FOR BORED PILE

**Example:** Calculate the settlement of the bored pile given below.



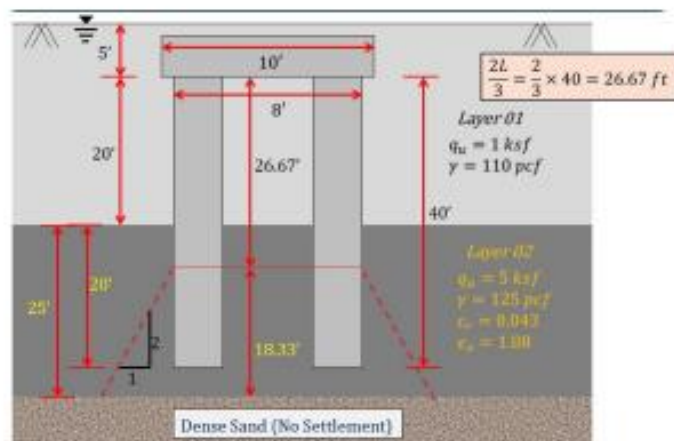
**Solution:**

$$P_o = \sum \gamma' h$$

upto mid layer of 18.33' zone  
 $= 25 \times (110 - 62.5)$   
 $+ \left(6.67 + \frac{18.33}{2}\right)(125 - 62.5)$   
 $= 2177.1875 \text{ psf}$

$$\Delta P = \frac{380 \times 1000}{\left(8 + \frac{18.33}{2}\right)^2} = 1289.72 \text{ psf}$$

$H_c = 18.33 \text{ ft}$



$$S = \frac{c_r H_c}{1 + e_o} \log \left( \frac{P_o + \Delta P}{P_o} \right)$$

$$= \frac{0.043 \times 18.33 \times 12}{1 + 1.08} \log \left( \frac{2177.1875 + 1289.72}{2177.1875} \right)$$

$$= 0.92 \text{ inch} < 2 \text{ inch}$$

**NB:** If  $S > 2''$ , Greater depth should be provided but then required no. of pile may reduce in respect of bearing capacity

## SETTLEMENT OF MAT FOOTING

- ❑ Basically same as individual footing (Single Footing), difference is in individual footing we have calculated one settlement but in mat footing we have to calculate two settlement
  1. Settlement in corner
  2. Settlement in center
- ❑ As individual footing is generally small in size, so its settlement in corner and settlement in center is almost equal. So we have calculated it in one time
- ❑ In mat footing, as it is large in size, their settlement in corner and center varies. So we have to calculate two settlements. For this variable settlement in corner and center extra stress develops. So we can't neglect it.

$$S = \frac{C_c H_c}{1 + e_o} \log \left( \frac{P_o + \Delta P}{P_o} \right)$$

Increase in vertical stress ( $\Delta P$ ) is found by -----

- ❖ **2:1 Method** : Used for individual footing and Pile foundation
- ❖ **Empherical Formula** : Used for Mat Footing
- ❖ **Fadum Chart** : Used for Mat Footing
- ❖ **Newmark's Influence Chart** : Used for Mat Footing **etc.**

For Mat Foundation

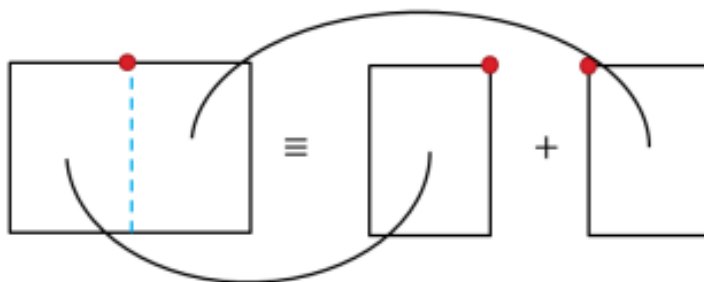
- ❖ Empherical Formula
- ❖ Fadum Chart
- ❖ Newmark's Influence Chart etc.

**Note 1:**

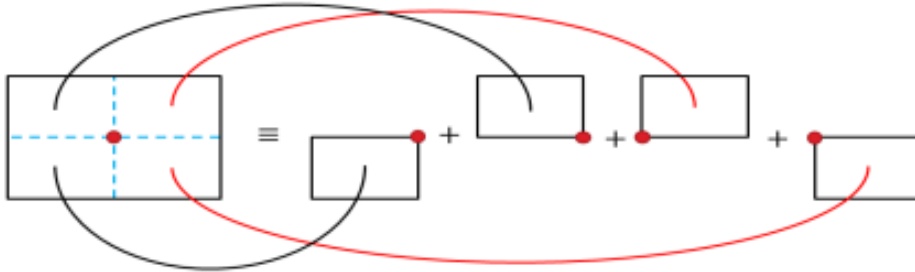
For **Empherical Formula** and **Fadum Chart** we can only determine the **increase in vertical stress ( $\Delta P$ )** at corner; so if we have to determine  $\Delta P$  at other point then we have to make it corner.

**Example:**

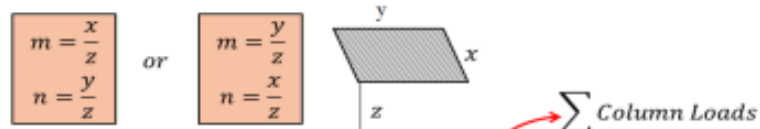
Determine  $\Delta P$  at denoted point



**Example:**  
Determine  $\Delta P$  at denoted point



**Note 2:**  
For **Emperical Formula and Fadum Chart**

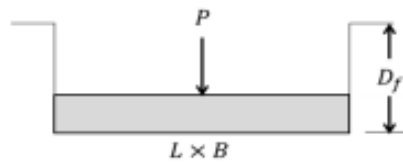


$$\Delta P = q_o \times I$$

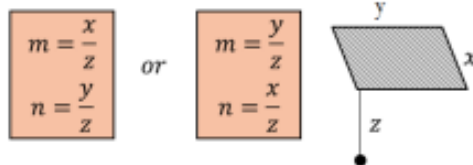
$$q_o = q - \gamma D_f$$

$$q = \frac{P}{L \times B}$$

$$I = f(m, n)$$

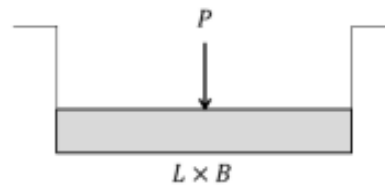


**Emperical Formula**



$$\Delta P = q_o \times I$$

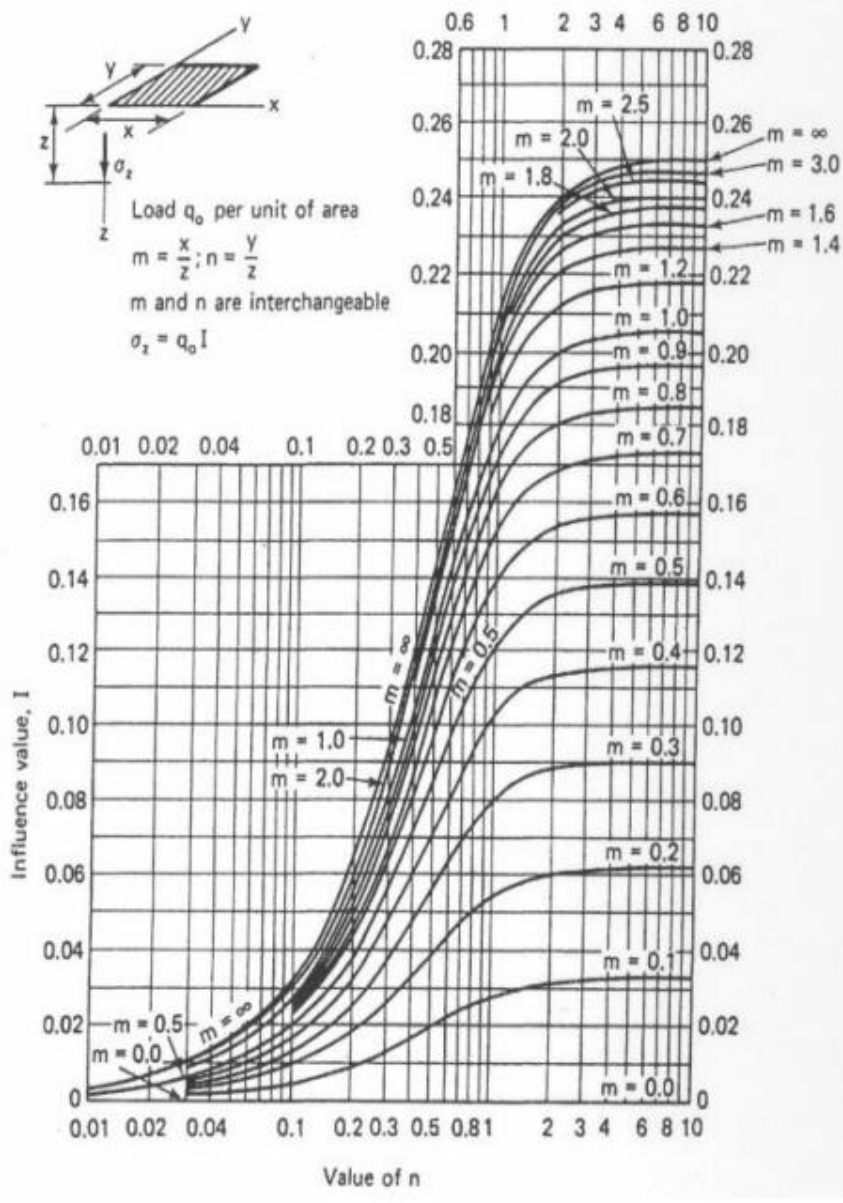
$$I = f(m, n)$$



$$I = \frac{1}{4\pi} \left[ \frac{2mn\sqrt{m^2+n^2+1}}{m^2+n^2+m^2n^2+1} \left( \frac{m^2+n^2+2}{m^2+n^2+1} \right) + \tan^{-1} \left( \frac{2mn\sqrt{m^2+n^2+1}}{m^2+n^2-m^2n^2+1} \right) \right]$$

**Radian**

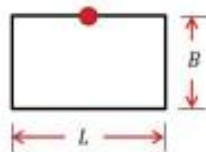




### Newmark's Influence Chart

A point where  $\Delta P$  is required must be at the center of the Newmark's Influence Chart

**Example:**

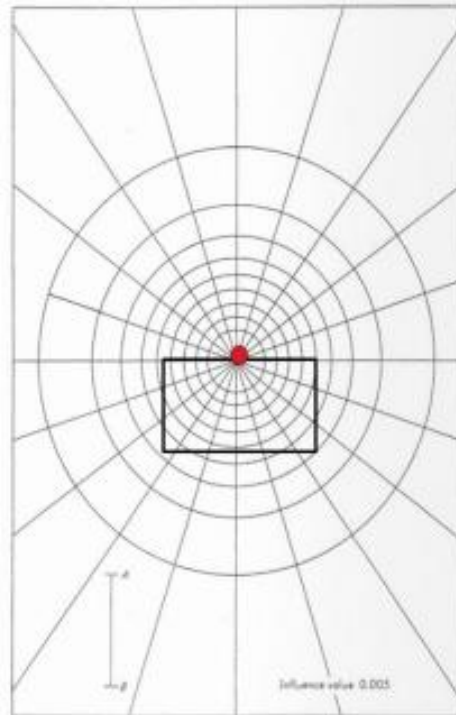


$$L = AB \text{ or } B = AB$$

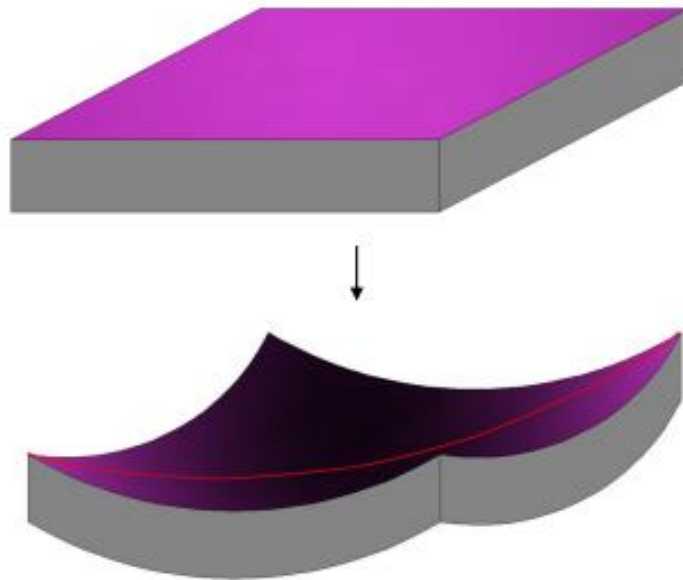
$$\Delta P = q_o IN$$

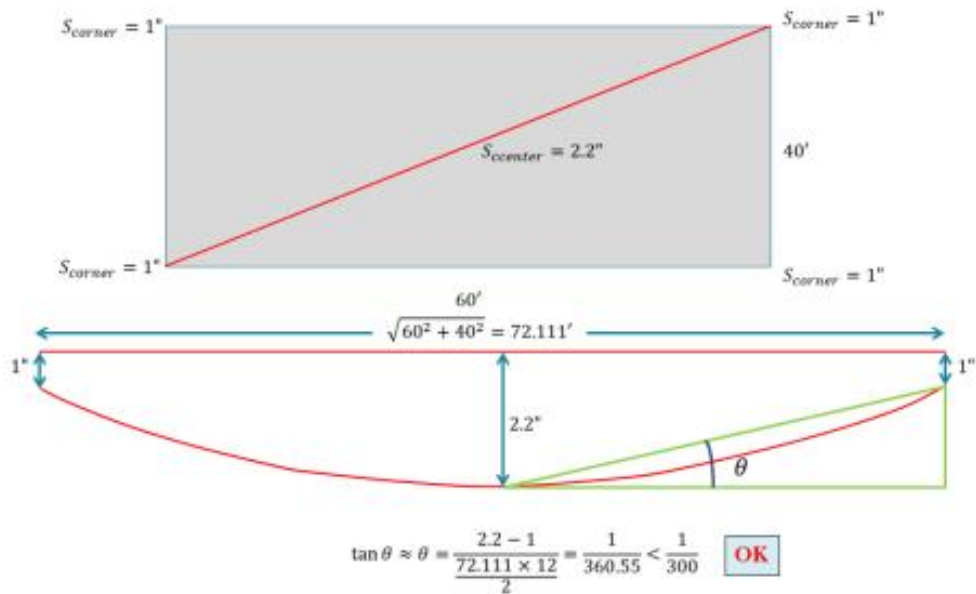
$I$  = Influence Value = 0.005

$N$  = Number of blocks with in the shape



When calculating **settlement** of Mat footing, **rotation** is also determined

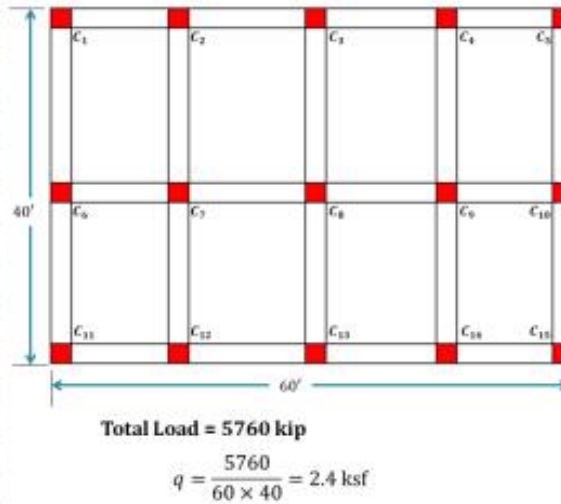




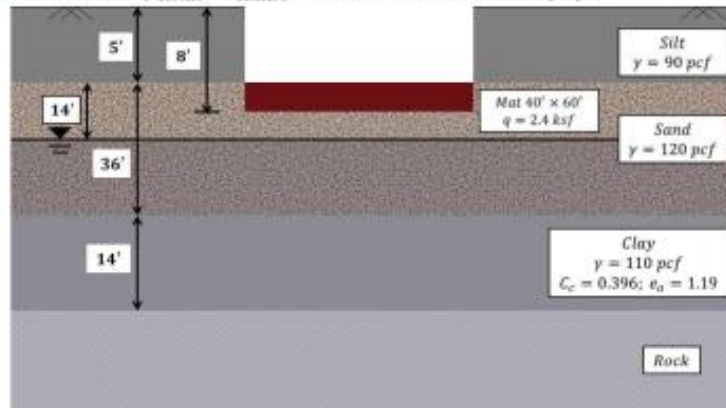
In 1956, Skempton and McDonald proposed the following limiting values for maximum settlement and maximum angular distortion, to be used for building purposes:

Maximum settlement, $S_{T(max)}$	
In sand	32 mm
In clay	45 mm
Maximum differential settlement, $\Delta S_{T(max)}$	
Isolated foundations in sand	51 mm
Isolated foundations in clay	76 mm
Raft in sand	51–76 mm
Raft in clay	76–127 mm
Maximum angular distortion, $\beta_{max}$	1/300

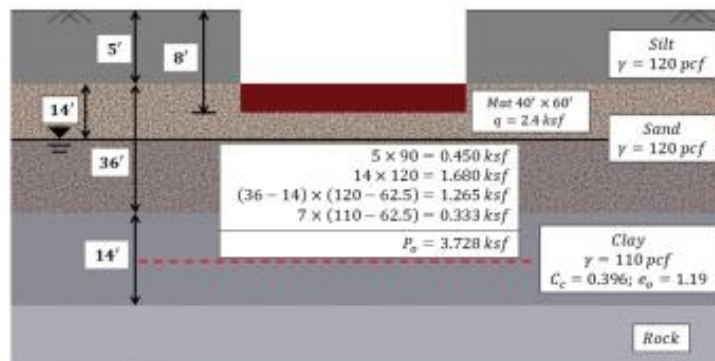
Column	Load (kip)
C <sub>1</sub>	400
C <sub>2</sub>	380
C <sub>3</sub>	386
C <sub>4</sub>	390
C <sub>5</sub>	370
C <sub>6</sub>	375
C <sub>7</sub>	379
C <sub>8</sub>	425
C <sub>9</sub>	350
C <sub>10</sub>	384
C <sub>11</sub>	397
C <sub>12</sub>	389
C <sub>13</sub>	378
C <sub>14</sub>	387
C <sub>15</sub>	370



**Example:** Find settlement ( $S_{corner}$  &  $S_{center}$ ) of Mat foundation due to 14' clay layer



**Solution:**



**Corner:**

$$m = \frac{x}{z} = \frac{60}{40} = 1.5$$

$$n = \frac{y}{z} = \frac{40}{40} = 1$$

Interchangable

$z =$  distance between **bottom of footing** and **mid clay layer**

$q = 2.4 \text{ ksf} = 2400 \text{ psf}$

Contact Pressure,  
 $q_o = 2400 - 5 \times 90 - 3 \times 120 = 1590 \text{ psf}$

$$I = \frac{1}{4\pi} \left[ \frac{2mn\sqrt{m^2+n^2+1}}{m^2+n^2+m^2n^2+1} \left( \frac{m^2+n^2+2}{m^2+n^2+1} \right) + \tan^{-1} \left( \frac{2mn\sqrt{m^2+n^2+1}}{m^2+n^2-m^2n^2+1} \right) \right]$$

$I = 0.194$

$\Delta P = I \times q_o = 0.196 \times 1590 = 308.46 \text{ psf}$

**Center:**

$$m = \frac{x}{z} = \frac{30}{40} = 0.75$$

$$n = \frac{y}{z} = \frac{20}{40} = 0.5$$

Interchangable

$z =$  distance between **bottom of footing** and **mid clay layer**

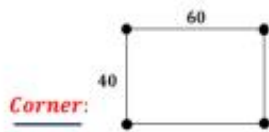
$q = 2.4 \text{ ksf} = 2400 \text{ psf}$

Contact Pressure,  
 $q_o = 2400 - 5 \times 90 - 3 \times 120 = 1590 \text{ psf}$

$$I = 0.107$$

$\Delta P = 4I \times q_o = 4 \times 0.107 \times 1590 = 680.52 \text{ psf}$

**ΔP determination (Fadum Chart)**



$$m = \frac{x}{z} = \frac{60}{40} = 1.5$$

$$n = \frac{y}{z} = \frac{40}{40} = 1$$

} **Interchangeable**

$z$  = distance between **bottom of footing** and **mid clay layer**

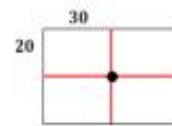
$q = 2.4 \text{ ksf} = 2400 \text{ psf}$

Contact Pressure,

$$q_o = 2400 - 5 \times 90 - 3 \times 120 = 1590 \text{ psf}$$

$l = 0.196$

$$\Delta P = l \times q_o = 0.196 \times 1590 = 311.64 \text{ psf}$$



$$m = \frac{x}{z} = \frac{30}{40} = 0.75$$

$$n = \frac{y}{z} = \frac{20}{40} = 0.5$$

} **Interchangeable**

$z$  = distance between **bottom of footing** and **mid clay layer**

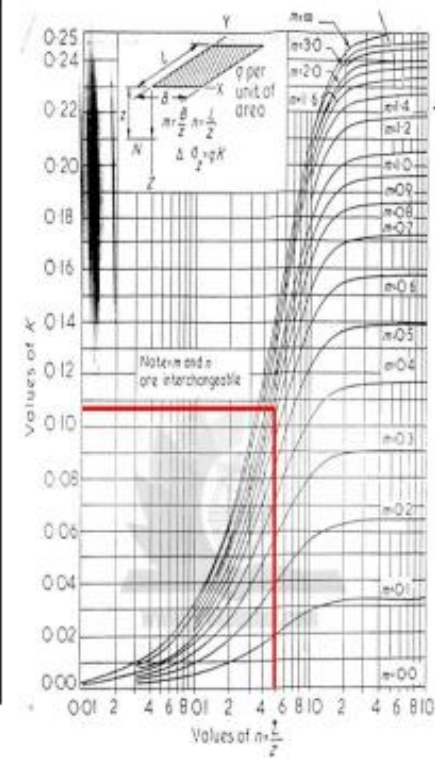
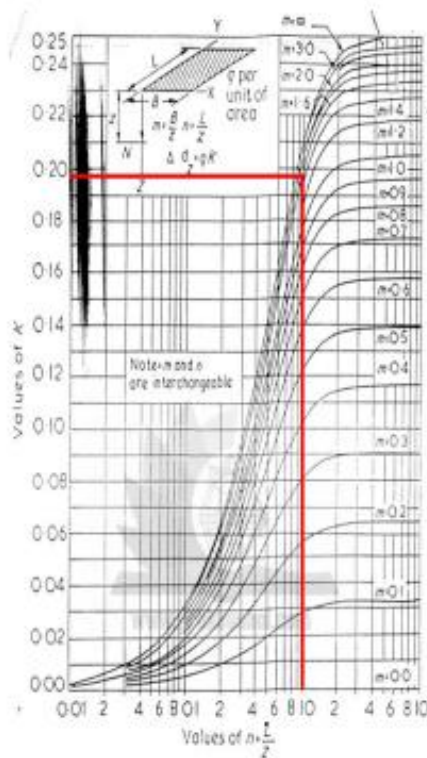
$q = 2.4 \text{ ksf} = 2400 \text{ psf}$

Contact Pressure,

$$q_o = 2400 - 5 \times 90 - 3 \times 120 = 1590 \text{ psf}$$

$l = 0.107$

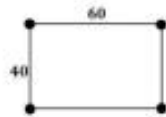
$$\Delta P = 4l \times q_o = 4 \times 0.107 \times 1590 = 680.52 \text{ psf}$$



$\Delta P$  determination (Newmark's Influence Chart)

**Corner:**

$AB = 60 \text{ ft}$

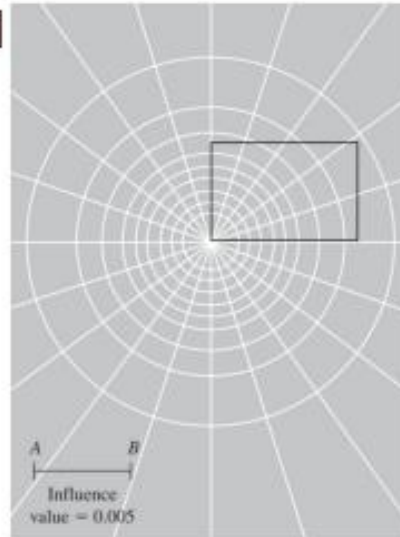


$\Delta P = q_0 IN$

$I = \text{Influence Value} = 0.005$

$N = \text{Number of Blocks within the Rectangular Area} = 38.6$

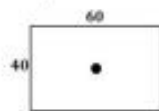
$\Delta P = 1590 \times 0.005 \times 38.6 = 306.87 \text{ psf}$



$\Delta P$  determination (Newmark's Influence Chart)

**Center:**

$AB = 60 \text{ ft}$

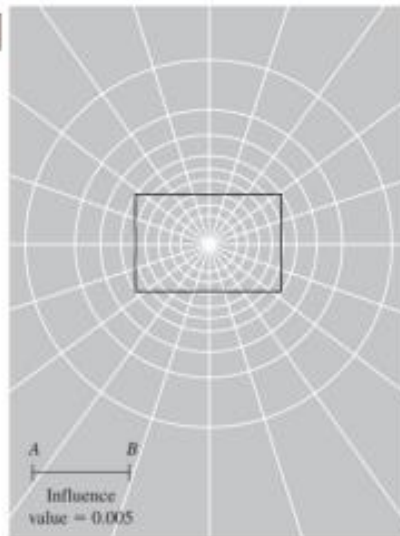


$\Delta P = q_0 IN$

$I = \text{Influence Value} = 0.005$

$N = \text{Number of Blocks within the Rectangular Area} = 84.8$

$\Delta P = 1590 \times 0.005 \times 84.8 = 674.16 \text{ psf}$



$$S = \frac{C_c H_c}{1 + e_o} \log \left( \frac{P_o + \Delta P}{P_o} \right)$$

$$P_o = 3.728 \text{ ksf} = 3728 \text{ psf}$$

$$C_c = 0.396$$

$$e_o = 1.19$$

$$H_c = 14' = 14 \times 12 = 168''$$

Empherical Formula

**Corner:**

$$\Delta P = 311.64 \text{ psf}$$

$$S = \frac{0.396 \times 168}{1 + 1.19} \log \left( \frac{3728 + 311.64}{3728} \right)$$

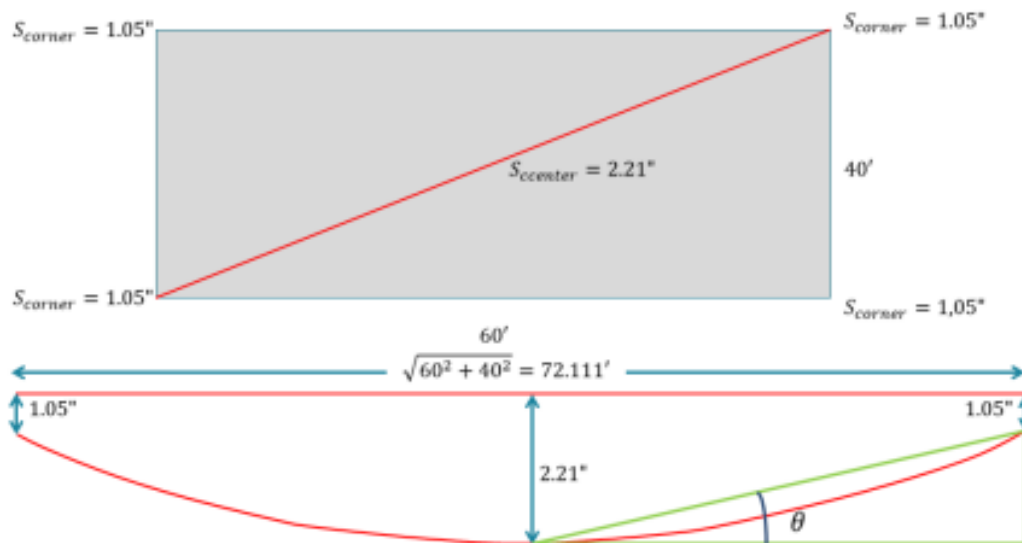
$$= 1.06'' < 2.56''$$

**Center:**

$$\Delta P = 680.52 \text{ psf}$$

$$S = \frac{0.396 \times 168}{1 + 1.19} \log \left( \frac{3728 + 680.52}{3728} \right)$$

$$= 2.21'' < 2.56''$$



$$\tan \theta \approx \theta = \frac{2.21 - 1.05}{\frac{72.111 \times 12}{2}} = \frac{1}{372.99} < \frac{1}{300} \quad \text{OK}$$

$$S = \frac{C_c H_c}{1 + e_o} \log \left( \frac{P_o + \Delta P}{P_o} \right)$$

$$P_o = 3.728 \text{ ksf} = 3728 \text{ psf}$$

$$C_c = 0.396$$

$$e_o = 1.19$$

$$H_c = 14' = 14 \times 12 = 168''$$

Fadum Chart

**Corner:**

$$\Delta P = 308.46 \text{ psf}$$

$$S = \frac{0.396 \times 168}{1 + 1.19} \log \left( \frac{3728 + 308.46}{3728} \right)$$

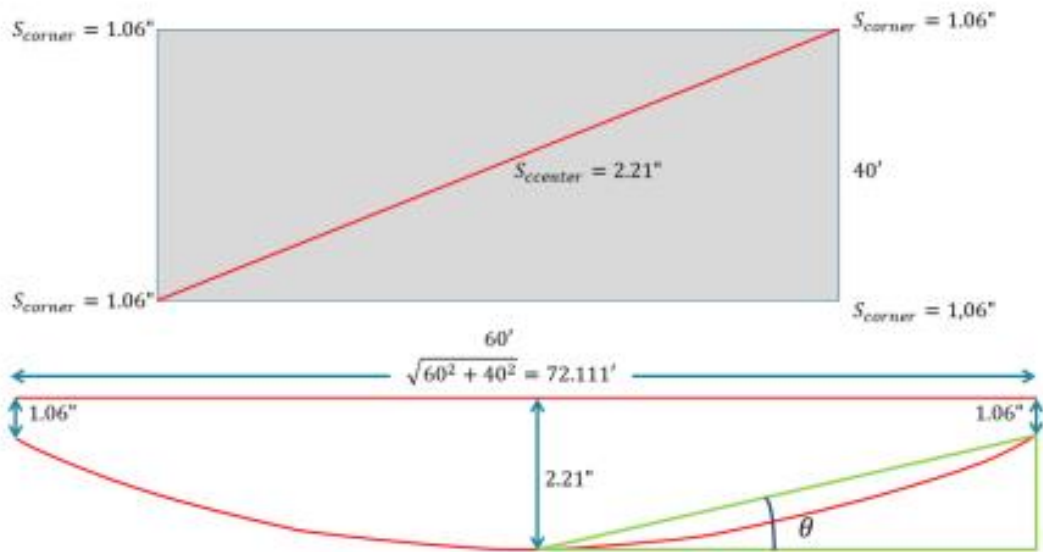
$$= 1.05'' < 2.56'' \text{ [OK]}$$

**Center:**

$$\Delta P = 680.52 \text{ psf}$$

$$S = \frac{0.396 \times 168}{1 + 1.19} \log \left( \frac{3728 + 680.52}{3728} \right)$$

$$= 2.21'' < 2.56'' \text{ [OK]}$$



$$\tan \theta \approx \theta = \frac{2.21 - 1.06}{\frac{72.111 \times 12}{2}} = \frac{1}{376.23} < \frac{1}{300} \quad \text{OK}$$



$$S = \frac{C_c H_c}{1 + e_o} \log \left( \frac{P_o + \Delta P}{P_o} \right)$$

$$P_o = 3.728 \text{ ksf} = 3728 \text{ psf}$$

$$C_c = 0.396$$

$$e_o = 1.19$$

$$H_c = 14' = 14 \times 12 = 168''$$

Newmark's Influence Chart

**Corner:**

$$\Delta P = 306.87 \text{ psf}$$

$$S = \frac{0.396 \times 168}{1 + 1.19} \log \left( \frac{3728 + 306.87}{3728} \right)$$

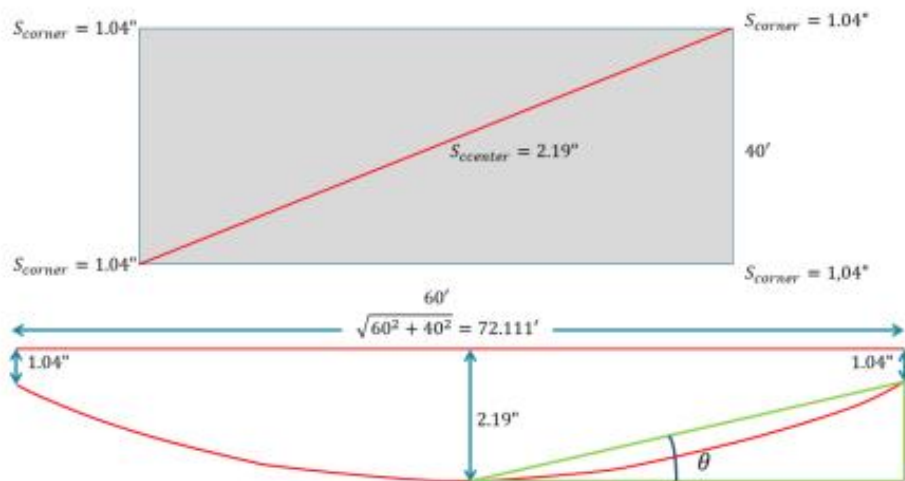
$$= 1.04'' < 2.56'' \text{ [OK]}$$

**Center:**

$$\Delta P = 674.16 \text{ psf}$$

$$S = \frac{0.396 \times 168}{1 + 1.19} \log \left( \frac{3728 + 674.16}{3728} \right)$$

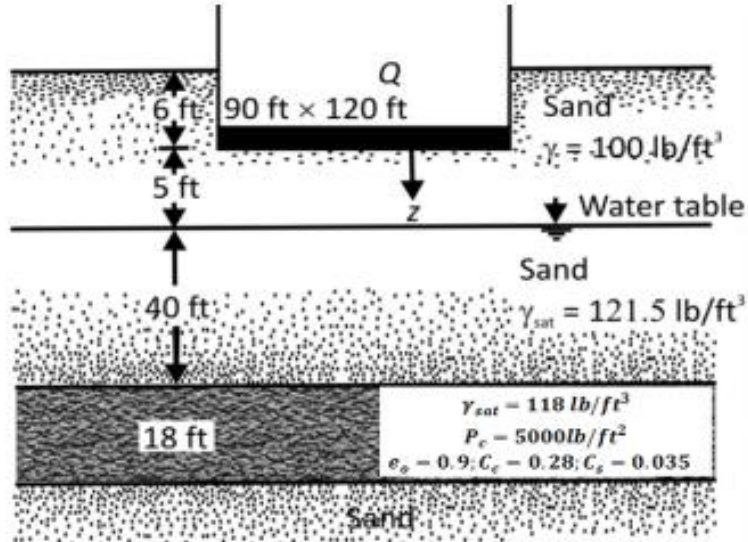
$$= 2.19'' < 2.56'' \text{ [OK]}$$



$$\tan \theta \approx \theta = \frac{2.19 - 1.04}{\frac{72.111 \times 12}{2}} = \frac{1}{376.23} < \frac{1}{300} \quad \text{OK}$$

**Example :**

Consider a mat foundation 90 ft × 120 ft in plan, as shown in Figure. The total dead load and live load on the raft is 45 × 10<sup>3</sup> kip. Estimate the **consolidation settlement** at the **center** of the foundation.



**Solution:**

ΔP determination (Empirical Formula)

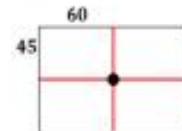
Center:

$$m = \frac{x}{z} = \frac{60}{54} = 1.111$$

$$n = \frac{y}{z} = \frac{45}{54} = 0.833$$

} **Interchangeable**

z = distance between **bottom of footing** and **mid clay layer**



$$q_o = q - \gamma D_f$$

$$= \frac{P}{L \times B} - \gamma D_f$$

$$= \frac{45 \times 10^6}{120 \times 90} - 100 \times 6$$

$$= 3566.67 \text{ psf}$$

$$I = \frac{1}{4\pi} \left[ \frac{2mn\sqrt{m^2+n^2+1}}{m^2+n^2+m^2n^2+1} \left( \frac{m^2+n^2+2}{m^2+n^2+1} \right) + \tan^{-1} \left( \frac{2mn\sqrt{m^2+n^2+1}}{m^2+n^2-m^2n^2+1} \right) \right]$$

$$I = 0.168$$

$$\Delta P = 4I \times q_o = 4 \times 0.168 \times 3566.67 = 2396.80 \text{ psf}$$

$$P_o = 11 \times 100 + 40 \times (121.5 - 62.4) + \frac{18}{2} \times (118 - 62.4) = 3964.4 \text{ psf}$$

$$C_c = 0.28$$

$$C_s = 0.035$$

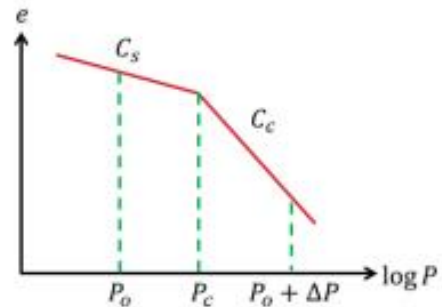
$$e_o = 0.9$$

$$H_c = 18' = 18 \times 12 = 216 \text{ inch}$$

$$\Delta P = 2396.8 \text{ psf}$$

$$P_o + \Delta P = 3964.4 + 2396.8 = 6361.2 \text{ psf}$$

$$P_o < (P_c = 5000 \text{ psf}) < P_o + \Delta P$$



$$S = \frac{C_s H_c}{1 + e_o} \log\left(\frac{P_c}{P_o}\right) + \frac{C_c H_c}{1 + e_o} \log\left(\frac{P_o + \Delta P}{P_c}\right)$$

$$= \frac{0.035 \times 216}{1 + 0.9} \log\left(\frac{5000}{3964.4}\right) + \frac{0.28 \times 216}{1 + 0.9} \log\left(\frac{6361.2}{5000}\right)$$

$$= 3.73" (< 3.94 \text{ in})$$

OK

### Skempton and MacDonald suggested the following permissible settlements

#### SANDS

- Maximum total settlement = 40 mm for isolated footing  
= 40 – 65 mm for rafts.
- Maximum differential settlement = 25 mm between adjacent columns.

#### CLAYS

- Maximum total settlement = 65 mm for isolated footing  
= 65 – 100 mm for rafts.
- Maximum differential settlement = 40 mm between adjacent columns.

# Structural Design of Foundation



## Design of Isolated Footing

### Step 1: Footing size

Column load (DI+LL) = P

Considering self weight of footing is 3% of column load.

# Footing area,  $A = \frac{P \times 1.03}{q_a}$  (rounded value)

# Width of footing,  $B = \sqrt{A}$  (for square footing)

# Net under pressure producing shear and bending,  $q_{net} = \frac{1.2DI + 1.6LL}{A}$

# Assume any thickness = t

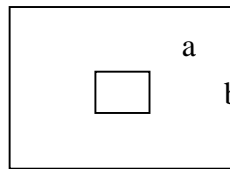
Assuming t :

Footing length	Thickness
3'	12"
8'	2'
10'	2.5'
12'	3'

### Step 2: Punching Shear Check

# Punching Shear:

$$V = P - \frac{(a+d)(b+d)}{144} \times q_{net}$$



Here,  
a, b = column dimension  
d = t - 3  
(3" clear cover at footing)

# Resistive/ Allowable Shear:

$$V = 2\sqrt{f'_c} b_o d \text{ (WSD)}$$

$$V = 4\phi\sqrt{f'_c} b_o d \text{ (USD)}$$

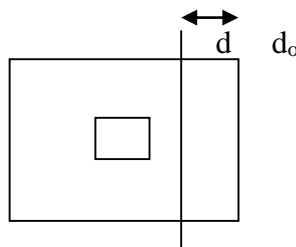
\*  $b_o = 2(a+d) + 2(b+d)$

\* If resistive/ allowable shear is greater than punching shear than ok. If smaller than increase thickness.

### Step 3: Beam Shear Check

# Beam Shear:

$$V = q_{net} d_o$$



# Resistive/ Allowable Shear:

$$V = 1.1\sqrt{f'_c} b_o d \text{ (WSD)}$$

$$V = 2\phi\sqrt{f'_c} b_o d \text{ (USD)}$$

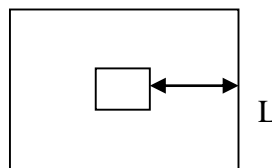
### Step 4: Moment calculation

$$\text{Moment, } M = \frac{q_{net} L^2}{2}$$

For short direction,  $M_s$

For long direction,  $M_L$

(For square footing both side is equal,  
So moment will be same.)



## Step 5: Reinforcement calculation

### WSD method:

$$\# n = \frac{E_s}{E_c} = \frac{E_s}{57000\sqrt{f'_c}}$$

$$\# r = \frac{f_s}{f_c} = \frac{0.4f_y}{0.45f'_c}$$

$$\# k = \frac{n}{n+r}$$

$$\# J = 1 - \frac{K}{3}$$

$$\# R = \frac{f_c}{2} kJ$$

$$\# d = \sqrt{\frac{M}{Rb}}$$

$$\# A_s = \frac{M}{f_s J d}$$

$$\# A_{s \min} = \frac{200}{f_y} bd$$

### USD method:

$$\# r_{\max} = 0.85\beta_1 \frac{f'_c}{f_y} \frac{\epsilon_u}{\epsilon_u + \epsilon_y}$$

$$\# R = r_{\max} f_y \left(1 - 0.59 r_{\max} \frac{f_y}{f'_c}\right)$$

$$\# d = \sqrt{\frac{M}{Rb}}$$

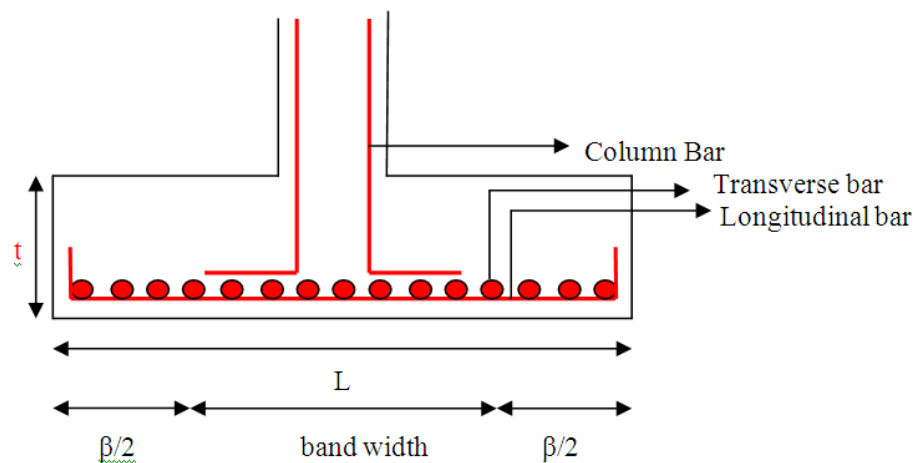
$$\# A_s = \frac{M}{0.9f_y(d - \frac{a}{2})} \text{ check. } A = \frac{A_s f_y}{0.85f'_c b}$$

Reinforcement at band width:

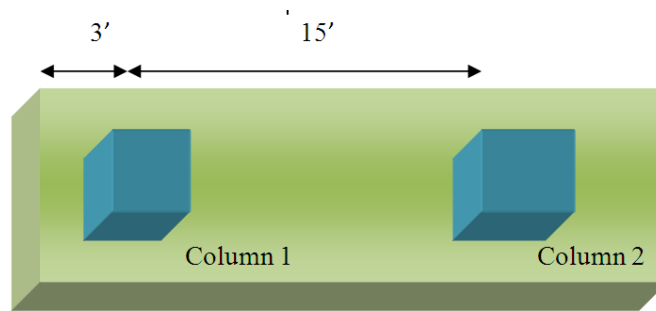
$$\text{Band width, } \beta = \frac{L}{B}$$

$$A_s \text{ in band width} = A_s \times \frac{2}{\beta + 1}$$

### Detailing:



## Design of Combined Footing



### Given Data:

#### **Column 1:**

Size: 16" X 20"

Dead Load: 150 kips

Live Load: 100 Kips

#### **Column 2:**

Size: 20" X 20"

Dead Load: 230 kips

Live Load: 180 Kips

Center to center distance between columns: 15'

Limited length from column 1 to edge: 3'

Depth of foundation: 5'

Allowable Bearing capacity of soil: 6 ksf

Concrete compressive strength: 3ksi

Yield strength of steel: 60 ksi

Design the footing

### Solution:

#### Step 1: Calculation of footing size

Assume the average unit weight of concrete and soil filling 5' from EGI is  $\frac{100+150}{2} = 125$  psf

So pressure due to soil and concrete =  $5 \times 125 = 625$  psf

Available bearing pressure of soil for footing,  $q_a = 6000 - 625 = 5375$  psf = 5.375ksf

Required footing are =  $\frac{DL+LL}{q_a} = \frac{(230+150)+(180+100)}{5.375} = 122.8$  sft

Now we have to find the resultant of column loads.

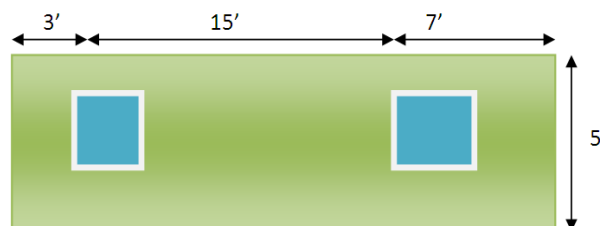
Distance from the left column:  $\frac{(150+100) \times 0 + (230+180) \times 15}{(150+100+230+180)} = 9.32'$

So the length existing of left side of the resultant force point is  $9.32+3 = 12.32$

So, total length is  $12.32+12.32 = 24.64'$ . Select 25'

Required width =  $\frac{122.8}{25} = 4.912'$  Select 5'

Size of the combined footing is 25'X5'



#### Step 2: Draw SFD & BMD of the Footing

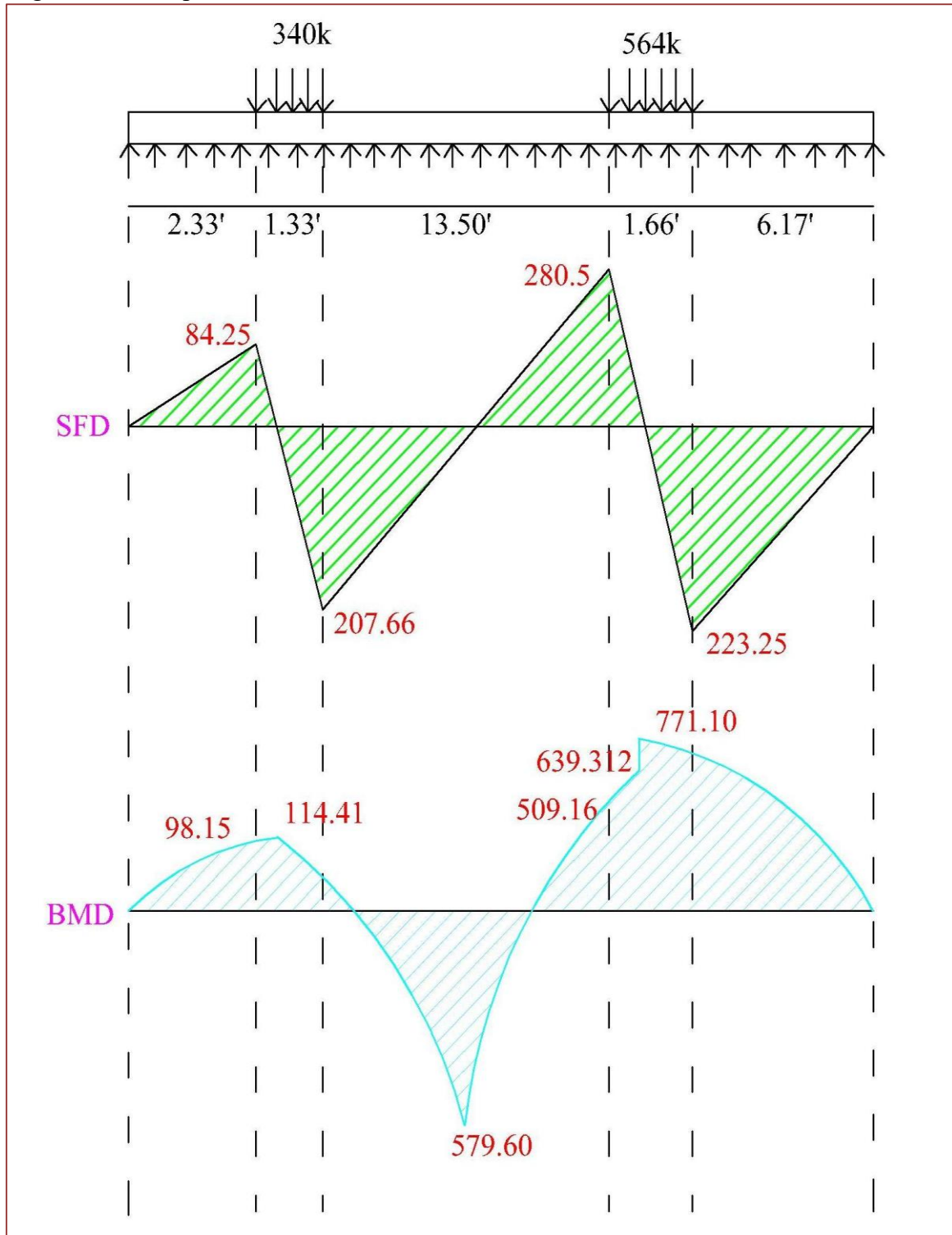
Factored load on exterior column =  $1.2 \times 150 + 1.6 \times 100 = 320\text{K}$

Factored load on exterior column =  $1.2 \times 230 + 1.6 \times 180 = 564\text{K}$

Net upward ultimate pressure =  $\frac{\text{Total Load}}{\text{Area of footing}} = \frac{320+564}{25 \times 5} = 7.232\text{K/ft}$

Width of footing = 5'

Longitudinal load per feet =  $7.232 \times 5 = 36.16'$



**Step 3: Design Beam & punching Shear**



Let thickness of footing = 25" + 5" = 30" so d = 30 - 3 = 27"

**Beam Shear check:**

$$\text{Allowable shear} = 2 \phi \sqrt{f'_c} B d = 2 \times 0.75 \times \sqrt{3000} \times (5 \times 12) \times 27 / 1000 = 133.09 \text{ k}$$

According to the Shear force diagram, maximum shear force occurs at the left side of the interior support.

So the shear force at 27" from the interior support is = 198.84K > 133.09K (Not Ok)

Increase the footing thickness.

Try t = 40". So, d = 40 - 3 = 37"

$$\text{Allowable shear} = 2 \phi \sqrt{f'_c} B d = 2 \times 0.75 \times \sqrt{3000} \times (5 \times 12) \times 37 / 1000 = 182.39 \text{ k}$$

Shear force at 37" from the interior support is = 168.44K < 182.09K (Ok)

**Punching Shear check:**

Punching Shear is resisted by an area on which column sides down scratching the footing.

For a column, the area of punching is composed of four vertical surface that have width equal to column dimension + d/2

$$\text{Allowable shear} = 4 \phi \sqrt{f'_c} \phi b_0 d = 4 \times .75 \times \sqrt{3000} \times [2\{16 + 37/2\} + 2\{20 + 37/2\}] \times 37 = 851 \text{ K}$$

Resisting Shear = Column load – upward force

$$= 340 - 7.232 \times \left(\frac{16 + 37/2}{12}\right) \times \left(\frac{20 + 37/2}{12}\right) = 273.3 \text{ K} \ll 851 \text{ K (OK)}$$

**Step 4: Reinforcement Calculation**

**Longitudinal direction:**

According to bending moment diagram, maximum -ve moment = 579.60 Kip.

$$\text{Assume, } a = 1.5 \text{ thus } A_s = \frac{M}{\phi f_y (d - a/2)} = \frac{579.60 \times 1000 \times 12}{.9 \times 60000 \times (37 - 1.5/2)} = 3.553 \text{ in}^2$$

$$\text{Check } a, a = \frac{A_s f_y}{.85 f'_c b} = \frac{3.553 \times 60000}{.85 \times 3000 \times 5 \times 12} = 1.393$$

$$\text{Assume } a = 1.4, \text{ thus } A_s = \frac{M}{\phi f_y (d - a/2)} = \frac{579.60 \times 1000 \times 12}{.9 \times 60000 \times (37 - 1.4/2)} = 3.548 \text{ in}^2$$

$$\text{Check } a, a = \frac{A_s f_y}{.85 f'_c b} = \frac{3.548 \times 60000}{.85 \times 3000 \times 5 \times 12} = 1.39 \text{ (ok)}$$

According to bending moment diagram, maximum +ve moment = 771.10 Kip

$$\text{Assume, } a = 1.9 \text{ thus } A_s = \frac{M}{\phi f_y (d - a/2)} = \frac{771.10 \times 1000 \times 12}{.9 \times 60000 \times (37 - 1.9/2)} = 4.753 \text{ in}^2$$

$$\text{Check } a, a = \frac{A_s f_y}{.85 f'_c b} = \frac{4.753 \times 60000}{.85 \times 3000 \times 5 \times 12} = 1.86 = 1.9 \text{ (ok)}$$

Minimum reinforcement:

$$A_{s \text{ min}} = \frac{3 \times \sqrt{f'_c} b d}{f_y} = \frac{3 \times \sqrt{3000} \times 5 \times 12 \times 37}{60000} = 6.079 \text{ in}^2$$

$$A_{s \text{ min}} = \frac{200 b d}{f_y} = \frac{200 \times 5 \times 12 \times 37}{60000} = 7.4 \text{ in}^2$$

So use  $A_s$  7.4 in<sup>2</sup> both in top and bottom along long direction.

If we use #6 or  $\square 20$ , we have to provide  $7.4 / .44 = 16.81 = 17$  pc.

**Use 17-#6 bar along long direction both at top and bottom.**

### Transverse direction:

#### Under interior column:

Transverse length =  $20'' + 2 \times 37/2 = 57'' = 4.75'$

Width of footing =  $5'$

Column Load =  $564 \text{ K}$

Upward pressure from soil along transverse span direction =  $564/5 = 112.8 \text{ k/ft}$

Reinforcement is designed for moment at the face of the column, where bending moment,  $M = wL^2/2 = 112.8 \times 1.666^2/2 = 156.60$

Assume,  $a = .4$  thus  $A_s = \frac{M}{\phi f_y (d-a/2)} = \frac{156.60 \times 1000 \times 12}{.9 \times 60000 \times (37-.4/2)} = 0.946 \text{ in}^2$

Check  $a$ ,  $a = \frac{A_s f_y}{.85 f'_c b} = \frac{0.946 \times 60000}{.85 \times 3000 \times 5 \times 12} = .37 = .4 \text{ (ok)}$

Minimum reinforcement:

$$A_{s \text{ min}} = \frac{3 \times \sqrt{f'_c} \times b \times d}{f_y} = \frac{3 \times \sqrt{3000} \times 57 \times 37}{60000} = 5.775 \text{ in}^2$$

$$A_{s \text{ min}} = \frac{200 \times b \times d}{f_y} = \frac{200 \times 57 \times 37}{60000} = 7.03 \text{ in}^2$$

Use **7.03 in<sup>2</sup>** over longitudinal bar under interior column along 4.75'

**Use 16-#6 under interior column.**

#### Under exterior column:

Transverse length =  $16'' + 2 \times 37/2 = 53'' = 4.416'$

Width of footing =  $5'$

Column Load =  $340 \text{ K}$

Upward pressure from soil along transverse span direction =  $340/5 = 68 \text{ k/ft}$

Reinforcement is designed for moment at the face of the column, where bending moment,  $M = wL^2/2 = 68 \times 1.666^2/2 = 94.368$

Assume,  $a = .23$  thus  $A_s = \frac{M}{\phi f_y (d-a/2)} = \frac{94.368 \times 1000 \times 12}{.9 \times 60000 \times (37-.23/2)} = 0.569 \text{ in}^2$

Check  $a$ ,  $a = \frac{A_s f_y}{.85 f'_c b} = \frac{0.569 \times 60000}{.85 \times 3000 \times 5 \times 12} = .22 = .23 \text{ (ok)}$

Minimum reinforcement:

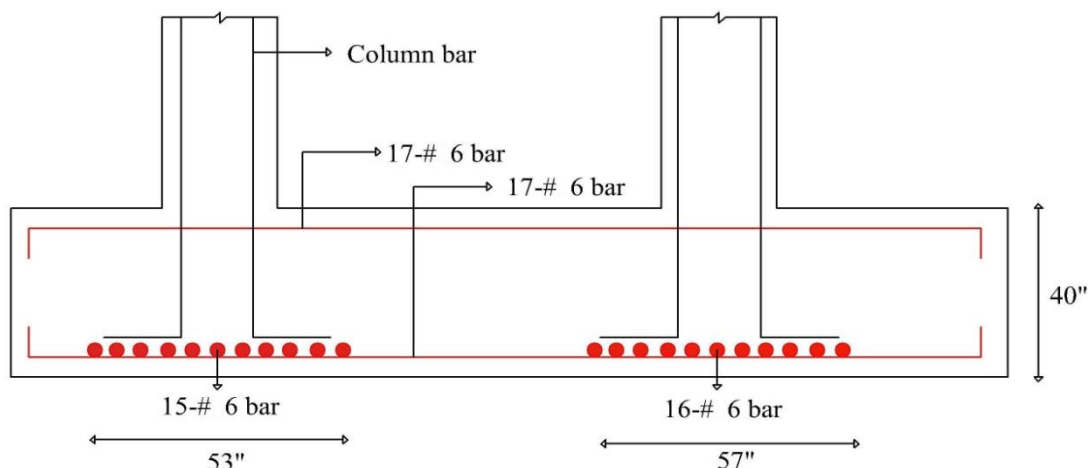
$$A_{s \text{ min}} = \frac{3 \times \sqrt{f'_c} \times b \times d}{f_y} = \frac{3 \times \sqrt{3000} \times 53 \times 37}{60000} = 5.37 \text{ in}^2$$

$$A_{s \text{ min}} = \frac{200 \times b \times d}{f_y} = \frac{200 \times 53 \times 37}{60000} = 6.54 \text{ in}^2$$

Use **6.54 in<sup>2</sup>** over longitudinal bar under interior column along 4.416'

**Use 15-#6 under exterior column.**

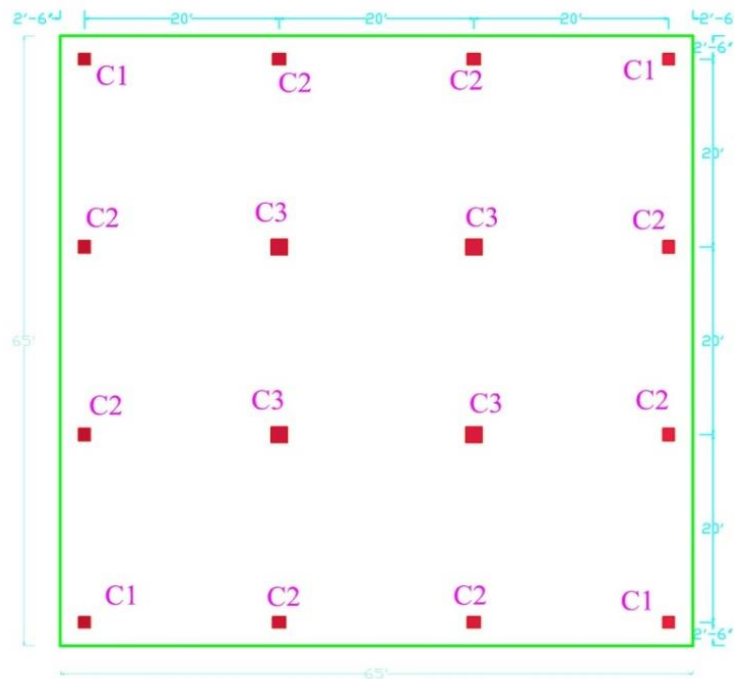
### Step 4: Detailing



## Design of Mat Foundation

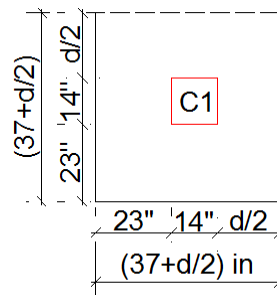
### Problem 4:

A six storied residential building is supported on 16 columns arranged as shown in plan in Fig. Three sized columns used, C1 = 14" \* 14", C2 = 14" \* 16" & C3 = 20" \* 20". For column C1, C2 and C3 the dead loads are: 241Kip, 401Kip and 673kip and live loads are: 47Kip, 89Kip and 168Kip. Concrete compressive strength is 3500 psi and Steel yield strength is 60000 psi. Design the mat foundation.



### **Solution:**

**Determination of Mat thickness by punching shear:  
Punching shear check for corner column C1**



Ultimate Load

$$\begin{aligned}
 P_U &= 1.2 \text{ dead load} + 1.6 \text{ live load} \\
 &= 1.2 * 241 + 1.6 * 47 \\
 &= 364.4 \text{ kip} = 364 \text{ kip}
 \end{aligned}$$

$$\text{Punching perimeter, } b_0 = \left( 37 + \frac{d}{2} \right) * 4$$

$$= (148+2d) \text{ in}$$

According to ACI Code,

$$\phi V_c \geq V_u$$

Where,  $V_c$  = nominal shear strength of concrete

$V_u$  = factored shear strength of concrete

We know,

$$\begin{aligned} \phi V_c &= 4\phi \sqrt{f'_c} b_o \cdot d \\ &= 4 \times 0.85 \times \sqrt{3500} \times (148 + 2d) && [b_o = (37+d/2) \times 4] \\ &= \frac{201.15 \times (148 + 2d) \times d}{1000} \text{ kip} \end{aligned}$$

$$\begin{aligned} V_u &= P_u = 364 \text{ kip} \\ &= \frac{201.15 \times (148 + 2d) \times d}{1000} \geq 364 \\ &= (148+2d) \times d \geq 1811.58 \\ &= 2d^2 + 148d \geq 1811.58 \end{aligned}$$

By solving the equation

$$d_1 = 10.69''$$

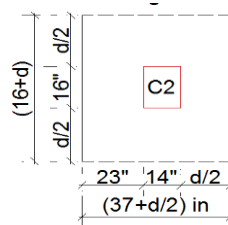
$$d_2 = -84.69''$$

$$d \geq 10.69''$$

Select for design,  $d=12''$

With a minimum cover of 3 inch over the steel reinforcement and 1 inch diameter steel bars, the total slab thickness,  $h = 12+3+1 = 16''$

### Punching Shear for Exterior Column C2



Ultimate Load

$$\begin{aligned} P_u &= 1.2 \text{ dead load} + 1.6 \text{ live load} \\ &= 1.2 \times 401 + 1.6 \times 89 = 623.6 \text{ kip} = 624 \text{ kip} \end{aligned}$$

$$\begin{aligned} \text{Punching perimeter, } b_o &= \left(37 + \frac{d}{2}\right) \times 2 + (16+d) \times 2 \\ &= (148+2d) + 32+2d \\ &= (180+4d) \text{ in} \end{aligned}$$

According to ACI Code,

$$\phi V_c \geq V_u$$

Where,  $V_c$  = nominal shear strength of concrete

$V_u$  = factored shear strength of concrete

We know,

$$\begin{aligned} \phi V_c &= 4\phi \sqrt{f'_c} b_o \cdot d \\ &= 4 \times 0.85 \times \sqrt{3500} \times (180 + 4d) && [b_o = (37+d/2) \times 2 + (16+d) \times 2] \\ &= 201.15 \times (180+4d) \times d \text{ lb} \end{aligned}$$

$$= \frac{201.15 * (180 + 4d) * d}{1000} \text{ kip}$$

$$\begin{aligned} V_u = P_u &= 624 \text{ kip} \\ &= \frac{201.15 * (176 + 4d) * d}{1000} \geq 624 \\ &= (180+4d) d \geq 3100.17 \\ &= 4d^2 + 180d \geq 3100.17 \end{aligned}$$

By solving the equation

$$d_1 = 13.29''$$

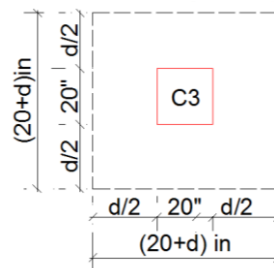
$$d_2 = -58.30''$$

$$d \geq 13.29''$$

Select for design,  $d = 14''$

With a minimum cover of 3 inch over the steel reinforcement and 1 inch diameter steel bars, the total slab thickness,  $h = 14+3+1 = 18''$

### Punching Shear for Interior Column C3



Ultimate Load

$$\begin{aligned} P_u &= 1.2 \text{ dead load} + 1.6 \text{ live load} \\ &= 1.2 * 673 + 1.6 * 168 = 1076.4 \text{ kip} = 1076 \text{ kip} \end{aligned}$$

$$\begin{aligned} \text{Punching perimeter, } b_0 &= (20 + d) * 4 \\ &= (80 + 4d) \\ &= (80 + 4d) \text{ in} \end{aligned}$$

According to ACI Code,

$$\phi V_c \geq V_u$$

Where,  $V_c$  = nominal shear strength of concrete

$V_u$  = factored shear strength of concrete

We know,

$$\begin{aligned} \phi V_c &= 4\phi \sqrt{f'_c} b_0 \cdot d \\ &= 4 * 0.85 * \sqrt{3500} * (20 + d) * 4 * d \quad [b_0 = (37+d/2)*2 + (16+d)*2] \\ &= 201.15 * (80 + 4d) * d \text{ lb} \\ &= \frac{201.15 * (80 + 4d) * d}{1000} \text{ kip} \end{aligned}$$

$$\begin{aligned} V_u = P_u &= 1076 \text{ kip} \\ &= \frac{201.15 * (80 + 4d) * d}{1000} \geq 1076 \\ &= (80 + 4d) d \geq 5351.23 \end{aligned}$$

$$= 4d^2 + 80d \geq 5351.23$$

By solving the equation

$$d_1 = 27.92''$$

$$d_2 = -47.92''$$

$$d \geq 27.92''$$

Select for design,  $d = 28''$

With a minimum cover of 3 inch over the steel reinforcement and 1 inch diameter steel bars, the total slab thickness,  $h = 28 + 3 + 1 = 32''$

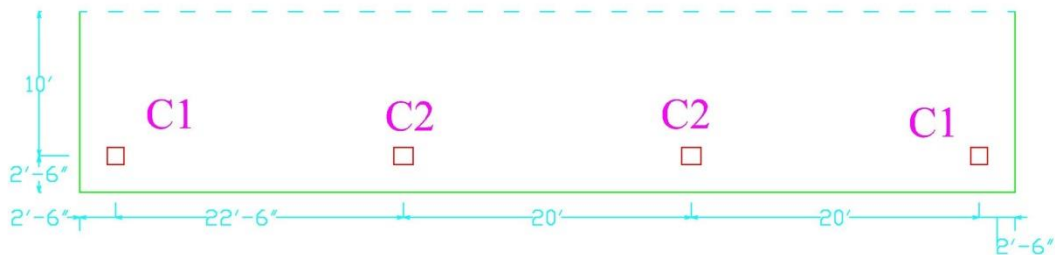
### Final Selection of Mat thickness

Mat thickness for Column	C1	=	16''
	C2	=	18''
	C3	=	32''

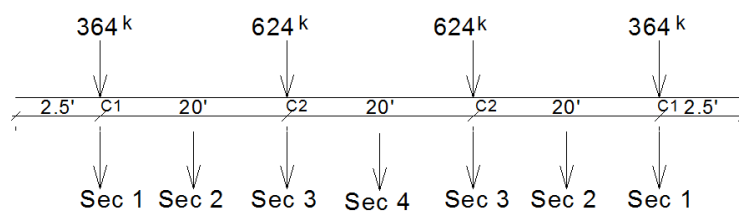
So, the thickness of mat foundation is equal to 32''

### Steel Calculation:

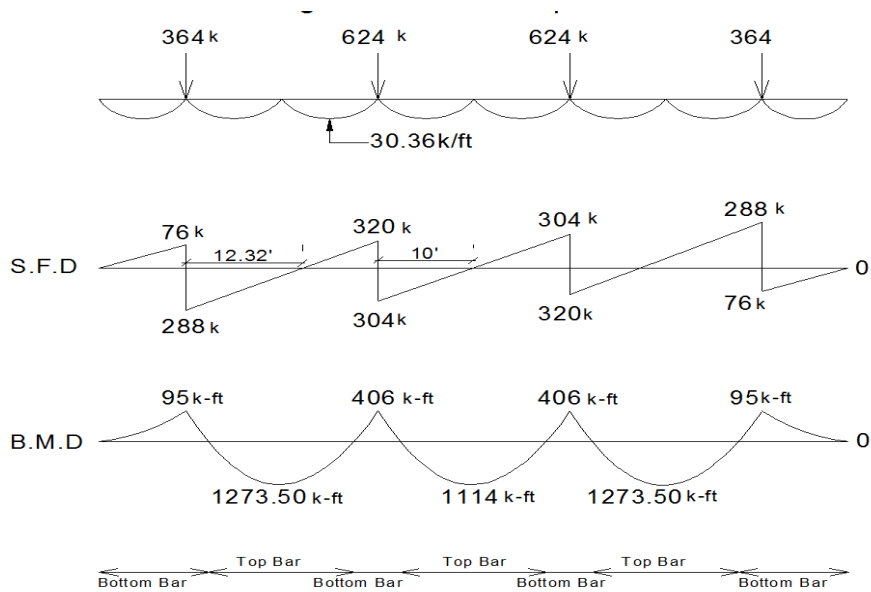
Load diagram for Side Strip of mat foundation (strip size 65' X 12.5'):



### Load diagram:



Shear and moment diagram for side strip:



Moment Chart for Interior panel, Length-65', Width-12.5':

Panel Section	Positive Moment		Negative Moment	
	Total Moment k-ft	Moment k-ft/ft	Total Moment k-ft	Moment k-ft/ft
Section 1	95	7.6		
Section 3	406	32.48		
Section 2			1273.50	101.88
Section 4			1114	89.12

General formula for Steel Calculation

$$A_s = \frac{M_u}{\phi_y (d - a/2)}$$

$$a = \frac{A_s M_u}{0.85 f'_c b}$$

$$A_s = \frac{101.88 * 12}{.9 * 60 (32 - 2/2)} \text{ (Let } a=2 \text{ inch) check, } a = \frac{A_s M_u}{0.85 f'_c b}$$

$$A_s = 0.72 \text{ in}^2 = \frac{.72 * 101.88}{0.85 * 3.5 * 12} = 2 \text{ inch (ok)}$$

Minimum Steel according to ACI Code

$$A_{s, \min} = 0.0018 bt$$

Where, b = 12" and t = total thickness of mat

$$\text{Minimum steel according to ACI code} = 0.0018 * 12 * 32 = 0.69 \text{ in}^2$$

Steel for Interior Panel

Section	Positive Steel (in <sup>2</sup> )		Negative Steel (in <sup>2</sup> )	
Section – 1	0.69	# 5 bar @ 5" c/c		
Section – 3	0.69	# 5 bar @ 5" c/c		
Section – 2			0.72	# 5 bar @5"c/c
Section – 4			0.69	# 5 bar @5"c/c

Do the same for Mid Strip of mat foundation (strip size 65' X 20'):



# **Appendix**

# Appendix 1

## Work to Do

The column-beam layout plan is of a four storied residential building. Different parameters are given below. A soil test report is also provided with this Lab manual.

Slab Thickness: 6"

Columns      C1 = 10" X 10"  
                   C2 = 12" X 12"  
                   C3 = 12" X 14"

Beams         B1 = 12" X 18"  
                   B2 = 12" X 20"

Live Load    = (60 - a) psf

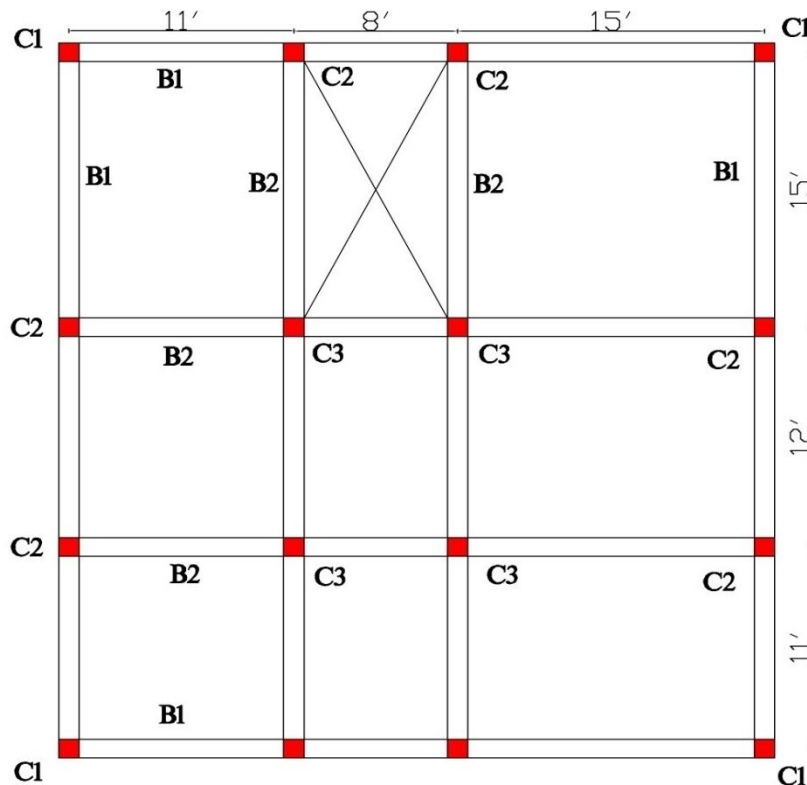
Floor Finish = (25 + a) psf

Partition Wall = (50 + a) psf

$f'_c = (3 + a)$  ksi

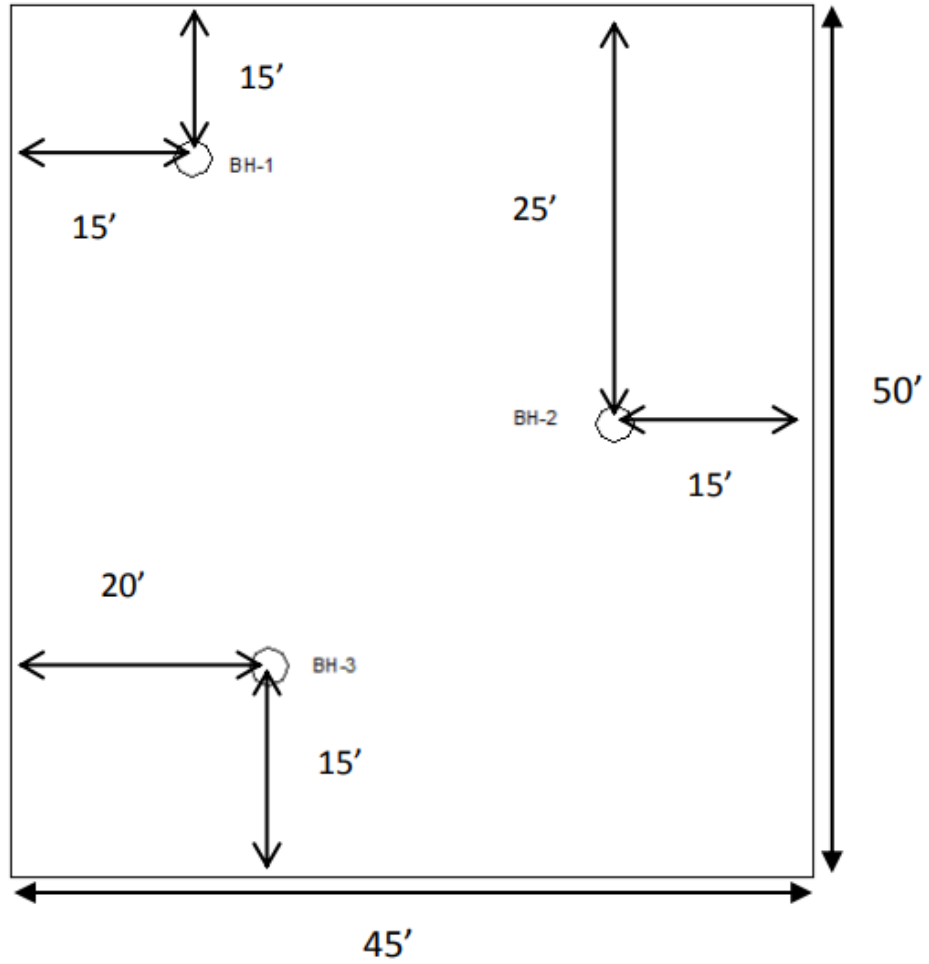
$f_y = (60 - a)$  ksi

**Factor, a = (Last two digits of roll x 0.1)**



1. Calculate the foundation load from each column.
2. Calculate the bearing capacity and footing size if shallow foundation is provided.
3. Calculate the bearing capacity and footing size if deep foundation is provided.
4. Calculate the bearing capacity and footing size if mat foundation is provided.
5. Calculate consolidation settlement for soil under each column and also calculate the differential settlement of columns and check the angular rotation.
6. Design the Isolated footings, Combined Footings, Mat Foundation.

## Appendix 2 Soil Test Report





Site Plan

### SPT Bore Log

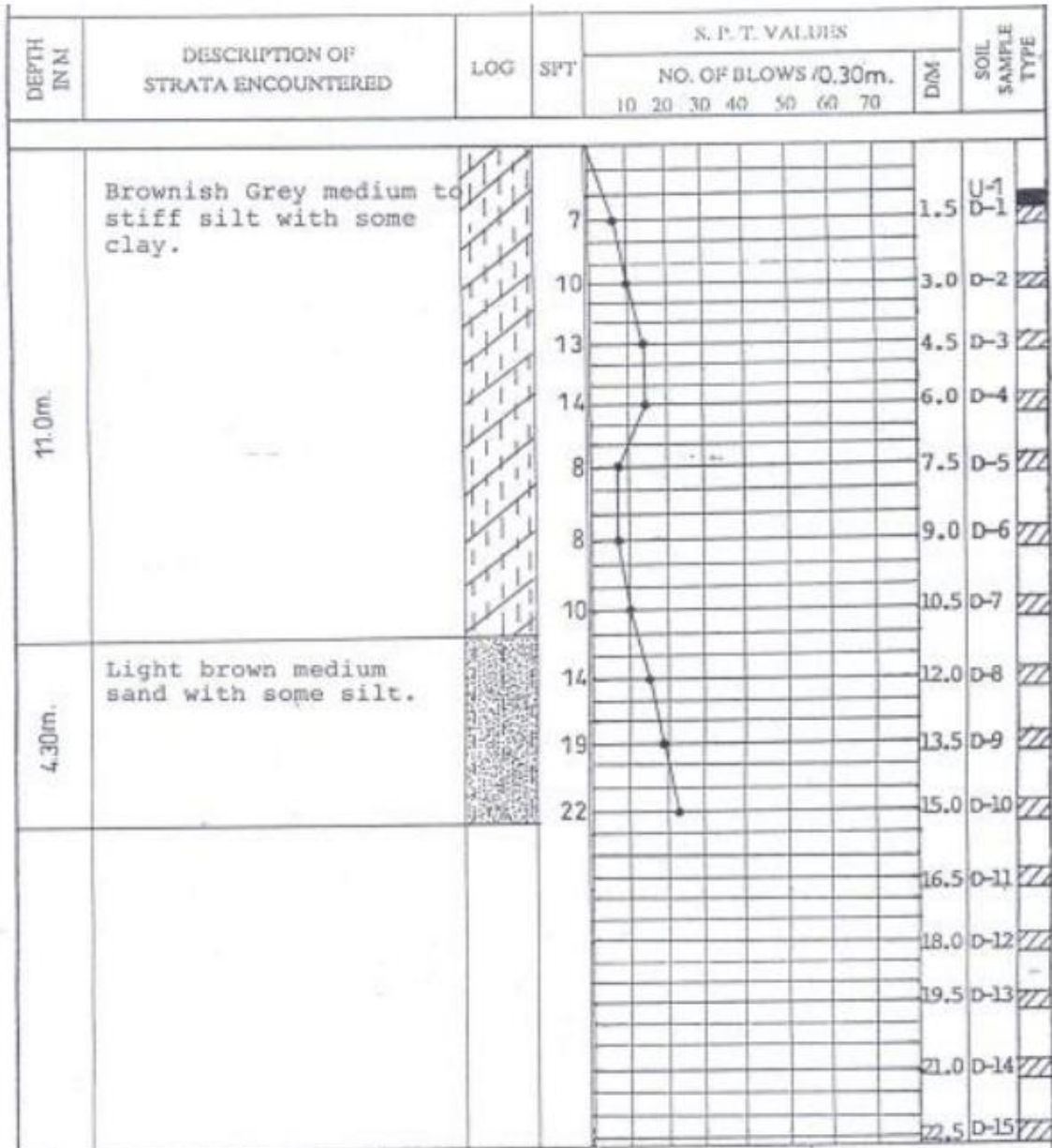
BH No. : 01

Grown Water Table: 1.90 m below

DEPTH IN M	DESCRIPTION OF STRATA ENCOUNTERED	LOG	SPT	S. P. T. VALUES							D/M	SOIL SAMPLE TYPE		
				NO. OF BLOWS /0.30m. 10 20 30 40 50 60 70										
11.0m.	Brownish Grey medium to stiff silt with some clay.		7									1.5	U-1 D-1	
			10										3.0	D-2
			13										4.5	D-3
			14										6.0	D-4
			8										7.5	D-5
			8										9.0	D-6
			10										10.5	D-7
			14										12.0	D-8
			19										13.5	D-9
			22										15.0	D-10
4.30m.	Light brown medium sand with some silt.											16.5	D-11	
												18.0	D-12	
													19.5	D-13
													21.0	D-14
													22.5	D-15


















BH No. : 02

Grown Water Table: 1.90 m below

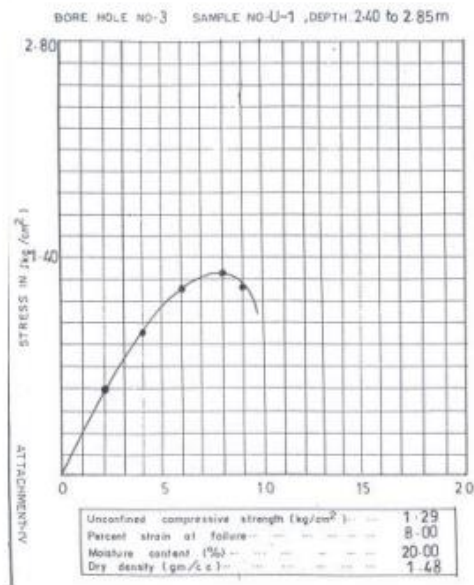
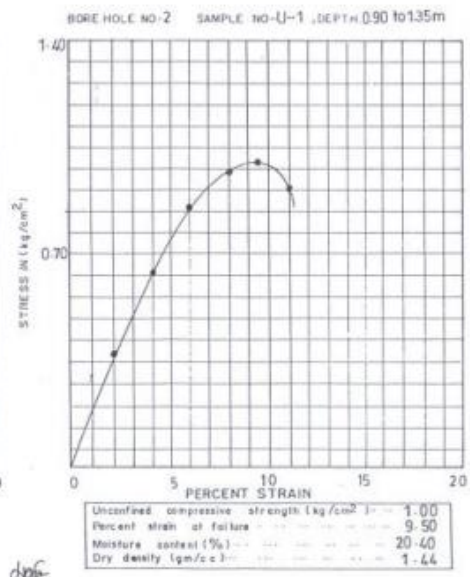
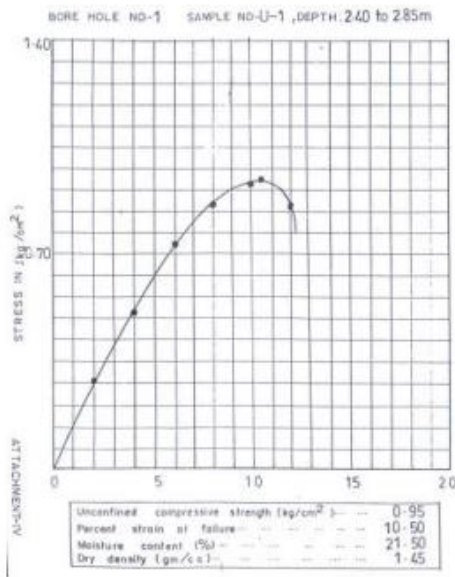


BH No. : 03

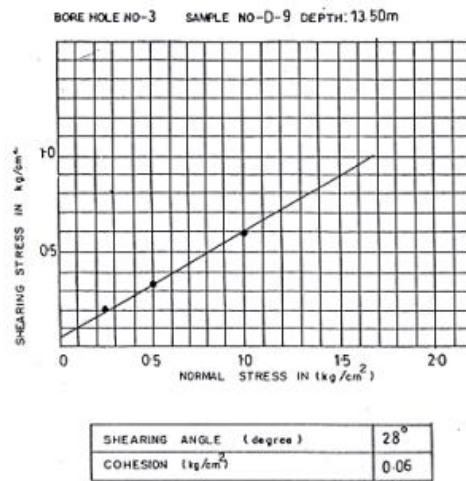
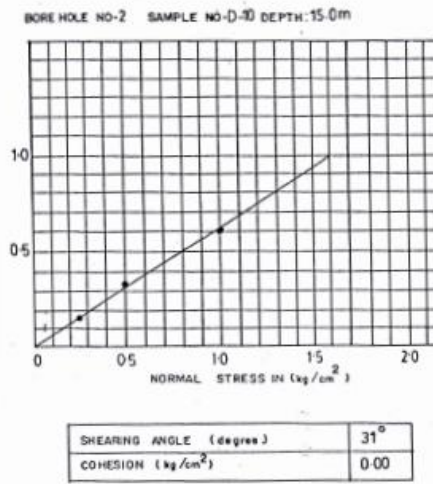
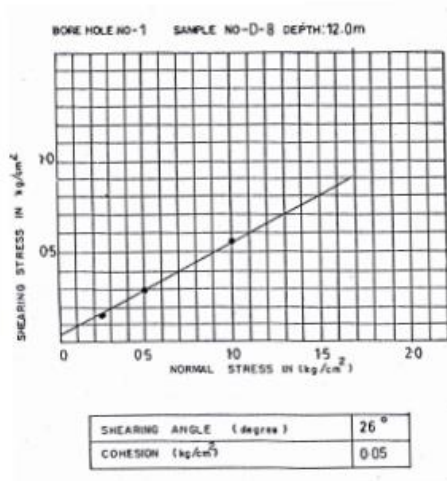
Grown Water Table: 1.78 m below

INCLINATION : VERTICAL		GROUND WATER TABLE : 01.78m. below											
DEPTH IN M	DESCRIPTION OF STRATA ENCOUNTERED	LOG	SPT	S. P. T. VALUES						SOIL SAMPLE TYPE			
				NO. OF BLOWS /0.30m.									
				10	20	30	40	50	60	70	D/M		
10.0m.	Brownish Grey medium to stiff silt with some clay.		7								1.5	D-1	
			9								3.0	U-1 D-2	
			12								4.5	D-3	
			12								6.0	D-4	
			7								7.5	D-5	
			8								9.0	D-6	
			10								10.5	D-7	
5.30m	Light brown medium sand with some silt.		14								12.0	D-8	
			18								13.5	D-9	
			23								15.0	D-10	
											16.5	D-11	
											18.0	D-12	
								19.5	D-13				
								21.0	D-14				
								22.5	D-15				

## Unconfined Compression Test



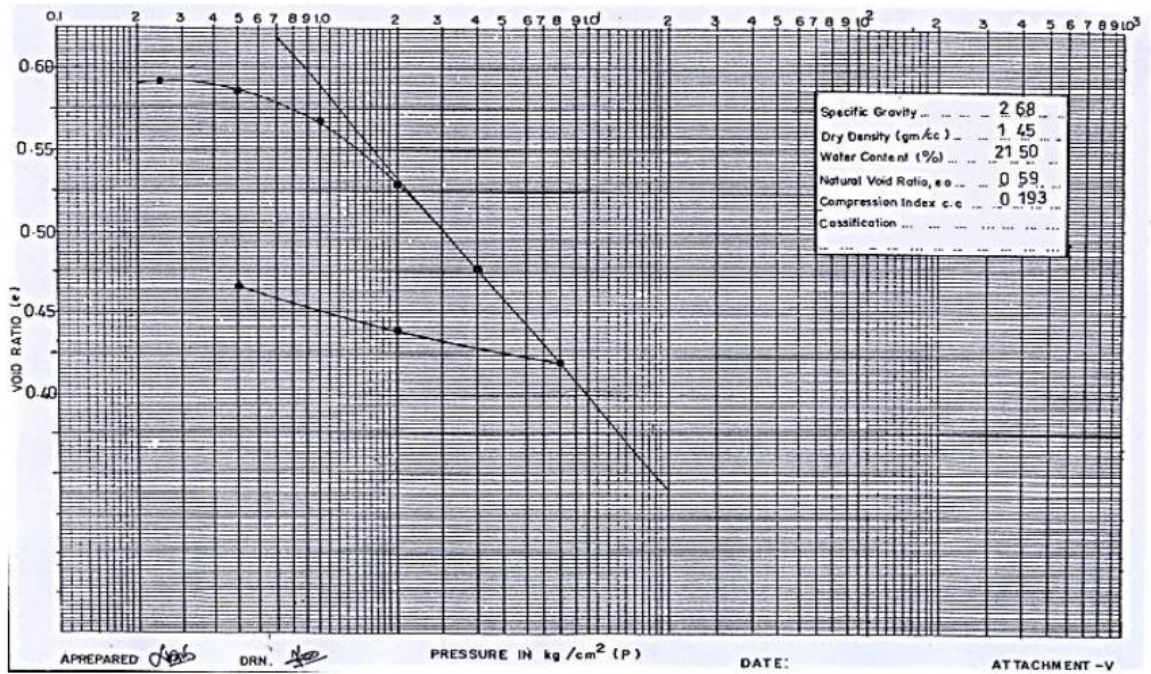
## Direct Shear Test





### Consolidation Test

BH No. : 01  
 Depth: 2.4 m to 2.85 m



## Appendix 3 Geo-properties and Correlations

### Unit weight from SPT

Unit weight of a soil mass is the ratio of the total weight of soil to the total volume of soil.

Unit Weight,  $\gamma$ , is usually determined in the laboratory by measuring the weight and volume of a relatively undisturbed soil sample obtained from a brass ring. Measuring unit weight of soil in the field may consist of a sand cone test, rubber balloon or nuclear densiometer.

Empirical values for  $\gamma$ , of granular soils based on the standard penetration number, (from Bowels, *Foundation Analysis*).

SPT Value/ N-Value	$\gamma$ (lb/ft <sup>3</sup> )
0 - 4	70 - 100
4 - 10	90 - 115
10 - 30	110 - 130
30 - 50	110 - 140
>50	130 - 150

Empirical values for  $\gamma$ , of cohesive soils based on the standard penetration number, (from Bowels, *Foundation Analysis*).

N-Value	$\gamma_{sat}$ (lb/ft <sup>3</sup> )
0 - 4	100 - 120
4 - 8	110 - 130
8 - 32	120 - 140

Typical Soil Characteristics (from Lindeburg, *Civil Engineering Reference Manual for the PE Exam, 8th ed.*)

Soil Type	$\gamma$ (lb/ft <sup>3</sup> )	$\gamma_{sat}$ (lb/ft <sup>3</sup> )
Sand, loose and uniform	90	118
Sand, dense and uniform	109	130
sand, loose and well graded	99	124
Sand, dense and well graded	116	135
glacial clay, soft	76	110
glacial clay, stiff	106	125

Typical Values of Soil Index Properties (from NAVFAC 7.01)

Soil Type	$\gamma$ (lb/ft <sup>3</sup> )	$\gamma_{sub}$ (lb/ft <sup>3</sup> )
Sand; clean, uniform, fine or medium	84 - 136	52 - 73
Silt; uniform, inorganic	81 - 136	51 - 73
Silty Sand	88 - 142	54 - 79
Sand; Well-graded	86 - 148	53 - 86
Silty Sand and Gravel	90 - 155	56 - 92
Sandy or Silty Clay	100 - 147	38 - 85
Silty Clay with Gravel; uniform	115 - 151	53 - 89
Well-graded Gravel, Sand, Silt and Clay	125 - 156	62 - 94
Clay	94 - 133	31 - 71
Colloidal Clay	71 - 128	8 - 66
Organic Silt	87 - 131	25 - 69
Organic Clay	81 - 125	18 - 62

Typical Soil Characteristics (from Lindeburg, *Civil Engineering Reference Manual for the PE Exam, 8th ed.*)

Soil Type	$\gamma$ (lb/ft <sup>3</sup> )	$\gamma_{sat}$ (lb/ft <sup>3</sup> )
Sand, loose and uniform	90	118
Sand, dense and uniform	109	130
sand, loose and well graded	99	124
Sand, dense and well graded	116	135
glacial clay, soft	76	110
glacial clay, stiff	106	125

#### **Angle of Internal Friction from SPT**

Angle of internal friction for a given soil is the angle on the graph (Mohr's Circle) of the shear stress and normal effective stresses at which shear failure occurs.

Angle of Internal Friction,  $\phi$ , can be determined in the laboratory by the *Direct Shear Test* or the *Triaxial Stress Test*.

Typical relationships for estimating the angle of internal friction,  $\phi$ , are as follows:

Empirical values for  $\phi$ , of granular soils based on the standard penetration number, (from Bowels, *Foundation Analysis*).

N-Value	$\phi$ (degrees)
0	25 - 30
4	27 - 32
10	30 - 35
30	35 - 40
50	38 - 43

Relationship between  $\phi$ , and standard penetration number for sands, (from Peck 1974, *Foundation Engineering Handbook*).

N-Value	Density of Sand	$\phi$ (degrees)
<4	Very loose	<29
4 - 10	Loose	29 - 30
10 - 30	Medium	30 - 36
30 - 50	Dense	36 - 41
>50	Very dense	>41

Relationship between  $\phi$ , and N-value for sands, (from Meyerhof 1956, *Foundation Engineering Handbook*).

N-Value	Density of Sand	$\phi$ (degrees)
<4	Very loose	<30
4 - 10	Loose	30 - 35
10 - 30	Medium	35 - 40
30 - 50	Dense	40 - 45
>50	Very dense	>45

### Bearing Capacity factor from Angel of Internal Friction

Bearing capacity is the ability of the underlying soil to support the foundation loads without shear failure.

Bearing capacity factors are empirically derived factors used in a bearing capacity equation that usually correlates with the angle of internal friction of the soil.

Terzaghi's Bearing Capacity Factors

$\phi$	$N_c$	$N_q$	$N_\gamma$
0	5.7	1	0
5	7.3	1.6	0.5
10	9.6	2.7	1.2
15	12.9	4.4	2.5
20	17.7	7.4	5
25	25.1	12.7	9.7
30	37.2	22.5	19.7
34	52.6	36.5	35.0
35	57.8	41.4	42.4
40	95.7	81.3	100.4
45	172.3	173.3	297.5

Meyerhof Bearing Capacity Factors

$\phi$	$N_c$	$N_q$	$N_\gamma$
0	5.14	1.0	0.0
5	6.5	1.6	0.07
10	8.3	2.5	0.37
15	11.0	3.9	1.1
20	14.8	6.4	2.9
25	20.7	10.7	6.8
30	30.1	18.4	15.7
32	35.5	23.2	22.0
34	42.4	29.4	31.2
36	50.6	37.7	44.4
38	61.4	48.9	64.1
40	75.3	64.2	93.7
42	93.7	85.4	139.3
44	118.4	115.3	211.4

Bearing Capacity Factors for Deep Foundations

Meyerhof Values of  $N_q$  For Driven and Drilled Piles

$\phi$	Driven	Drilled
20	8	4
25	12	5
28	20	8
30	25	12
32	35	17
34	45	22
36	60	30
38	80	40
40	120	60
42	160	80
45	230	115

### Cohesion of Soil

Cohesive soils are clay type soils. Cohesion is the force that holds together molecules or like particles within a soil. Cohesion,  $c$ , is usually determined in the laboratory from the *Direct Shear Test*. Unconfined Compressive Strength,  $S_{uc}$ , can be determined in the laboratory using the *Triaxial Test* or the *Unconfined Compression Test*.

There are also correlations for  $S_{uc}$  with shear strength as estimated from the field using *Vane Shear Tests*.  $c = S_{uc}/2$

Where:

$c$  = cohesion,  $kN/m^2$  ( $lb/ft^2$ ), and

$S_{uc}$  = unconfined compressive strength,  $kN/m^2$  ( $lb/ft^2$ ).

Guide for Consistency of Fine-Grained Soil,

N-value	Estimated Consistency	$S_{uc}$ (tons/ $ft^2$ )
<2	Very Soft	<0.25
2 - 4	Soft	0.25 - 0.50
4 - 8	Medium	0.50 - 1.0
8 - 15	Stiff	1.0 - 2.0
15 - 30	Very Stiff	2.0 - 4.0
>30	Hard	> 4

Empirical Values for Consistency of Cohesive Soil, (from Foundation Analysis, Bowels)

N-value	Estimated Consistency	$S_{uc}$ (kips/ $ft^2$ )
0 - 2	Very Soft	0 - 0.5
2 - 4	Soft	0.5 - 1.0
4 - 8	Medium	1.0 - 2.0
8 - 16	Stiff	2.0 - 4.0
16 - 32	Very Stiff	4.0 - 8.0
>32	Hard	>8

Typical Strength Characteristics (from Lindeburg, *Civil Engineering Reference Manual for the PE Exam, 8th ed.*)

USCS Soil Group	$c$ , as compacted ( $lb/ft^2$ )	$c$ , saturated ( $lb/ft^2$ )
GW	0	0
GP	0	0
GM	-	-
GC	-	-
SW	-	-
SP	-	-
SM	1050	420
SM-SC	1050	300
SC	1550	230
ML	1400	190
ML-CL	1350	460
CL	1800	270
OL	-	-
MH	1500	420

**Factor of Safety**

*Foundation Analysis* by Bowles has good recommendations for safety factors. He evaluates uncertainties and assigns a factor of safety by taking into account the following:

1. Magnitude of damages (loss of life and property damage)
2. Relative cost of increasing or decreasing the factor of safety
3. Relative change in probability of failure by changing the factor of safety
4. Reliability of soil data
5. Construction tolerances
6. Changes in soil properties due to construction operations
7. Accuracy (or approximations used) in developing design/ analysis methods

Typical values of customary safety factors, F.S., as presented by Bowles.

<b>Failure Mode</b>	<b>Foundation Type</b>	<b>F.S.</b>
Shear	Earthwork for Dams, Fills, etc.	1.2 - 1.6
Shear	Retaining Walls	1.5 - 2.0
Shear	Sheetpiling, Cofferdams	1.2 - 1.6
Shear	Braced Excavations (Temporary)	1.2 - 1.5
Shear	Spread Footings	2 - 3
Shear	Mat Footings	1.7 - 2.5
Shear	Uplift for Footings	1.7 - 2.5
Seepage	Uplift, heaving	1.5 - 2.5
Seepage	Piping	3 - 5

Other customary factors of safety, F.S., used are:

- 1.5 for retaining walls overturning with granular backfill
- 2.0 for retaining walls overturning with cohesive backfill
- 1.5 for retaining walls sliding with active earth pressures
- 2.0 for retaining walls sliding with passive earth pressures

**Lateral Earth Pressure Coefficient for Soils**

**Piles**

- NAVFAC: 1.0 - 1.5 for a single displacement pile in compression
- USACE: 1.0 - 2.0 for compression piles in sand that are not pre-bored, jetted or vibrated  
1.0 for same conditions except silt  
higher values are for displacement piles
- Broms: 0.5 - 1.0 for low density to high density steel  
1.0 - 2.0 low density to high density concrete  
1.5 - 4.0 low density to high density timber
- Bowles: 0.6 - 1.25. Lower values for silty sands, and higher values for other soils
- Nordlund: uses charts to identify the value for lateral earth pressure coefficients, k, based on the angle of internal friction,  $\phi$ . Ranges from 0.25 to 1.2

Mansure & Hunter: 1.0 - 1.3 for steel pipe piles  
 1.4 - 1.9 for H piles  
 1.45 - 1.6 for precast concrete piles

**Retaining Walls**

$K = (1 - \sin\phi)/(1 + \sin\phi)$  for active earth pressures  
 $K = (1 + \sin\phi)/(1 - \sin\phi)$  for passive earth pressures  
 $K = 1 - \sin\phi$  for at-rest earth pressures  
 where  $\phi$  = angle of internal friction of the soil (degrees)

**Young's Modulus of Soil**

The modulus of elasticity or Young's modulus of a soil is an elastic soil parameter most commonly used in the estimation of settlement from static loads.

Young's soil modulus,  $E_s$ , may be estimated from empirical correlations, laboratory test results on undisturbed specimens and results of field tests. Laboratory tests that may be used to estimate the soil modulus are the triaxial unconsolidated undrained compression or the triaxial consolidated undrained compression tests. Field tests include the plate load test, cone penetration test, standard penetration test (SPT) and the pressuremeter test. Empirical correlations summarized from USACE EM 1110-1-1904 is presented below:

$E_s = K_c C_u$   
 where:  $E_s$  = Young's soil modulus (tsf)  
 $K_c$  = correlation factor  
 $C_u$  = undrained shear strength, tsf

Typical Elastic Moduli of soils based on soil type and consistency/ density, (from USACE, *Settlement Analysis*).

Soil	$E_s$ (tsf)
very soft clay	5 - 50
soft clay	50 - 200
medium clay	200 - 500
stiff clay, silty clay	500 - 1000
sandy clay	250 - 2000
clay shale	1000 - 2000
loose sand	100 - 250
dense sand	250 - 1000
dense sand and gravel	1000 - 2000
silty sand	250 - 2000

## **Appendix 4**

### **Lab Report Format**

1. All students must have a same colored printed **cover page**. The design of cover page is provided with the lab manual. Students have to compose only the course teacher's name and designation and their information.
2. An **index** is provided. It should be printed and set after the cover page. Table may be filled up by pen during each submission after test.
3. Each report must have a common printed **top page**. Only the experiment name and no. and the date may be filled up by pen. A top page design is provided.
4. **A4 papers** have to be used for preparing the lab report. Writing should be done with **pen**. Pencil may be used for any kind of sketch.





# CE 442

## Geotechnical Engineering Sessional II



**Prepared For**  
Name of Course Teacher  
Designation of Course Teacher  
&  
Name of Course Teacher  
Designation of Course Teacher

**Prepared By**  
Name of Student  
Student's ID  
Year/ Semester  
Group

# INDEX

Sl No.	Topic	Date of Submission	Signature	Comments	Page no.



# CE 344

## Geotechnical Engineering Sessional-I (Lab Report)

Experiment No. :  
Experiment Name :

Date of Performance :  
Date of Submission :

**Prepared For**  
Name of Course Teacher  
Designation of Course Teacher  
&  
Name of Course Teacher  
Designation of Course Teacher

**Prepared By**  
Name of Student  
Student's ID  
Year/ Semester  
Group

## **Lab Instructions**

1. All students must have to be present at design class just in time.
2. All students must have to submit the lab report just after the entrance and before the class start.
3. Lab reports have to be submitted serially according to Student's ID.
4. All students must have to bring the lab manual in the class.